# Time series investigation for juniors. (Levels 2-6) 

## Name:

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## Problem and Plan

Time series data is about data that is collected over time.

## Exercises:

Problem - I wonder if the Umbrella Shop sells more umbrellas in summer or winter?

Plan - Over the last year, the Umbrella Shop has recorded how many umbrellas they sold each season.

1) Predict what you think the graph may look like on the axis below.

> Spring Summer Autumn Winter
> Time (season)
2) Do you think that this pattern (of bigger sales in winter and smaller sales in summer) would repeat itself every year? Explain why/why not.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
3) Why might it be good to have several years of data to look for patterns?
4) Predict what you think the graph of toy sales might look like on the axis below.



Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec Time (months)
5) Predict what you think the graph of movie ticket sales might look like on the axis below.
y
ñ
N
6) Predict what you think the graph of food sales from a cafe might look like on the axis below.
$\frac{y}{\pi}$
n

## 6am 8am 10am 12noon 2pm 4pm 6pm 8pm

 Time (hours)
## Data

We need two variables:

- time
- either count or measurement data (E.g. sales, economic data, births, etc)


## Exercise:

1) Write down all the different units of time that you can think of.
2) Why would we connect the data points together rather than drawing the co-ordinates separately? Explain.

## Analysis

## Graphs

With time series data, we draw a line graph. The connections between the dots show that the data is connected.

## Line Graph

Below is an example of a line graph.


## How to draw a line graph.

Consider this data set of how many car sales were made each month over the year.

| Month | Car Sales |
| :--- | :--- |
| January | 16 |
| February | 24 |
| March | 22 |
| April | 26 |
| May | 27 |
| June | 31 |
| July | 30 |
| August | 29 |
| September | 34 |
| October | 35 |
| Dovember | 35 |

1) Draw the horizontal axis, putting time on this axis. Remember to label your axis
2) Draw the vertical axis. Look at what your largest data value is. Remember to label your axis
3) Use dots to mark the data points on the axis. Then connect these points together with a line. Your graph should look like the example on the previous page.

## Exercise:

1) Below is data on car sales over the last year, from a car sales yard down the road.

a) Describe how you see this yards car sales.
2) 

b) Is the number of cars sold by a car yard a good indication of how well it is doing? What other factors might be involved?

1) The dataset below shows the total ticket sales from the cinema complex Movietime.

| Day | Date | Tickets sold |
| :--- | :--- | :--- |
| Sunday | June 9 | 622 |
| Monday | June 10 | 205 |
| Tuesday | June 11 | 271 |
| Wednesday | June 12 | 583 |
| Thursday | June 13 | 710 |
| Friday | June 14 | 1416 |
| Saturday | June 15 | 1784 |

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| Sunday | June 16 | 812 |
| :---: | :---: | :---: |
| Monday | June 17 | 407 |
| Tuesday | June 18 | 590 |
| Wednesday | June 19 | 608 |
| Thursday | June 20 | 802 |
| Friday | June 21 | 1196 |
| Saturday | June 22 | 1345 |
| Sunday | June 23 | 310 |
| Monday | June 24 | 414 |
| Tuesday | June 25 | 415 |
| Wednesday | June 26 | 834 |
| Thursday | June 27 | 1221 |
| Friday | June 28 | 1468 |
| Saturday | June 29 | 1582 |

Draw both axes with the appropriate scale and label, and plot the points to create a line graph of movie ticket sales.


3)
c) What does 'total daily ticket sales' mean here?
4)
d) How many movie tickets were sold on June 13th?
5)
e) Do you think more or less tickets were sold on 24 th June than 23 rd?
6)
f) Could it be guaranteed that fewer tickets would be sold on any Monday than would be sold on the Saturday before? Explain why/why not.
7)
2) The dataset below shows the total chemist sales (in millions of dollars) from June 2009 to June 2013.

| Chemist sales (\$million) | 204.6 |
| :--- | :--- |
| Jun-2009 | 211.8 |
| Sep-2009 | 242 |
| Dec-2009 | 226.3 |
| Mar-2010 | 208.9 |
| Jun-2010 | 223.9 |
| Sep-2010 | 236.6 |
| Dun-2012 | 243.8 |
| Sep-2011 | 2010 |
| Mar-2011 | 238.6 |


| Sep-2012 | 250.7 |
| :--- | :--- |
| Dec-2012 | 269.8 |
| Mar-2013 | 251.2 |
| Jun-2013 | 242.3 |

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Draw both axes with the appropriate scale and label, and plot the points to create a line graph of chemist sales.

a) What does 'chemist sales' mean here?
8)
b) How much money was spent in chemists from January 2010 to March 2010?
9)
10)
c) How much money was spent at chemists over all of 2010?
11)
d) Over what months are chemist sales higher?
12)
e) Why would there be more sales in December? Explain.
13)

Analysis
Here are the features you need to analyse.

- Trend
- Seasonality

We will now go through each feature, before putting it all together.

## Trend

1) Draw a trend line through the graph.

- Try to get it through the middle, with about half of the data values above the line, and half below the line.

2) Describe whether the trend (line of best fit) has a positive, negative or zero gradient.
3) Lastly, write a sentence about the trend. Describe:

- The direction - is it going up, down or has no trend
- How much it is increasing or decreasing by.

Sentence Framework:

Level 2 / 3 / 4:
I notice that the data has an increasing/decreasing/no trend.
This is because the line of best fit is going _up / down / straight across

Level 5:
I notice that the context has an increasing / decreasing / no trend.

The line of best fit starts at final trend value.
$\qquad$ initial trend value and changes to
$\qquad$

Level 6:
For every 1 time unit increase, measurement increases / decreases by \# units

Example


Level 2 / 3 / 4:
I notice that the data has an increasing trend. This is because the line of best fit is going up.

Level 5:
I notice that the car sales has an increasing trend.
The line of best fit starts at 21 and changes to 36 .
Level 6:
For every one month increase, the number of car sales increases by 1.3. OR

The number of car sales is increasing by around 15 cars over the year. Seasonality

If you have data that covers more than one time period (for example several years), we can notice if there is a common pattern that occurs each season (e.g. summer, autumn, January, etc).

## STEP 1

Figure out if you have seasons that you can compare. Some examples may be:

Seasons: Summer, Autumn, Winter, Spring.
Months: January, February, March, April, May, June, July, August, September, October, November, December.

Days: Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday. Hours: 1am, 2am, 3am, 4am, 5am, 6am, 7am, 8am, 9am, 10am, 11am, 12noon, 1pm, 2pm, 3pm, 4pm, 5pm, 6pm, 7pm, 8pm, 9pm, 10pm, $11 \mathrm{pm}, 12 \mathrm{pm}$.

## STEP 2

Match up and highlight repeating seasons. For example, match up and highlight all the Spring seasons.

Example

| 2012 |  |  |  | 2013 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Summer | Autumn | Winter | Spring | Summer | Autumn | Winter | Spring |

STEP 3
Notice whether each season (e.g. Summer) is always above, below, or the same as the trend line.

## STEP 4

Write sentences about the seasons. Describe:

- How many seasons there are.
- Whether each season is above, below, or the same as the trend.

STEP 5 (Level 6)
Can you link this to the context, and explain why the seasons may be above or below the trend?

Sentence Framework:
I notice that the data has number seasons. They are: autumn, winter, spring and summer / January, February, etc / Monday, Tuesday, etc / $1 \mathrm{am}, 2 \mathrm{am}, 3 \mathrm{am}$, etc

I notice that season 1 is always the trend.

I notice that season 2 is always above / below / the same as the trend.

Etc.

Example


I notice that there are 4 seasons: March, June, September, December. This means that the March season is the total chemist sales from January, February and March.

The June season is the total chemist sales from April, May and June.
The September season is the total chemist sales from July, August and September.

The December season is the total chemist sales from October, November and December.

## June

I'll start with matching up and highlighting every June.


I notice that the June chemist sales are always under the trend.
This may be because in the months of April, May and June these are the autumn seasons, where people are quite healthy generally speaking after a warm summer. Therefore they don't have big demands on sunscreen (in summer) or flu medication (in winter).

September


I notice that the September chemist sales are either just under the trend or the same as the trend.

This may be because in the months of July, August and September these are the winter seasons, where people purchase more flu medications.


I notice that the December chemist sales are always above the trend.
This may be because in the months of October, November and December these are the spring seasons, where people are still recovering from winter bugs, purchasing sunscreen as the weather gets warmer, and of course in December there is Christmas, and people will likely be purchasing gifts from all shops including the chemist, raising the sales higher than normal.

March


I notice that the March chemist sales are either just under the trend or the same as the trend.

This may be because in the months of January, February and March these are the summer seasons, where people are purchasing more sunscreens.

## Exercise:

1) Here is the graph of movie ticket sales in the last 3 weeks.

a) Draw a trend line through the data in the graph above.
b) What does the trend line show?

I notice ... $\qquad$

Here is the graph drawn again with a trend line added. You now want to look at the seasons.

a) What are the seasons, and how many are there for this data? 14)
15)
16)
b) Match up and highlight all the Monday movie ticket sales. What do you notice?
17) I notice ...
c) Match up and highlight all the Tuesday movie ticket sales. What do you notice?
18) I notice ....
d) Match up and highlight all the Wednesday movie ticket sales. What do you notice?
19) I notice ...
e) Match up and highlight all the Thursday movie ticket sales. What do you notice?
20) I notice ...
f) Match up and highlight all the Friday movie ticket sales. What do you notice?
21) I notice ...
g) Match up and highlight all the Saturday movie ticket sales. What do you notice?
22) I notice ...
h) Match up and highlight all the Sunday movie ticket sales. What do you notice?
23) I notice ...
2) Below is a graph of the amount (in millions of dollars) that people in NZ spent on takeaway foods from 2006 to 2010.

a) Draw a trend line through the data in the graph above.
b) What does the trend line show?

I notice ... $\qquad$

You now want to look at the seasons.
c) What are the seasons, and how many are there for this data? 24)
d) What patterns do you notice with the different seasons?
25) I notice ... $\qquad$
26)
27)

## Conclusion

For your conclusion you need to:

- Make a concluding sentence, stating if there is any trend or seasonality present.
- Discuss variation.
- Discuss which population the sample may be applied to.


## Variation



When we look at time series graphs, the patterns are never exactly the same from year to year.

All data has random variation. Some data sets have very little random variation, and other data sets have a lot of random variation.

Example


Conclusion:
From our sample, we can conclude that a there is an increasing trend from 2009 to 2013, and a seasonality pattern that regularly repeats each year.

Variation is present in this data set as we can see the pattern is not exactly the same each time.

The data is from the total chemist sales in New Zealand from 2009 to 2013. These results may be similar in countries such as Australia.

## Exercise:

Draw conclusions about the following data.

1) Movie ticket sales in the last 3 weeks.

## Movie ticket sales


35)
2) Chemist sales from 2007 to 2010 .


Investigation Exercise

## Problem

I wonder if there are any patterns in our classes' absence data?

## Plan

We will collect data each day, over term the first 4 weeks of term 3.
Then we will record how many students from our class were absent each day.

| Week | Day | Number of absences |
| :---: | :---: | :---: |
| 1 | Monday | 3 |
|  | Tuesday | 2 |
|  | Wednesday | 2 |
|  | Thursday | 1 |
|  | Friday | 2 |
| 2 | Monday | 4 |
|  | Tuesday | 2 |
|  | Wednesday | 1 |
|  | Thursday | 1 |
|  | Friday | 3 |
| 3 | Monday | 4 |
|  | Tuesday | 2 |
|  | Wednesday | 2 |
|  | Thursday | 3 |
|  | Friday | 4 |
| 4 | Monday | 6 |
|  | Tuesday | 4 |
|  | Wednesday | 3 |
|  | Thursday | 3 |
|  | Friday | 5 |

Analysis
Draw a line graph.


Analysis
Describe the trend and seasonality. Justify your description.

## Conclusion

Answer the investigation question.

What does this data suggest about attendance in this class? Can the results be applied to the whole school or other schools in NZ?

