$$
\begin{gathered}
\text { Year } 10 \\
\text { Probability } \\
\text { Concepts \& } \\
\text { Tables }
\end{gathered}
$$



## Name:



Written by Liz Sneddon

## Language of probability

## Probability

A number that describes the likely
occurrence of an event, measured on a scale from 0 (impossible event) to I (certain event).


## Event

## Something

 which has a number of outcomes.E.g. rolling a die

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## Sample space

A list of all the possible outcomes of an experiment.
E.g. a dice

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## Frequency

the number of times an event occurs


## Outcome

One possible result of an experiment.
E.g. rolling a 6


## $P($ outcome $A)=$

"The probability of getting outcome $A$ is ...:"
$P($ event $)=\frac{\text { number of ways it can happen }}{\text { total number of outcomes }}$
Lur secestan
$\qquad$
_

## Equally likely

Outcomes with the same chance.
E.g. outcomes on this spinner


## Independent

Events that do not affect or are not affected by another event.


Each coin
toss is not affected by the previous coin toss.


Probability is a measure of the chance of an event happening. Probabilities can also be called "proportions", or "chance".
Sometimes the question will explicitly ask for a percentage, but if it just asks for a probability, then ANY of these forms is correct. Choose which form YOU prefer to use.

Here is a reminder about how to convert numbers between decimals, fractions and percentages. Know how to do this on whichever calculator you use. When rounding your answers, I suggest you round decimal answers to 4.d.p. and percentages to 2.d.p.


Calculate using percentages on the calculator



Rounding to decimal places

Find your place and look next door. 5 or greater, add one more.

All digits in front, stay the same. All digits behind, zero's the name.

## Example:

1) Rolling a die has the following outcomes: $1,2,3,4,5$, or 6 The probability that the number 5 comes up when a die is rolled is:

$P(5$ on an die $)=\frac{1}{6} \quad$ or 0.1667 or $16.67 \%$
2) A bag of marbles has 3 blue and 2 white marbles.

The probability that a blue marble is chosen randomly is:

$$
P(\text { blue })=\frac{3}{5} \quad \text { or } \quad 0.6 \quad \text { or } \quad 60 \%
$$

Theoretical Probability

| A coin: <br> A coin has two sides, heads and tails. | A Spinner: <br> A spinner is a circle (usually) that has been divided up into any number of pieces. |
| :---: | :---: |
| A die (plural: dice): <br> A standard die has 6 sides, with the numbers $1-6$ on each side. You can get die with 10 , 12 , or other numbers of sides. | Random number generator: <br> Your calculator has a random number generator, which can generate a random number between 0 and 1 . |

## A pack of cards:

In a pack of cards there are 4 suites: Diamonds, Hearts, Clubs, Spades
Each suite has 13 cards:
Ace, King, Queen, Jack, 10, 9, 8, 7, 6, 5, 4, 3, 2

| $\begin{aligned} & 2 \\ & 0 \end{aligned}$ | 3 0 | 4 | 5 0 | 6 0 | 7 0 | 8 0 | 9 0 | 10 0 | J | Q $\square$ | $K$ 0 | A $\square$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & 2 \\ & \diamond \end{aligned}$ | 3 | 4 | $5$ | $6$ | $\begin{aligned} & 7 \\ & \diamond \end{aligned}$ | $8$ | $\begin{aligned} & 9 \\ & \diamond \end{aligned}$ | $10$ | J | Q $\diamond$ | K | A |
| 2 4 | 3 | 4 4 | 5 | 6 8 | 7 4 | 8 8 | 9 4 | 10 4 | J | Q 4 | K 4 | A 4 |
| 2 | 3 | 4 | 5 | 6 4 | 7 4 | 8 | 9 4 | 10 4 | J | Q | K ¢ | A 4 |

## Example:

Write the sample space for the following:

1) A single dice

2) A spinner

3) Two dice

Sample space $=1,2,3,4,5,6$

Sample space $=A, B, C, D$

Sample space:


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| $\bullet$ | $\because$ | $\because$ | $\stackrel{\circ}{\circ}$ | $\because$ | $\because$ $\because$ | ! |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\stackrel{\circ}{\circ}$ |  |  |  | $\begin{aligned} & \because: \\ & \because \end{aligned}$ | $\because$ | ! |
| : | $\stackrel{\circ}{\therefore}$ | $\because$ | $\because$ | $\because$ | $\because$ | ! |
| $\because$ | $\because$ | $\because$ | $\because$ | $\begin{aligned} & \because: \\ & \because \end{aligned}$ | $\begin{aligned} & \because \\ & \because \end{aligned}$ | : |
| ! : | $\stackrel{\bullet}{\vdots}$ | $\vdots$ | $\stackrel{\bullet}{\vdots}$ | $\begin{aligned} & \text { : } \\ & \vdots \vdots \end{aligned}$ | $\begin{aligned} & \because \because \\ & : \vdots \end{aligned}$ | : |

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## Exercise 1:

1) Write down the sample space for the following objects:
a)

b)

c)

A 20-sided dice

d)

e) A bag of black and white

2) Write the sample space for each of the following.
a) selecting a day of the week
b) selecting a month of the year
c) rolling a die once
d) tossing a coin once
e)
choosing a letter from the alphabet

|  |
| :--- |
|  |
|  |
|  |

3) The letters of the word MATHEMATICS are written on cards and turned face down. A card is then selected at random.
a)
b)

| Write the sample space. |  |
| :--- | :--- |
| How many elements are in the sample space? |  |
| How many different elements are in the sample <br> space? |  |

4) For each of the following, state whether each element of the sample space is equally likely to occur (circle your answer).
a) tossing a coin
b) rolling a die
c) the result of a cricket game between two teams
d) selecting a card from a normal pack of cards

| Equally likely / not equally likely |
| :--- |
| Equally likely / not equally likely |
| Equally likely / not equally likely |
| Equally likely / not equally likely |

5) Complete the table below for the sample space for a dice and a spinner.

6) Complete the table below for the sample space for a dice and a spinner.

7) A card is chosen at random from a full pack of cards (see the diagram below).

| $\begin{aligned} & 2 \\ & 0 \end{aligned}$ | 3 0 | 4 0 | 5 0 | 6 0 | 7 $\square$ | 8 | 9 0 | 10 $\Gamma$ | J | $Q$ 0 | K $\square$ | A 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | J | Q | K | A |
| $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ |
| 2 4 | 3 4 | 4 | 5 4 | 6 4 | 7 4 | 8 4 | 9 4 | 10 4 | J | Q 4 | K 4 | A 4 |
| $2$ | 3 | 4 | 5 | 6 4 | 7 | 8 | 9 | 10 4 | J ¢ | Q + | K ¢ | A ¢ |

a) What is the probability that the card I select is a king?
b) What is the probability that the card I select is an Ace?
c) What is the probability that the card I select is a Diamond?
d)

| What is the probability that the card I select is a <br> Black card? |  |
| :--- | :--- |
| What is the probability that the card I select is a 5 <br> (five)? |  |
| What is the probability that the card I select is the 8 <br> of hearts? |  |

8) A bag contains 6 blue marbles, 10 orange marbles and 4 red marbles. If a marble is picked randomly, what is the probability of getting:
a)

| A blue marble? |  |
| :--- | :--- |
| An orange marble? |  |
| A red marble? |  |

## NOT probabilities

Let's take a moment to understand the terminology.


## Example:

1) 

The probability of having sunshine tomorrow is $75 \%$. What is the chance that we do NOT have

$$
\begin{aligned}
& P(\text { NOT sunshine })=100 \%-75 \% \\
& =25 \%
\end{aligned}
$$

sunshine tomorrow?
2)

The probability of being late to school is 0.2 .
What is the chance of NOT being late?
$P($ NOT late $)=1-0.2$
$=0.8$

## Exercise 2:

1) 

What is the chance of tossing a coin and NOT getting a Head?
2)
3)

The chance of Mrs Sneddon having takeaways for dinner on Friday night is $34 \%$. What is the chance that she does NOT have takeaways this coming Friday?
4) What is the chance of rolling a die and NOT getting a 3 ?

## AND probabilities

Let's take a moment to understand the terminology.


Remember to convert percentages into decimals or fractions before multiplying.

## Example:

If a student has Instagram AND Snapchat, that means they have BOTH Apps.

## Example:

1) The probability of having sunshine tomorrow is $75 \%$. The probability that it is windy tomorrow is $20 \%$. What is the chance that tomorrow is sunny AND windy?
$P($ sunny AND windy $)=P($ sunny $) \times P($ wind $y)$
$=75 \% \times 20 \%$
$=0.75 \times 0.2$
$=0.15$
$=15 \%$
2) 

The probability of being late to school is 0.2 , and the chance of being late to class is 0.05 . What is the chance of being late to school AND late to class?
$P($ school AND class $)=P($ school $) \times P($ class $)$
$=0.2 \times 0.05$
$=0.1$

## Exercise 3:

1) What is the chance of tossing a coin twice and getting a head AND a Tail?
2) 

What is the chance of tossing a coin twice and getting TWO heads?
3) What is the probability of choosing two cards randomly (with replacement) and getting a Jack AND a heart?
4)
5)

Dr Sneddon has 2 pairs of shoes for work, a black pair and a brown pair. He has three pairs of work socks, one black, one blue and one red. Find the probability of him wearing brown shoes and red socks.

Seth, Anna and Zoe go to Kent's café and buy a drink each. They can choose from Coke, Sprite and L\&P. It is equally likely as to which drink they buy. Find the probability that all 3 of them buying a Coke.

## OR probability

Let's take a moment to understand the terminology.


## Example:

If a student has Instagram $\mathbf{O}$ snapchat, that means they have ONEOR
BOTH of the Apps.


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## Example:

1) The probability of having sunshine tomorrow is $75 \%$. The probability that it is windy tomorrow is $20 \%$. What is the chance that tomorrow is sunny OR windy?
$P($ sunny OR windy $)=P($ sunny $)+P($ windy $)$
$=75 \%+20 \%$
$=90 \%$
2) 

The probability of being late to school is 0.2 , and the chance of being late to class is 0.05 . What is the chance of being late to school OR late to class?
$P($ school OR class $)=P($ school $)+P($ class $)$
$=0.2+0.05$
$=0.25$

## Exercise 4:

1) What is the chance of tossing a coin twice and getting a head OR a Tail?
2) 

What is the probability of choosing two cards randomly (with replacement) and getting a Jack
OR a heart?
3)

Dr Sneddon has 2 pairs of shoes for work, a black pair and a brown pair. He has three pairs of work socks, one black, one blue and one red. Find the probability of him wearing brown shoes OR red socks.
4)

What is the probability that a card randomly removed from a pack is a heart OR a spade?
5)

A bag contains 5 red marbles, 3 blue marbles, and 2 green marbles. What is the probability a red OR blue marble is drawn?

## Mixed Exercise 1:

1) A bag contains 5 red, 3 blue and 2 white balls. If a ball is drawn at random, find the probability that it is:
a)
```
        P(blue) =
```

b)
$\mathrm{P}($ red $)=$
c)
$\mathrm{P}($ not red $)=$
d) $\quad \mathrm{P}($ blue or red $)=$
e) $\quad \mathrm{P}($ blue and red $)=$
f)
$\mathrm{P}(\mathrm{red}$ and white $)=$
g) $\quad \mathrm{P}($ red or white $)=$
h)
$\mathrm{P}($ blue or white $)=$
i)
$\mathrm{P}($ red and blue and white $)=$
j)
$\mathrm{P}($ red and blue or white $)=$
2) The spinner is spun once. Find the probability that:
a)
b) $\quad \mathrm{P}(\mathrm{B})=$
c)

$\square$
$\mathrm{P}(\mathrm{C})=$
d)
$P(D)=$
e)
$\mathrm{P}(\mathrm{A}$ or B$)=$
f)
$\mathrm{P}(\mathrm{A}$ and B$)=$

g) $\quad P(B$ and $C)=$
h) $\quad \mathrm{P}(\mathrm{A}$ or D$)=$
i) $\quad \mathrm{P}(\mathrm{A}$ and B and C$)=$
j) $\quad \mathrm{P}(\mathrm{A}$ or B or C$)=$
k) $\quad \mathrm{P}(\mathrm{A}$ and B or C$)=$
3) A number is chosen at random from 1 to 10 . Find the probability that the number is:
a) $\square$
d)
$\mathrm{P}($ not 5$)=$
e)
$\mathrm{P}($ more than 7$)=$
f)
$P(2$ or 5$)=$
g) $\quad \mathrm{P}(1,3$, or 5$)=$
h)
i)
$P($ at most 2$)=$
$P($ at least 4$)=$
j)
$\mathrm{P}($ less than 3$)=$
k)
$P($ more than 2$)=$
4) From the letters of the word 'PROBABILITY', one letter is selected at random. What is the probability that the letter is:
a) $\quad \mathrm{P}($ a vowel $)=$
b) $\mathrm{P}($ the letter P$)=$
c) $\mathrm{P}($ the letter P or B$)=$
d) $\mathrm{P}($ the letter M$)=$
5) A card is drawn at random from a normal pack of 52 cards.

| 2 0 | 3 | 4 | 5 | 6 0 | 7 | 8 | 9 0 | 10 | J | $\mathbf{Q}$ 0 | K | A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | J | Q | K | A |
| $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ | $\diamond$ |
| 2 4 | 3 4 | 4 | 5 4 | 6 4 | 7 4 | 8 4 | 9 4 | 10 4 | J 4 | Q | K 4 | A 4 |
| 2 | 3 | $4$ | 5 | $\begin{array}{r}6 \\ \hline\end{array}$ | $7$ | 8 | 9 | 10 | J | Q | K | A + |

Find the probability that the card is:
a)
b)

| $\mathrm{P}($ a diamond $)=$ |
| :--- |
| $\mathrm{P}($ a red card $)=$ |
| $\mathrm{P}($ a king $)=$ |
| $\mathrm{P}($ not a club $)=$ |
| $\mathrm{P}($ a red ace $)=$ |
| $\mathrm{P}($ a 5 of clubs $)=$ |
| $\mathrm{P}($ an 8$)=$ |
| $\mathrm{P}($ Jack, Queen or King $)=$ |
| $\mathrm{P}($ less than 4$)=$ |
| $\mathrm{P}($ not a 5$)=$ |

## Expected value

Let's take a moment to understand the terminology.

## Expected value

When you get your answer, if the variable is discrete, round to a whole number.
E.g. number of people should be a whole number.

## Expected value <br> $$
E(X)=P(X) X \cap
$$

$E(X)$ is the expected value
$P(X)$ is the probability from the sample data or theoretical probability
$n$ is the population size

Remember to convert percentages into decimals or fractions before multiplying.

## Example:

1) 

In the last month $60 \%$ of days were sunny. There are 365 days in a year, how many sunny days do we EXPECT next year?
$E($ sunny $)=P($ sunny $) \times n$
$=60 \% \times 365$
$=0.6 \times 365$

$$
=219 \text { days }
$$


2)

In Term 1, busses were late $6 \%$ of the time. Term 2 has 10 weeks, how many days should the school EXPECT busses to be late?
$E($ late $)=P($ late $) \times n$
$=0.2 \times 10$ weeks $\times 5$ days per week
$=10$ days


## Exercise 5:

If I toss a coin 100 times, how many should I EXPECT to be Tails?
2)
3)

If I randomly choose a card from a full deck 40 times with replacement, how many times should I EXPECT to get diamond?

When Mrs Sneddon ordered pizza for her tutor group in Term one, 6 of the 14 pizzas were Pepperoni. Next term she is sharing her classroom with a second tutor group, with a total of 28 boys. How many Pepperoni pizzas should she EXPECT to order?
4)

Dr Sneddon likes coffee, and the chance that he has a coffee in a break is 1 out of 5 . Teachers get a break before school, at morning tea and a lunch break each day. How many coffee's does he EXPECT to have each week?

Teachers have to do duty twice in our seven-day timetable. If the term has 10 weeks, how many times should a teacher EXPECT to have duty each term?

When we collect data we can display this in a table and calculate probabilities from this data.


## Example:

A Year 9 student collected information about how many pets they have. The information is in the table below.

| Number of pets | Frequency |
| :---: | :---: |
| 0 | 7 |
| 1 | 6 |
| 2 | 14 |
| 3 | 9 |
| 4 | 5 |
| 5 | 4 |
| 6 | 1 |
| Total |  |

a) Work out the total frequency in the table above (which is
the total number of students who were surveyed).

46
b)
c)
d)

|  |  |
| :--- | :--- |
| What is the probability that a randomly selected student <br> has no pets? | $\frac{7}{46}$ |
| What is the chance that a randomly chosen student has 2 <br> pets? | $\frac{14}{46}=\frac{7}{23}$ |
| What is the probability that a randomly selected student <br> has 4 or more pets? | $\frac{5+4+1}{46}=\frac{10}{46}=\frac{5}{23}$ |

e)

What percentage of students have less than 2 pets?

$$
\frac{7+6}{46}=\frac{13}{46}=28.26 \%
$$

## Exercise 6:

1) Students were asked how many burgers that had eaten in the last week. Here are the results.

| Number of burgers | Frequency |
| :---: | :---: |
| 0 | 15 |
| 1 | 23 |
| 2 | 28 |
| 3 | 19 |
| 4 | 15 |
| 5 | 10 |
| 6 | 3 |
| Total |  |

a) Work out the total frequency.
b) What is the probability that a student had 4 burgers last week?
c) What is the probability that a student did not eat any burgers last week?
d) What is the probability that a student had at least 5
burgers last week?
e) What is the probability that a student had less than 3 burgers last week?
f)

What is the probability that a student had 2 or 3 burgers
last week?
g)

SKC has around 2200 students, how many of these would you expect to have had 6 burgers last week?
2) A survey was done on students in NZ and data on their eye colour was collected. ${ }^{1}$ Here are the results.

| Apps | Frequency |
| :---: | :---: |
| Blue | 54 |
| Brown | 90 |
| Green | 22 |
| Grey | 5 |
| Hazel | 29 |
| Total | 200 |

Distribution of Eye.Colour

a) What is the probability that a student has Blue eyes?
b) What is the probability that a student has Grey eyes?
c)
d)

What is the probability that a student doesn't have Green eyes?

[^0]e) What is the probability that two students both have Blue eyes?
f)

SKC has around 2200 students, how many of these would you expect to have Grey eyes?
$\square$

|  |
| :--- |
| SKC has around 2200 students, how many of these <br> would you expect to have Grey eyes? |

3) A survey was done on students in NZ and data on how they get to school in the morning was collected. ${ }^{2}$ Here are the results.

| Travel method | Frequency |
| :---: | :---: |
| Bike | 18 |
| Boat | 1 |
| Bus | 64 |
| Motorcar | 137 |
| Scooter | 11 |
| Skateboard | 1 |
| Train | 3 |
| Walk | 63 |
| Other | 2 |
| Total | 300 |

Distribution of Travel.method.to.school

a)

What is the probability that a student came to school on the train?

[^1]b)

| What is the probability that a student came to school on <br> a boat? |  |
| :--- | :--- |
| What is the probability that a student came to school on <br> a bus or train? |  |
| What is the probability that a student did not walk to <br> school? |  |
| SKC has around 2200 students, how many of these <br> would you expect came to school by car, based on this <br> data? |  |

4) A survey was done on students in NZ and data on what type of watch students have was collected. ${ }^{3}$ Here are the results.

| Watch type | Count |
| :---: | :---: |
| Analog | 3 |
| Digital | 8 |
| Analog and <br> Digital | 2 |
| Smart | 12 |
| Doesn't have a <br> watch | 75 |
| Total | 100 |

Distribution of Watch.type

a) $\square$

[^2]b)

| What is the probability that a student has a smart watch? |  |
| :--- | :--- |
| What is the probability that a student has some kind of <br> digital watch? |  |
| What is the probability that two students chosen at |  |
| random both have a smart watch? |  |
| SKC has around 2200 students, how many of these |  |
| would you expect to have any type of watch? |  |

5) A survey was done on students in NZ and data on students' opinions about how they feel about learning at home versus learning at school was. ${ }^{4}$ Here are the results.

| Opinion | Count |
| :---: | :---: |
| Much worse | 27 |
| Worse | 51 |
| About the same | 76 |
| Better | 50 |
| Much Better | 46 |
| Total | 250 |



[^3]a)

| What is the probability that a student feels about the <br> same? |  |
| :--- | :--- |
| What is the probability that a student feels worse or <br> much worse? |  |
| What is the probability that a student doesn't feel better? |  |
| What is the probability that three students' chosen |  |
| randomly feel much better? |  |
| SKC has around 2200 students, how many of these |  |
| would you expect to prefer learning at home? |  |

## Two-way tables

When we collect categorical data, we can display this in a table format. When we have two categorical variables such as gender and ethnicity, we can display this as a two-way table.

## Example:

## Categorical variable 1



| Cat <br> egor | A |  |  |  |
| :--- | :---: | :--- | :--- | :--- |
| ical <br> vari | Not A |  |  |  |
| able <br> $\mathbf{2}$ | Total |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |

Notice that we always need a column at the end for a total, and a row at the bottom for the total. If you get a table that doesn't have the totals, your first step is to make these.

## Example:

If the two categorical variables are Gender and Ethnicity, then this is how the two-way table might look:

|  |  | Ethnicity |  |  |  |  | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Maori | Pasifika | Pakeha | Asian | Other |  |
| $\begin{gathered} \text { G } \\ \text { en } \\ \text { de } \\ \text { r } \end{gathered}$ | Male |  |  |  |  |  |  |
|  | Female |  |  |  |  |  |  |
|  | Other |  |  |  |  |  |  |
|  | Total |  |  |  |  |  |  |

We need to make sure that the sample space (all outcomes) for each variable is displayed on the table. This is why we have the "Other" categories for both Gender and Ethnicity.

## Exercise 7:

1) If the two categorical variables are Gender and whether you like Statistics (Yes/No), complete the two-way table below:


|  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Total |  |  |  |  |

2) If the two categorical variables are Year level at high school and whether you are right or left-handed, complete the two-way table below:


## Putting data into two-way tables

Once we have the table setup, the next step is to enter the data into the tables.
Remember the total column and the total row, this is where you will put the sizes of each group.

The inside boxes are the combinations of the groups (the AND probabilities)

## Example:

The cells that are shaded are the totals, and the white cells in the middle are the combination categories (AND probabilities).

Step 1: Here is the same table, but I have now filled in the total numbers of each gender and ethnicity.

|  |  | Ethnicity |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Maori | Pasifika | Pakeha | Asian | Other | Total |
| $\begin{gathered} \text { G } \\ \text { en } \\ \text { de } \\ \text { r } \end{gathered}$ | Male |  |  |  |  |  | 243 |
|  | Female |  |  |  |  |  | 251 |
|  | Other |  |  |  |  |  | 6 |
|  | Total | 85 | 40 | 300 | 70 | 5 | 500 |

For example, there are 251 females from this sample of 500 people.

Step 2: Here is the same table, but I have now filled in the combinations of gender and ethnicity.

|  |  | Ethnicity |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Maori | Pasifika | Pakeha | Asian | Other | Total |
| G <br> en <br> de <br> r | Male | 38 | 18 | 152 | 33 | 2 | 243 |
|  | Female | 46 | 21 | 145 | 36 | 3 | 251 |
|  | Other | 1 | 1 | 3 | 1 | 0 | 6 |

For example, there are 46 Maori females in this sample of 500 people.

## Exercise 8:

Answer the questions below about the table shown here.

|  |  | Ethnicity |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Maori | Pasifika | Pakeha | Asian | Other | Total |
| G <br> en <br> de <br> r | Male | 38 | 18 | 152 | 33 | 2 | 243 |
|  | Female | 46 | 21 | 145 | 36 | 3 | 251 |
|  | Other | 1 | 1 | 3 | 1 | 0 | 6 |

a) How many people of Asian ethnicity were in this sample?
b) How many Pasifika males were in this sample?
c) How many people identified their gender as other?
d) How many males are there in this sample?
e) How many people were sampled in total?
f) What percentage of people were Maori?
g) What percentage of people were females?
h)

What percentage of people were Asian males?
2) Dr Sneddon did a survey of the Year 9 and Year 10 students and collected the following information.

|  | Right-handed | Left-handed |
| :---: | :---: | :---: |
| Girls | 188 | 32 |
| Boys | 203 | 37 |

a)

| What two questions do you think <br> she asked? |  |  |
| :--- | :--- | :--- |
|  |  |  |
| What would the categorical <br> variables be? |  |  |
| How many students are there in total? |  |  |
| How many students in Year 9 and 10 are left-handed? |  |  |
| How many boys are there? |  |  |

f)

| What percentage of students are left-handed? |  |
| :--- | :--- |
| What percentage of students are girls who are left-handed? |  |

## Rows and Columns

Each row adds up to its total, and each column adds up to its total. We can use this to help fill in the table if we haven't been given all the information.

Categorical variable 1

|  | B | Not B | Total |  |
| :--- | :---: | :---: | :---: | :---: |
|  <br> Cat <br> egor | $\mathbf{A}$ |  |  |  |
| ical <br> vari <br> able <br> $\mathbf{2}$ | Not A |  |  |  |
|  | Total |  |  |  |
|  |  |  |  |  |

## Categorical variable 1

|  | B | Not B | Total |  |
| :--- | :---: | :---: | :---: | :---: |
| Cat <br> egor <br> ical <br> vari <br> able <br> 2 | A |  |  |  |


| Total |  |  |  |
| :--- | :--- | :--- | :--- |

## Example:

Fill in the table below, using the information that is given.

Mrs Sneddon carried out a survey of her class with 22 students. There were 13 males and 2 students were left-handed. Of the males, one was left-handed.

|  | Handedness |  |  | Total |
| :---: | :---: | :---: | :---: | :---: |
| G <br> en <br> de <br> r |  | Male | Left | Right |
|  | 1 |  | 13 |  |

Once you have the information in the table, you can work out the empty cells by remembering that all rows add up and all columns add up.

|  | Handedness |  |  | Total |
| :--- | :---: | :---: | :---: | :---: |
| G <br> en <br> de <br> r | Male | Female | 1 | Right |

## Exercise 9:

1) Dr Sneddon did a survey of students and collected the following information. Complete the table below.

|  | Left-handed | Right-handed | Total |
| :---: | :---: | :---: | :---: |
| Girls | 188 | 32 |  |
| Boys | 203 | 37 |  |
| Total |  |  |  |

2) Mrs Sneddon did a survey of 100 of her students and found that of the 52 male students, 42 preferred dogs and the others preferred cats. There were 49 students who preferred cats. Complete the table below.

|  | Dog | Cat | Total |
| :---: | :---: | :---: | :---: |
| Males |  |  |  |
| Females |  |  |  |
| Total |  |  |  |

3) A survey was done asking people about whether they preferred their pizza to have a thick crust or thin crust. The pizza company also collected data on what children and adults preferred. They found that from the 120 people surveyed that 60 preferred thin crust. Of the 90 adults, 54 preferred thin crust. Complete the table below.

|  |  |  |  |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

## Two-way tables - putting it together

Once you have constructed the table, then we can extract information to find probabilities and expected values.

Remember that the inside cells are the combinations (the AND probabilities).

## Example:

Mrs Sneddon carried out a survey of her class, here are the results.

|  | Left | Right | Total |
| :---: | :---: | :---: | :---: |
| Male | 1 | 12 | 13 |
| Female | 1 | 8 | 9 |
| Total | 2 | 20 | 22 |

a) What is the probability that a student chosen at random is left-handed?
b)

What is the probability that a student chosen at random is male?

What is the probability that a student chosen at random is a female who is right-handed?
d)

What is the probability that a student chosen at random is a left-handed male?

$$
\frac{1}{22}
$$

e)

What is the probability that a student chosen at random is not a left-handed female?

$$
\frac{1+12+8}{22}=\frac{21}{22}
$$

## Example:

Here are the results of a survey of New Zealanders:

|  | Maori | Pasifika | Pakeha | Asian | Other | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Male | 38 | 18 | 152 | 33 | 2 | 243 |
| Female | 46 | 21 | 145 | 36 | 3 | 251 |
| Other | 1 | 1 | 3 | 1 | 0 | 6 |
| Total | 85 | 40 | 300 | 70 | 5 | 500 |

a) What is the probability that a New Zealander chosen at random is Pakeha?
b) What is the probability that a New Zealander chosen at random identifies their gender as "other"?
$\frac{300}{500}=\frac{3}{5}$
c) What is the probability that a New Zealander chosen at random is a Maori Male?
d) What is the probability that a New Zealander chosen at random is Maori or Pasifika ethnicity?

$$
\frac{85+40}{500}=\frac{125}{500}=\frac{1}{4}
$$

e)

| What is the probability that a New Zealander chosen at random is not |  |
| :--- | :--- |
| Female? | $\frac{500-251}{500}=\frac{249}{500}$ | | What is the probability that a New Zealander chosen at random is a |
| :--- |
| female who is Maori or Pakeha? |

## Exercise 10:

1) Students collected information about their favourite sport to watch on television, and what their gender is.

|  | Soccer | Basketball | Rugby | Total |
| :---: | :---: | :---: | :---: | :---: |
| Male | 15 | 22 | 40 | 77 |
| Female | 12 | 16 | 45 | 63 |
| Total | 27 | 38 | 85 | 140 |

a) What is the probability that a student chosen at random prefers Soccer?
b) What is the probability that a student chosen at random is Female?
c) What is the probability that a student chosen at random is a male who prefers Basketball?
d) What is the probability that a student chosen at random prefers Rugby or Soccer?
e) What is the probability that a student chosen at random does not like Soccer?
f) What is the probability that a student chosen at random is a male who likes soccer or basketball?
g) If there are 2200 students at our school, how many do you expect to like Rugby?
2) Data was collected on what type of TV show people preferred to watch.

|  | Dance | Sports | Movies | Total |
| :---: | :---: | :---: | :---: | :---: |
| Women | 16 | 6 | 8 | 30 |
| Men | 2 | 10 | 8 | 20 |
| Total | 18 | 16 | 16 | 50 |

a) What is the probability that a person chosen at random likes to watch Sports?
b) What is the probability that a person chosen at random is a man?
c) What is the probability that a person chosen at random is a woman who likes to watch dancing?
d) What is the probability that a person chosen at random likes to watch sports or movies?
e) What is the probability that a person chosen at random is a woman that likes to watch dance or a movie?
f) What is the probability that a person chosen at random is not a man who likes to watch sports?
g) If there are 2200 students at our school, how many do you expect to prefer to watch movies?

## 3) A survey was done on students about whether they eat breakfast or not and

 their age group.|  | Eat breakfast | Skip breakfast | Total |
| :---: | :---: | :---: | :---: |
| Age $\mathbf{1 0}-\mathbf{1 3}$ | 40 | 14 |  |
| Age $\mathbf{1 4}-\mathbf{1 7}$ | 12 | 24 |  |
| Total |  |  |  |

a) What is the probability that a student chosen at random eats breakfast?
b) What is the probability that a student chosen at random is aged 10-13?
c) What is the probability that a student chosen at random is aged 14-17 and skips breakfast?
d) What is the probability that a student chosen at random is aged 14-17 and eats breakfast or is aged 10-13 and skips breakfast?
e) What is the probability that two students chosen (with replacement) at random both skip breakfast?
f)

| What is the probability that a student chosen at random is |
| :--- | :--- |
| not aged 14-17? |

4) A survey was done looking at how many drinks (Tea, coffee or water) were consumed each weekday (Monday - Friday) for staff at school during the term.

|  | Monday | Tuesday | Wednesday | Thursday | Friday | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Tea | 34 |  | 28 | 36 | 41 |  |
| Coffee |  | 32 | 38 | 24 |  | 167 |
| Water | 33 | 34 | 35 |  | 34 | 181 |
| Total | 109 | 101 |  | 105 | 106 | 522 |

a)

| What is the probability that a randomly chosen staff <br> member had tea during the week? |  |
| :--- | :--- |
| What is the probability that a randomly chosen staff <br> member had coffee on Thursday? |  |
| What is the probability that a randomly chosen staff <br> member had water during the middle of the week (Tuesday <br> to Thursday)? |  |
| What is the probability that a randomly chosen staff <br> member had tea or coffee during the whole week? |  |

e) What is the probability that a randomly chosen staff member did not have a drink of water?
f) What is the probability that a randomly chosen staff member had coffee on Monday or Friday?
g) If there are 200 staff at our school, how many do you expect to be drinking coffee during the week?
5) A survey was carried out exploring preferred flavours of ice-cream.

|  | Chocolate | Vanilla | Neither | Total |
| :---: | :---: | :---: | :---: | :---: |
| Children | 40 |  | 15 | 77 |
| Teens |  | 16 |  |  |
| Adults | 55 |  | 10 | 119 |
| Total | 107 |  | 70 | 269 |

a) What is the probability that a person chosen at random prefers vanilla ice-cream?
b) What is the probability that a person chosen at random is a teenager?
c) What is the probability that a person chosen at random is a teenager who doesn't like either flavour?
d) What is the probability that a person chosen at random is an adult who prefers chocolate ice-cream?
e)

| What is the probability that a person chosen at random |
| :--- | :--- |
| either likes vanilla or chocolate ice-cream? | | What is the probability that a person chosen at random is |
| :--- |
| either a child who likes chocolate ice-cream or a teenager |
| who likes chocolate ice-cream? |

6) Data was collected about whether students played sports (or not) and whether they drank soft drinks (or not). There were a total of 43 people who said they played sports, and from these 19 drank soft drinks. There were 33 people who did not play sport but did drink soft drinks, and 22 people who did not play sports and did not drink soft drinks.

|  |  |  | Total |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
|  |  |  |  |
| Total |  |  |  |

a) Complete the table above.
b) What is the probability that a person chosen at random drinks soft drinks?
c)

| What is the probability that a person chosen at random <br> plays sports? |  |
| :--- | :--- |
| What is the probability that a person chosen at random <br> plays sports but does not drink soft drinks? |  |
| What is the probability that a person chosen at random <br> does not play sport and does not drink soft drinks? |  |
| What is the probability that two people chosen (with <br> replacement) at random both play sports and drink soft <br> drinks? |  |
| If there are 2200 students at our school, how many do you |  |
| expect to not play sports and not drink soft drinks? |  |

7) A group of Aucklanders were surveyed, asking whether they preferred McDonald's, Burger King or Wendy's. Their gender was also recorded. From the 40 people who preferred McDonalds, they were evenly split between males and females. From the 45 males in the survey, 10 preferred Wendy's. From the 100 people in the survey, 25 preferred Burger King.

|  |  |  |  | Total |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |
|  |  |  |  |  |
| Total |  |  |  |  |

a) Complete the table above.
b) What is the probability that a person chosen at random prefers Wendy's?
c)

What is the probability that a person chosen at random is a female who prefers McDonalds?
d) What is the probability that a person chosen at random is a male who prefers Burger King?
e) What is the probability that a person chosen at random is a male who either prefers McDonalds or Burger King?
f) What is the probability that a person chosen at random doesn't prefer Burger King?
g) What is the probability that two people chosen (with replacement) at random both prefer Wendy's?
h) If there are 2200 students at our school, how many do you expect to be females who prefer Wendy's?
8) 42 Year Nine and Ten students were surveyed about how they get to school. Of the 24 who were in Year Nine, 10 came by car, 8 came by bus, and the rest walked to school. From the Year 10 students, 7 caught the bus, 5 walked, and the rest came in a car. There were 16 students altogether who came by car.

|  |  |  |  | Total |
| :---: | :--- | :--- | :--- | :--- |
|  |  |  |  |  |
|  |  |  |  |  |
| Total |  |  |  |  |

a) Complete the table above.
b) What is the probability that a student chosen at random came by bus?
c) What is the probability that a student chosen at random was in Year 10 and came by car?
d)
e)

What is the probability that a student chosen at random was Year Nine and walked to school?
f)

What is the probability that a student chosen at random either came by car or bus?
g) What is the probability that two students chosen (with replacement) at random were both Year 10 's who came on the bus?
h) If there are 2200 students at our school, how many do you expect to be Year Nine's who walked to school?

## Conditional probability (Extension)

There is one final type of probability that we need to cover, conditional probabilities.
A conditional probability is when you want to focus on a part of the data. For example, if I have data on the results of all students at SKC, I might want to focus just on the girls, and find the percentage of who pass Statistics, GIVEN that they are a girl.

## Conditional probability

An event that consists of the occurrence of one event based on
E.g. Given that you missed the school bus, what is the chance you are late to school? the knowledge that another event has already occurred.


| $P(A \mid B)=\frac{P(A B)}{P(B)}$ |  |  |  |
| :--- | :--- | :--- | :--- |
| $B$ | $A$ |  |  |
|  |  |  |  |
|  |  |  |  |

## Example:

Mrs Sneddon carried out a survey of her class, here are the results.

|  | Left | Right | Total |
| :---: | :---: | :---: | :---: |
| Male | 1 | 12 | 13 |
| Female | 1 | 8 | 9 |
| Total | 2 | 20 | 22 |

## Question:

Given that a female was chosen randomly, what is the chance that she is right-handed?

Step 1: The word given tells us the condition: Female.
Now we want to highlight and focus only on the row with females in it.

|  | Left | Right | Total |
| :---: | :---: | :---: | :---: |
| Male | 1 | 12 | 13 |
| Female | 1 | 8 | 9 |
| That | 2 | 20 | This group total (9) is the <br> denominator in your <br> probability. |

Step 2: Now find the combination of Female and Right-handed.

|  | Left | Right | Total |
| :---: | :---: | :---: | :---: |
| Male | 1 | 12 | 13 |
| Female | 1 | 8 | 9 |
| Total | 2 | 20 | 22 |

Step 3: Find the probability of Right-handed given Female.

$$
P(\text { Right }- \text { handed } \mid \text { Female })=\frac{P(\text { Right-handed } \& \text { Female })}{P(\text { Female })}
$$

$=\frac{8}{9}$

## Example:

Here are the results of a survey of New Zealanders:

|  | Maori | Pasifika | Pakeha | Asian | Other | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Male | 38 | 18 | 152 | 33 | 2 | 243 |
| Female | 46 | 21 | 145 | 36 | 3 | 251 |
| Other | 1 | 1 | 3 | 1 | 0 | 6 |
| Total | 85 | 40 | 300 | 70 | 5 | 500 |

Question: Given that a person of Pasifika ethnicity was chosen randomly, what is the chance that the person is a male?

Step 1: The word given tells us the condition: Pasifika.
Now we want to focus only on the column with Pasifika in it.

|  | Maori | Pasifika | Pakeha | Asian | Other | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Male | 38 | 18 | 152 | 33 | 2 | 243 |
| Female | 46 | 21 | 145 | 36 | 3 | 251 |
| Other | 1 | 1 | 3 | 1 | 0 | 6 |
| Total | 85 | 40 | 300 | 70 | 5 | 500 |

Step 2: Now find the combination of Pasifika and Male.

|  | Maori | Pasifika | Pakeha | Asian | Other | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Male | 38 | 18 | 152 | 33 | 2 | 243 |
| Female | 46 | 21 | 145 | 36 | 3 | 251 |
| Other | 1 | 1 | 3 | 1 | 0 | 6 |
| Total | 85 | 40 | 300 | 70 | 5 | 500 |

Step 3: Find the probability of Pasifika given Male.

$$
P(\text { Male } \mid \text { Pasifika })=\frac{P(\text { Pasifika \& Male })}{P(\text { Pasifika })}
$$

$=\frac{18}{40}$
$=\frac{9}{20}$

## Exercise 11:

1) Students collected information about their favourite sport to watch on television, and what their gender is.

|  | Soccer | Basketball | Rugby | Total |
| :---: | :---: | :---: | :---: | :---: |
| Male | 15 | 22 | 40 | 77 |
| Female | 12 | 16 | 45 | 63 |
| Total | 27 | 38 | 85 | 140 |

a) Given that a person likes Basketball, what is the probability that they are male?
b) For a randomly selected Female, what is the probability that they prefer to watch Soccer?
c) What is the chance that a randomly selected male likes rugby?
d) From students who prefer Rugby, what percentage are male?
e) What is the chance that a randomly selected person is female, given they prefer Soccer?
2) Data was collected on what type of TV show people preferred to watch.

|  | Dance | Sports | Movies | Total |
| :---: | :---: | :---: | :---: | :---: |
| Women | 16 | 6 | 8 | 30 |
| Men | 2 | 10 | 8 | 20 |
| Total | 18 | 16 | 16 | 50 |

a) For a randomly selected man, what is the chance that they prefer to watch sports?
b) Given that a person prefers to watch sports, what is the probability that they are a man?
c) What is the probability that a randomly chosen women prefers to watch Movies?
d) What is the probability that a randomly chosen person is female, given they prefer to watch dance?
e) For people who prefer to watch movies, what is the probability that they are male?
3) A survey was done on students about whether they eat breakfast or not and their age group.

|  | Eat breakfast | Skip breakfast | Total |
| :---: | :---: | :---: | :---: |
| Age $\mathbf{1 0}-\mathbf{1 3}$ | 40 | 14 |  |
| Age $\mathbf{1 4} \mathbf{- 1 7}$ | 12 | 24 |  |
| Total |  |  |  |

a) What is the probability that a randomly chosen student who skips breakfast is aged between 14 and 17 ?
b) For a randomly selected student aged between 10 and 13 , what is the chance that they eat breakfast?
c)

Given that a student eats breakfast, what is the
probability that they are aged between 10 and 13
d) What is the probability that a randomly chosen
student skips breakfast, given they are aged between
14 and 17 ?
e)

For students who skip breakfast, what is the probability of them being between 14 to 17 ?
4) A survey was done looking at how many drinks (Tea, coffee or water) were consumed each weekday (Monday - Friday) for staff at school during the term.

|  | Monday | Tuesday | Wednesday | Thursday | Friday | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Tea | 34 |  | 28 | 36 | 41 |  |
| Coffee |  | 32 | 38 | 24 |  | 167 |
| Water | 33 | 34 | 35 |  | 34 | 181 |
| Total | 109 | 101 |  | 105 | 106 | 522 |

a)

| Given that a staff member drinks tea, what is the <br> probability that they drank on Thursday? |  |
| :--- | :--- |
|  |  |

b) What is the probability that a randomly chosen coffee drinker had a drink on Friday?
c) On a Monday, what is the chance that a randomly selected staff member drinks water?
d) For staff who drank on Tuesday, what is the probability of them drinking tea?
e) What is the probability that it is Thursday, given that a staff member is drinking water?
5) A survey was carried out exploring preferred flavours of ice-cream.

|  | Chocolate | Vanilla | Neither | Total |
| :---: | :---: | :---: | :---: | :---: |
| Children | 40 |  | 15 | 77 |
| Teens |  | 16 |  |  |
| Adults | 55 |  | 10 | 119 |
| Total | 107 |  | 70 | 269 |

a)

Given that a person prefers Chocolate, what is the probability that they are a child?
b) What is the probability that a randomly chosen teenager prefers chocolate?
c) What is the probability that a randomly chosen person is an adult, given that they prefer vanilla?
d)

For those people who don't like either chocolate or vanilla, what is the probability of them being an adult?
e) For a randomly selected child, what is the chance that they don't like chocolate?

ANSWERS

Exercise 1:
1)
a)
c)
e)

| yellow, green, blue, red |
| :--- |
| $1,2,3,4,5,6,7,8,9,10,11,12,13,14, ~ 15, ~$ <br> $16,17,18,19,20$ |
| black ball 1, black ball 2, black ball 3, white <br> ball, 1, white ball 2 |

2) 

a)

| Monday, Tuesday, Wednesday, Thursday, <br> Friday, Saturday, Sunday |
| :--- |
| Heads, tails |
| a, b c, d, e, f, g, h, i, j, k, l, m, n, o, p, q, r, s, t, <br> $u, v, w, x, y, z$ |

3) 

a)
$M, A, T, H, E, M, A, T, I, C, S$
4)
a)
c)

| Heads are tails are both equally likely |
| :---: |
| Not equally likely |

b) $1,2,3,4,5$
d) $1,2,3,4,5,6,7,8,9,10,11,12,13,14,15$,
$16,17,18,19,20,21,22,23,24,25,26,27$, $28,29,30,31,32,33,34,35,36,37,38,39$, 40
b)

January, February, March, April, May, June, July, August, September, October, November, December
d)
$1,2,3,4,5,6$
b)

c) 8
b) Each element (1, 2, 3, 4, 5, 6) are equally likely
d) Equally likely
5)

|  |  | Dice |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\bullet$ | $\bullet$ | $\bullet^{\bullet}$ | $\cdots$ | $\cdots$ | $\bullet$ 0 <br> 0 8 |
| Spi <br> nne <br> r | A | 1, A | 2, A | 3, A | 4, A | 5, A | 6, A |
|  | B | 1, B | 2, B | 3, B | 4, B | 5, B | 6, B |
|  | C | 1, C | 2, C | 3, C | 4, C | 5, C | 6, C |
|  | D | 1, D | 2, D | 3, D | 4, D | 5, D | 6, D |

6) 

|  |  | Dice |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 5 |  |  |
| Spin <br> ner | Gellow | $\mathrm{Y}, 1$ | $\mathrm{Y}, 2$ | $\mathrm{Y}, 3$ | $\mathrm{Y}, 4$ | $\mathrm{Y}, 5$ |  |  |
|  | Green | $\mathrm{G}, 1$ | $\mathrm{G}, 2$ | $\mathrm{G}, 3$ | $\mathrm{G}, 4$ | $\mathrm{G}, 5$ |  |  |

7) 

a)
c)
e)

| $P($ king $)=4 / 52=1 / 13$ |
| :--- |
| $P($ diamond $)=13 / 52=1 / 4=0.25$ |
| $P(5)=4 / 52=1 / 13$ |

b)
$\mathrm{P}($ Ace $)=4 / 52=1 / 13$
d)
$\mathrm{P}($ Black $)=26 / 52=1 / 2=0.5$
f)

```
P}(8\mathrm{ of hearts })=1/5
```

8) 

a)
$P($ blue $)=6 / 20=3 / 10=0.3$
c)
$\mathrm{P}(\mathrm{red})=4 / 20=1 / 5=0.2$

## Exercise 2:

1) $\frac{1}{2}$
2) $\frac{3}{4}$
3) $66 \%$
4) $\frac{5}{6}$

## Exercise 3:

| $\frac{1}{2} \times \frac{1}{2}=\frac{1}{4}=0.25$ | 2)$\frac{1}{2} \times \frac{1}{2}=\frac{1}{4}=0.25$${ }^{1)}$ |
| :--- | :--- |

3) 

$\frac{4}{52} \times \frac{13}{52}=\frac{1}{52}=0.0192$
4) $\frac{1}{2} \times \frac{1}{3}=\frac{1}{6}=0.1667$
5)
$\frac{1}{3} \times \frac{1}{3} \times \frac{1}{3}=\frac{1}{27}=0.0370$

## Exercise 4:

1) | $\frac{1}{2}+\frac{1}{2}=1$ |
| :--- |
| $\frac{1}{2}+\frac{1}{3}=\frac{5}{6}=0.8333$ |
| $\frac{5}{10}+\frac{3}{10}=\frac{8}{10}=0.8$ |
2) 

$\frac{4}{52}+\frac{13}{52}=\frac{17}{52}=0.3269$
4)
$\frac{1}{4}+\frac{1}{4}=\frac{1}{2}=0.5$

## Mixed Exercise:

1) 

a)

| $\frac{3}{10}=0.3$ |
| :--- |
| $\frac{5}{10}=\frac{1}{2}=0.5$ |
| $\frac{3}{10} \times \frac{5}{10}=\frac{3}{20}=0.15$ |
| $\frac{5}{10}+\frac{2}{10}=\frac{7}{10}=0.7$ |
| $\frac{5}{10} \times \frac{3}{10} \times \frac{2}{10}=\frac{3}{100}$ |
| $=0.03$ |

b) $\frac{5}{10}=\frac{1}{2}=0.5$
d) $\frac{3}{10}+\frac{5}{10}=\frac{8}{10}=\frac{4}{5}=0.8$
f) $\frac{5}{10} \times \frac{2}{10}=\frac{1}{10}=0.1$
h) $\frac{3}{10}+\frac{2}{10}=\frac{5}{10}=\frac{1}{2}=0.5$
j) $\frac{5}{10}+\frac{3}{10} \times \frac{2}{10}=\frac{14}{25}$
$=0.56$
2)

| a) | $\frac{1}{2}=0.5$ | b) | $\frac{1}{4}=0.25$ |
| :---: | :---: | :---: | :---: |
| c) | $\frac{1}{8}=0.125$ | d) | $\frac{1}{8}=0.125$ |
| e) | $\frac{1}{2}+\frac{1}{4}=\frac{3}{4}=0.75$ | f) | $\frac{1}{2} \times \frac{1}{4}=\frac{1}{8}=0.125$ |
| g) | $\frac{1}{4} \times \frac{1}{8}=\frac{1}{32}=0.0313$ | h) | $\frac{1}{2}+\frac{1}{8}=\frac{5}{8}=0.625$ |
| i) | $\frac{1}{2} \times \frac{1}{4} \times \frac{1}{8}=\frac{1}{64}=0.0156$ | j) | $\frac{1}{2}+\frac{1}{4}+\frac{1}{8}=\frac{7}{8}=0.875$ |

3) 

| a) | $\frac{1}{10}=0.1$ | b) | $\frac{5}{10}=0.5$ | c) | $\frac{2}{10}=\frac{1}{5}=0.2$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| d) | $\frac{9}{10}=0.9$ | e) | $\frac{3}{10}=0.3$ | f) | $\frac{2}{10}=\frac{1}{5}=0.2$ |
| g) | $\frac{3}{10}=0.3$ | h) | $\frac{2}{10}=\frac{1}{5}=0.2$ | i) | $\frac{7}{10}=0.7$ |

j) | $\frac{2}{10}=\frac{1}{5}=0.2$ | k) $\quad \frac{8}{10}=\frac{4}{5}=0.8$ |
| :--- | :--- | :--- |

4) 

a)
b)
$\frac{1}{11}=0.0909$
c) $\frac{3}{11}=0.2727$

| $\frac{4}{11}=0.3636$ |
| :--- |
| 0 |

5) 

a)

| $\frac{1}{4}=0.25$ |
| :--- |
| $\frac{3}{4}=075$ |
| $\frac{1}{13}=0.0769$ |
| $\frac{12}{13}=0.9231$ |

b)
$\frac{1}{2}=0.5$
c) $\frac{1}{13}=0.0769$
e) $\frac{1}{26}=0.0385$ $\frac{1}{52}=0.0192$
h) $\frac{3}{13}=0.2308$
i)
k) $\frac{50}{52}=\frac{25}{26}=0.9615$

Exercise 5:

| 1) | $E=100 \times \frac{1}{2}=50$ tails |
| :---: | :---: |
| 3) | $\begin{aligned} E= & 28 \times \frac{6}{14} \\ & =12 \text { Pepperoni Pizza's } \end{aligned}$ |
| 5) | $\begin{aligned} & E=10 \times 5 \times \frac{2}{7} \\ & =14.3 \\ & =14 \text { or } 15 \text { duties } \end{aligned}$ |

2) $E=40 \times \frac{1}{4}=10$ diamonds
3) 


1)
a)

| 113 |
| :--- |
| $\frac{15}{113}=0.1327$ |
| $\frac{15+23+28}{113}=\frac{66}{113}$ <br> $=0.5841$ |
| $E=2200 \times \frac{3}{113}$ <br> $=58.4$ <br> $=58$ or 59 students |

b)
d)

| $\frac{15}{113}=0.1327$ |
| :--- |
| $\frac{13}{113}=0.1150$ |
| $\frac{28+19}{113}=\frac{47}{113}=0.4159$ |

b)

| $\frac{5}{200}=0.025$ |
| :--- |
| $\frac{200-22}{200}=\frac{178}{200}=0.89$ |
| $E=2200 \times \frac{5}{200}$ <br> $=55$ students |

b) $\frac{1}{300}=0.0333$
d)

e)
$E=2200 \times \frac{137}{300}$
$=1004.7$
$=1004$ or 1005 students
4)
a)
c)
$\frac{8+2}{100}=\frac{10}{100}=0.1$
e)
$E=2200 \times \frac{25}{100}$
$=550$ students
b)
$\frac{12}{100}=0.12$
5)

a) \begin{tabular}{l|l|}
\hline$\frac{76}{250}=0.304$ <br>

c) $\quad$| $\frac{27+51+76}{250}=\frac{154}{250}=0.616$ |
| :--- | \(\begin{array}{l}E=2200 \times \frac{50+46}{250} <br>

=844.8 <br>
=844 or 845 students\end{array}\) <br>
\hline
\end{tabular}

b) $\frac{27+51}{250}=\frac{78}{250}=0.312$
d) $\frac{46}{250} \times \frac{46}{250} \times \frac{46}{250}=0.00623$

## Exercise 7:

1) 

|  | Gender |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Male | Female | Other | Total |
| Like <br> Stati <br> stics <br> $?$ | Yes |  |  |  |  |

2) 

|  |  | Year level |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 9 | 10 | 11 | 12 | 13 |  |  |
| Ha <br> nd <br> ed <br> nes <br> s | Right |  |  |  |  |  |  |  |

## Exercise 8:

1) 

a)

| 70 |
| :--- |
| 6 |
| 500 |
| $\frac{251}{500} \times 100=50.2 \%$ |

b) 18
d) 243
f) $\frac{85}{500} \times 100=17 \%$
h) $\frac{33}{500} \times 100=6.6 \%$
2)

|  | Right-handed | Left-handed | Total |
| :---: | :---: | :---: | :---: |
| Girls | 188 | 32 | 220 |
| Boys | 203 | 37 | 240 |
| Total | 391 | 69 | 460 |

a) Question 1: whether they were right or left handed.

Question 2: if they were a girl or a boy.
c)
e)
g)

| 240 |
| :--- |
| $\frac{32}{460} \times 100=6.96 \%$ |

b)

| Variable 1: Handedness. |
| :--- |
| Variable 2: Gender. |
| 69 |
| $\frac{69}{460} \times 100=15 \%$ |

## Exercise 9:

1) 

|  | Left-handed | Right-handed | Total |
| :---: | :---: | :---: | :---: |
| Girls | 188 | 32 | 220 |
| Boys | 203 | 37 | 240 |
| Total | 391 | 69 | 460 |

2) 

|  | Dog | Cat | Total |
| :---: | :---: | :---: | :---: |
| Males | 42 | 10 | 52 |
| Females | 9 | 39 | 48 |
| Total | 51 | 49 | 100 |

3) 

|  | Thick crust | Thin crust | Total |
| :---: | :---: | :---: | :---: |
| Child | 24 | 6 | 30 |
| Adult | 36 | 54 | 90 |
| Total | 60 | 60 | 120 |

## Exercise 10:

1) 

a) $\frac{27}{140}=0.1929$
c) $\frac{22}{140}=\frac{11}{70}=0.1571$
e)

$$
\frac{140-27}{140}=\frac{113}{140}
$$

$$
=0.8071
$$

g)
$E=2200 \times \frac{85}{140}$
$=1335.7$
$=1335$ or 1336 students
2)
a)
$\frac{16}{50}=\frac{8}{25}=0.32$
$\frac{16}{50}=\frac{8}{25}=0.32$
b) $\frac{63}{140}=\frac{9}{20}=0.45$
d) $\frac{85+27}{140}=\frac{112}{140}=\frac{4}{5}=0.8$
f)

$$
\begin{aligned}
& \frac{15+22}{140}=\frac{37}{140} \\
& =0.2643
\end{aligned}
$$

e)

| $\frac{16+8}{50}=\frac{24}{50}=0.48$ |
| :--- |
| $E=2200 \times \frac{16}{50}$ |
| $=704$ students |

f) $\frac{50-10}{50}=\frac{40}{50}=0.8$
g)

$$
=704 \text { students }
$$ $\frac{50-10}{50}=\frac{40}{50}=0.8$

|  | Eat breakfast | Skip breakfast | Total |
| :---: | :---: | :---: | :---: |
| Age $\mathbf{1 0}-\mathbf{1 3}$ | 40 | 14 | 54 |
| Age $\mathbf{1 4} \mathbf{- \mathbf { 1 7 }}$ | 12 | 24 | 36 |
| Total | 52 | 38 | 90 |

a)

| $\frac{52}{90}=\frac{26}{45}=0.5778$ |
| :--- |
| $\frac{24}{90}=\frac{4}{15}=0.2667$ |
| $\frac{38}{90} \times \frac{38}{90}=\frac{361}{625}=0.5776$ |
| $E=2200 \times \frac{38}{90}$ <br> $=928.9$ <br> $=928$ or 929 students |

b) $\frac{54}{90}=\frac{3}{5}=0.6$
d)
$\frac{12+14}{90}=0.2889$
f)
e)
$\frac{54}{90}=\frac{3}{5}=0.6$
g)

| Monday | Tuesday | Wednesday | Thursday | Friday | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{e}$ | 34 | 35 | 28 | 36 | 41 |
| $\mathbf{r}$ | 32 | 32 | 38 | 24 | 31 |
|  | 109 | 34 | 35 | 45 | 34 |

a)

| $\frac{174}{522}=\frac{1}{3}=0.3333$ |
| :--- |
| $\frac{34+35+45}{522}=\frac{114}{522}$ |
| $=0.2184$ |
| $\frac{522-181}{522}=\frac{341}{522}$ |
| $=0.6533$ |
| $E=200 \times \frac{167}{522}$ |
| $=63.98$ |

b)
$\frac{24}{522}=\frac{4}{87}=0.0480$
d)

$$
\begin{aligned}
& \frac{174+167}{522}=\frac{341}{522} \\
& =0.6533
\end{aligned}
$$

f)

$$
\frac{42+31}{522}=\frac{73}{522}=0.1398
$$

$$
=63 \text { or } 64 \text { staff }
$$

5) 

|  | Chocolate | Vanilla | Neither | Total |
| :---: | :---: | :---: | :---: | :---: |
| Children | 40 | 22 | 15 | 77 |
| Teens | 12 | 16 | 45 | 73 |
| Adults | 55 | 54 | 10 | 119 |
| Total | 107 | 92 | 70 | 269 |

a)

| $\frac{92}{269}=0.3420$ |
| :--- |
| $\frac{45}{269}=0.1673$ |
| $\frac{107+92}{269}=\frac{199}{269}$ |
| $=0.7398$ |
| $E=12,000 \times \frac{92}{269}$ <br> $=4104.1$ <br> $=4104$ or 4105 people |

b)

| $\frac{73}{269}=0.2714$ |
| :--- |
| $\frac{55}{269}=0.2045$ |
| $\frac{40+12}{269}=\frac{52}{269}=0.1933$ |

6) a)

|  | Sports | No Sports | Total |
| :---: | :---: | :---: | :---: |
| Soft drink | 19 | 33 | 52 |
| No Soft drink | 24 | 22 | 46 |
| Total | 43 | 55 | 98 |

b)

| $\frac{52}{98}=\frac{26}{49}=0.5306$ |
| :--- |
| $\frac{24}{98}=0.2449$ |
| $\frac{19}{98} \times \frac{19}{98}=\frac{361}{9604}$ |
| $=0.0376$ |

c) \begin{tabular}{ll|}
\hline$\frac{43}{98}=0.4388$ <br>
e) \& $\frac{22}{98}=\frac{11}{49}=0.2245$ <br>

\hline \& | $E=2200 \times \frac{22}{98}$ |
| :--- |
| $=493.9$ | <br>

\hline
\end{tabular}

7) a)

|  | McDonalds | Burger King | Wendy's | Total |
| :---: | :---: | :---: | :---: | :---: |
| Male | 20 | 15 | 10 | 45 |
| Female | 20 | 10 | 25 | 55 |
| Total | 40 | 25 | 35 | 100 |

b)

| $\frac{35}{100}=\frac{7}{20}=0.35$ |
| :--- |
| $\frac{15}{100}=\frac{3}{20}=0.15$ |
| $\frac{100-25}{100}=\frac{75}{100}=0.75$ |
| $E=2200 \times \frac{25}{100}$ |
| $=550$ students |

c) $\frac{20}{100}=\frac{1}{5}=0.2$
e) $\frac{20+15}{100}=\frac{35}{100}=0.35$
g) $\frac{35}{100} \times \frac{35}{100}=\frac{49}{400}$
$=0.1225$
8) a)

|  | Car | Bus | Walk | Total |
| :---: | :---: | :---: | :---: | :---: |
| Year 9 | 10 | 8 | 6 | 24 |
| Year 10 | 6 | 7 | 5 | 18 |
| Total | 16 | 15 | 11 | 42 |

b)

| $\frac{15}{42}=0.3571$ |
| :--- |
| $\frac{6}{42}=\frac{1}{7}=0.1429$ |
| $\frac{42-16}{42}=\frac{26}{42}=0.6190$ |
| $E=2200 \times \frac{6}{42}$ <br> $=314.3$ <br> $=314$ or 315 students |

c)

| $\frac{6}{42}=\frac{1}{7}=0.1429$ |
| :--- |
| $\frac{16+15}{42}=\frac{31}{42}=0.7381$ |
| $\frac{7}{42}=\frac{1}{6}=0.1667$ |




[^0]:    ${ }^{1}$ Data from Census At School NZ 2021 Survey

[^1]:    ${ }^{2}$ Data from Census At School NZ 2021 Survey

[^2]:    ${ }^{3}$ Data from Census At School NZ 2021 Survey

[^3]:    ${ }^{4}$ Data from Census At School NZ 2021 Survey

