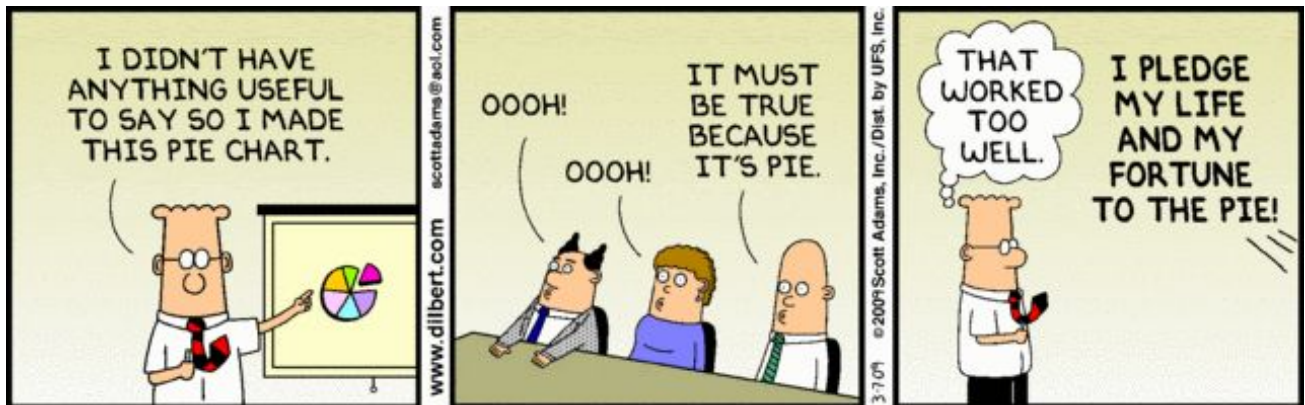


# Year 9 Statistics booklet

Teacher Name: Mrs Meera Phadke

Student Name: \_\_\_\_\_



“Data don't make any sense,  
we will have to resort to statistics.”

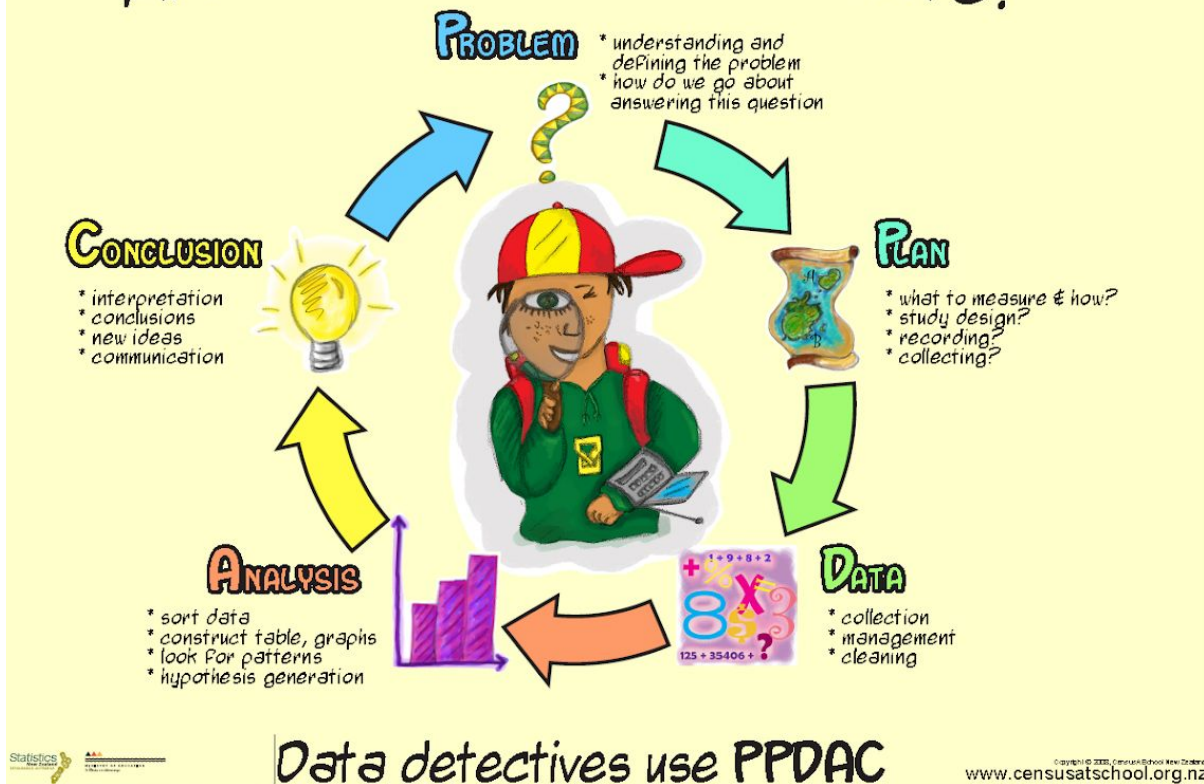
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**Statistical Vocabulary or Glossary:**

Average, Bar Graph, Bias ,Box and whisker plot, Certain, Cluster, Conclusion, Continuous, Comparative questions, Data, Discrete, Distribution, Dot plot, Shape distribution.

Experiment, Event, Frequency, Histogram, Inter-quartile range, Lower quartile, Mean, Median, Outcome, outlier , Pictogram, Pie Graph, Population, Trend, Predict, Probability, Range, Relative frequency, Relationship Questions, Scatter diagrams, Spread, Statistics, Stem and Leaf plot, Skew, Summary questions, Upper quartile, lower quartile, inter quartile.

# Are You a Data Detective?



**PROBLEM:** Write your “I wonder” question here that you are exploring.

**PLAN/DATA:** List the variables you will explore to answer your “I wonder” question.

**ANALYSIS:** From the tables and/or plots/graphs make four I notice statements about the data you have displayed. You should compare the shape of the data, spread of the data, the middle 50% of the data, and the summary statistics.

I notice...

I notice...

I notice...

I notice...

## **CONCLUSION**

Your question you started with (from PROBLEM)...

Answer to your question...

Support for this answer.

## Title: Nosey Parker Part 1

### Introduction/Background as appropriate

Are you a Nosey Parker?

Do you have lots of questions that you want to find the answers to?

We can use statistics to answer all sorts of questions and to investigate lots of ideas.



### Problem



Add your data to the last row of the table.

| Student | Gender | Age | Height (cm) | Length of arm span (cm) | Main way of travel to school* | Time taken to get to school (min) | Did most at lunchtime * |
|---------|--------|-----|-------------|-------------------------|-------------------------------|-----------------------------------|-------------------------|
| 1       | male   | 12  | 163         | 163                     | walk                          | Less 10                           | Ran                     |
| 2       | female | 14  | 155         | 155                     | bus                           | 20 - 30                           | Sat                     |
| 3       | female | 12  | 155         | 155                     | walk                          | 10 - 20                           | Ran                     |
| 4       | male   | 10  | 141         | 144                     | motor                         | Less 10                           | Ran                     |
| 5       | female | 14  | 163         | 164                     | motor                         | 20 - 30                           | Walked                  |
| 6       | male   | 9   | 144         | 144                     | bus                           | 30 plus                           | Walked                  |
| 7       | female | 13  | 164         | 165                     | bus                           | 30 plus                           | Sat                     |
| 8       | female | 14  | 158         | 118                     | motor                         | 10 - 20                           | Sat                     |
| 9       | female | 14  | 166         | 162                     | bus                           | 10 - 20                           | Sat                     |
| 10      | female | 10  | 143         | 138                     | motor                         | 10 - 20                           | Walked                  |
| 11      | male   | 11  | 149         | 144                     | bike                          | Less 10                           | Ran                     |
| 12      | female | 9   | 140         | 140                     | motor                         | 10 - 20                           | Ran                     |
| 13      | male   | 9   | 127         | 128                     | walk                          | 10 - 20                           | Ran                     |
| 14      | male   | 13  | 163         | 163                     | motor                         | 10 - 20                           | Ran                     |
| 15      | female | 13  | 150         | 147                     | walk                          | 10 - 20                           | Ran                     |
| 16      | male   | 11  | 146         | 125                     | bike                          | Less 10                           | Ran                     |
| 17      | male   | 13  | 165         | 154                     | motor                         | Less 10                           | Walked                  |

|    |        |    |     |     |       |         |        |
|----|--------|----|-----|-----|-------|---------|--------|
| 18 | female | 12 | 159 | 159 | motor | Less 10 | Walked |
| 19 | female | 15 | 160 | 156 | walk  | 30 plus | Stood  |
| 20 | male   | 13 | 168 | 175 | walk  | Less 10 | Ran    |
| 21 | female | 15 | 170 | 175 | motor | Less 10 | Sat    |
| 22 | female | 9  | 132 | 130 | motor | Less 10 | Ran    |
| 23 | male   | 14 | 174 | 182 | motor | Less 10 | Ran    |
| 24 | female | 12 | 150 | 150 | bus   | 30 plus | Stood  |
| Me |        |    |     |     |       |         |        |

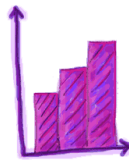
\* Questionnaire wording

**Main way to travel to school options:** walk, motor vehicle, bus, bike, other.

**What you did most at lunchtime options:** sat down, stood around, walked around, ran around or played

Source: CensusAtSchool.org.nz

## Analysis



|              |             |
|--------------|-------------|
| I notice ... | I wonder... |
|--------------|-------------|

|  |  |
|--|--|
|  |  |
|--|--|

## **Reflection**

I thought...

I was surprised...

## **To extend this activity**

Look over all the 'I notice...' and 'I wonder...' statements and sort them into groups. Investigate different ways of sorting and choose the one which seems most useful. Explain your choice.

## Types of investigative questions:

### Relationship Questions/Statements

- I notice that their height is similar to their arm span.
- I wonder if height has anything to do with how long it takes to get to school.
- I notice that the older the students are the taller they are.

### Summary Questions/Statements

- I wonder what the average height of these students is.
- I notice that most students run around at lunchtime.
- I notice that the most common way to get to school is using a motorcar.

### Comparison Questions/Statements

- I wonder if students who walk to school take longer to get to school.
- I wonder if female students are more active at lunchtime than male students.
- I wonder if younger students are more active than older students.
- I wonder if females are shorter than males.

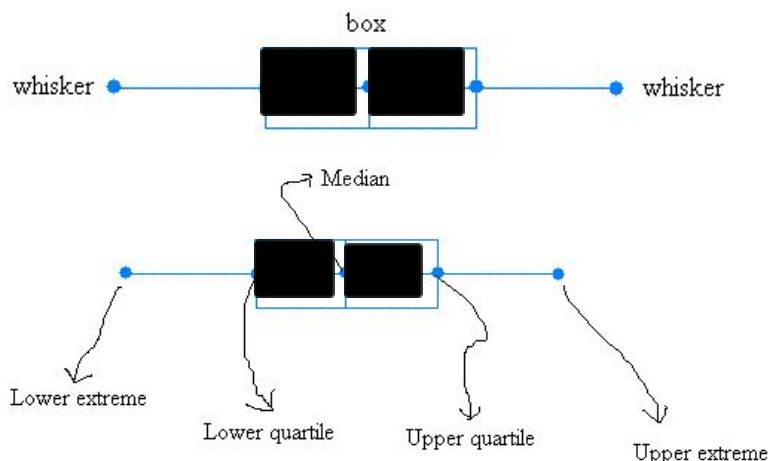
### Other Questions/Statements

- I wonder if students who went to school using a car could have used the bus.
- I wonder if the older students travel further to school than the younger students.
- I wonder if the results would be different for our class.
- I wonder why students don't ride bikes more.

### Where to from here:

Now that we know what sorts of questions we have we can identify the specific data we need and use statistical techniques to analyse the data. Each type of question uses different techniques.

## How to make a box and whisker plot:



**Lower extreme or Minimum:** the lowest or smallest value in a set of data

**Lower quartile or first quartile:** the median of all data below the median

**Median or second quartile:** the middle value of the set of data. If there are two values in the middle, the median is the average of the two values

**Upper quartile or third quartile:** the median of all data above the median

**Upper extreme or Maximum:** The biggest value in the set

### Example:

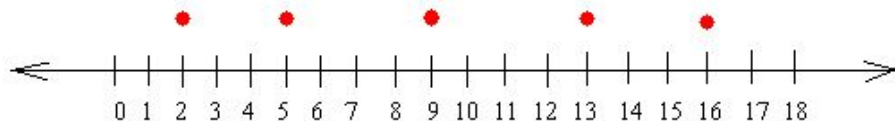
Construct a box and whiskers plot for the data set: {5, 2, 16, 9, 13, 7, 10}

- Put the data set in order from least to greatest  
*From least to greatest we get : 2 5 7 9 10 13 16*
- Since the smallest value in the set is 2, the **lower extreme is 2**  
Since the greatest value in the set is 16, the **upper extreme is 16**
- Now, look carefully at the set: 2 5 7 **9** 10 13 16  
You can see that 9 is located right in the middle of the set of data, therefore, **9 is the median**
- Now to get the lower quartile, you need all data before the median of 9  
**2 5 7** 9 10 13 16  
In bold right above we show all data before 9, so **2 5 7**  
Since the value in the middle for the set **2 5 7** is 5, the **lower quartile is 5**
- Finally, to get the upper quartile, you need all data after the median or 9  
2 5 7 9 **10 13 16**  
In bold right above we show all data after 9, so **10 13 16**  
Since the value in the middle for the set **10 13 16** is 13, the **upper quartile is 13**
- This is called a 5-point statistics and can be summarised as below:

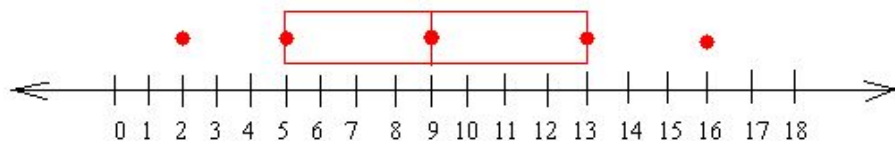
| Minimum | Lower Quartile | Median | Upper Quartile | Maximum |
|---------|----------------|--------|----------------|---------|
| 2       | 5              | 9      | 13             | 16      |



7. Now we make a number line and graph above the number line 2, 5, 9, 13, and 16 with five dots: one dot will represent the median, one dot will represent each extreme, finally, one dot will represent each quartile.

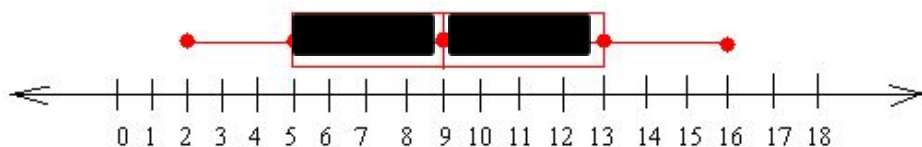


8. Draw a rectangle or box starting from the lower quartile to the upper quartile. Draw a vertical segment too to represent the median



9. Finally, draw horizontal segments or whiskers that connect all five dots together.

The box and whiskers plot for {5, 2, 16, 9, 13, 7, 10} is :



### Creating your own box and whisker plot:

We want to investigate the question ‘How many whiskers does a cat have?’

- We find cats with the following number of whiskers: 27, 21, 23, 25, 24, 23, 28, 27, and 20 whiskers
- Rearrange the numbers in numerical order, including repeats (from smallest to largest)
- What is the lowest and highest number? Write them here:  
**Minimum** = \_\_\_\_\_ **Maximum** = \_\_\_\_\_
- Find the middle number. This is your **median**. Write it here: **Med**= \_\_\_\_\_
- Look at the numbers before your median. What is the middle value between them? (for even numbers of data, find the middle number by adding the number either side and dividing by 2). This is your **Lower Quartile**. Write it here: **LQ** = \_\_\_\_\_
- Repeat the previous step for the numbers after your median. This is your **Upper Quartile**. Write it here: **UQ** = \_\_\_\_\_
- Now you are ready to draw your plot below. Plot dots for your 5-point statistics.
- Draw a box around your Lower quartile, Median and Upper Quartile.
- Draw lines from your minimum and maximum to the edge of the box.



## Bigger data sets (Stem and leaf graphs):

If you have a big data set, it can be tedious ordering the numbers from smallest to largest. In this case we use a stem and leaf graph to help us order the data and find the 5-point statistics.

These are results from a maths test taken: **13, 24, 22, 15, 33, 32, 12, 31, 26, 28, 14, 19, 20, 22, 31, 15**

1. Find the lowest and the greatest number in the data set. These are: 12 and 33
2. Then we draw a vertical line. On the left hand side of the line we write the numbers that corresponds to the tens, 12 has 1 in the tens place and 33 has 3 in the tens place.

```
1 |
2 |
3 |
```

3. On the right hand side of the line we will write the numbers that corresponds with the ones. Now we pair each unit's digit into the plot.

```
1 | 3 5 2 4 9 5
2 | 4 2 6 8 0 2
3 | 3 2 1 1
```

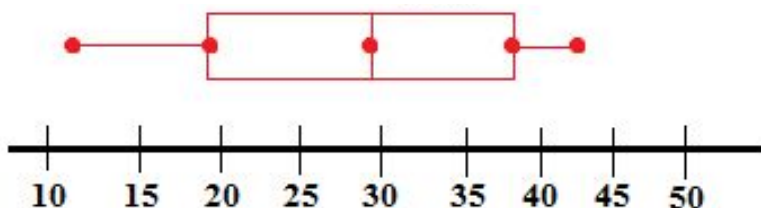
5. Then we arrange the digits in ordered, from the lowest to the greatest value to get our finished stem-and-leaf plot.

```
1 | 2 3 4 5 5 9
2 | 0 2 2 4 6 8
3 | 1 1 2 3
```

6. You can use a steam-and-leaf plot to find and display the median, the LQ and the UQ.  
The median is at  $(22 + 22)/2 = 22$  and is marked by a box. The LQ and UQ are marked by circles. The LQ is 15 while the UQ is 31.

```
1 | 2 3 4 5 5 9
2 | 0 2 2 4 6 8
3 | 1 1 2 3
```

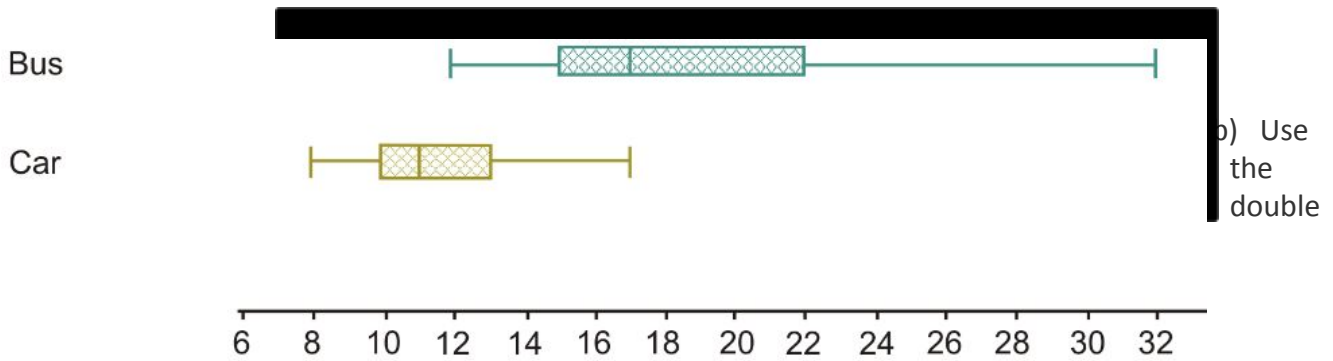
7. From this we can now draw our box and whisker plot



8. Emma and Daniel are surveying the times it takes students to arrive at school from home. There are 2 main groups of commuters who were in the survey. There were those who drove their own cars to school, and there were those who took the school bus. Emma and Daniel collected the following data:

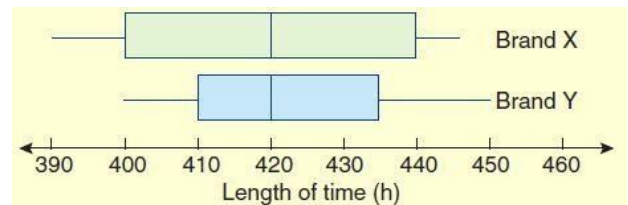
|                 |    |    |    |    |    |    |    |    |    |    |
|-----------------|----|----|----|----|----|----|----|----|----|----|
| Bus times (min) | 14 | 18 | 16 | 22 | 25 | 12 | 32 | 16 | 15 | 18 |
| Car times (min) | 12 | 10 | 13 | 14 | 9  | 17 | 11 | 10 | 8  | 11 |

- a) Draw a box-and-whisker plot for both sets of data on the same number line.

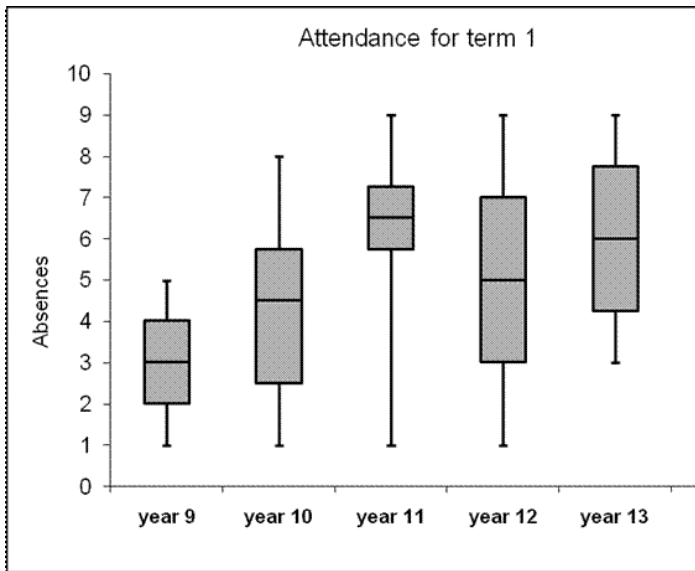


box-and-whisker plots to compare the times it takes for students to arrive at school either by car or by bus

9. A researcher tested two different brands of batteries to see how long they lasted. The results are shown in the double box-and-whisker plot alongside. Use the box-and-whisker plots to compare the performance of Brand X and Brand Y.

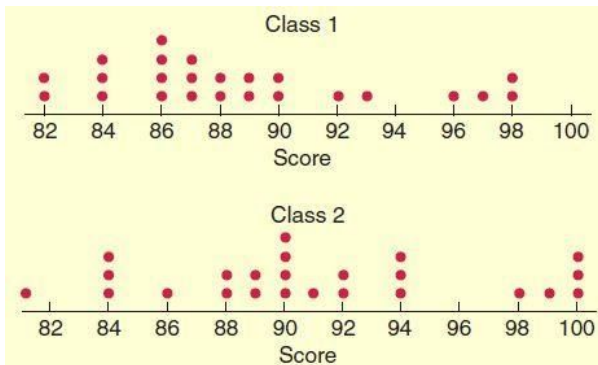


10. Below is a box and whisker plot of absentees of all tutor classes during term 1 in a certain school.



- What is the median number of absentees in year 9?
- The principal thinks year 13's are absent more often than year 9's. Would you say this is correct? Why/why not?
- Which year group tends to have more absentees? Justify your answer.

11. The marks for two classes on the same test are shown in the dot plot below.



- What is the mode score for each class?
- Which class would you say has the higher average score? Justify your answer.

## Shapes of Distributions

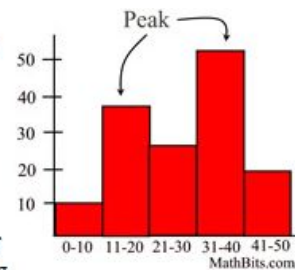
<http://mathbitsnotebook.com/Algebra1/StatisticsData/STShapes.html>

The **shape of a distribution** is described by its number of peaks and by its possession of symmetry, its tendency to skew, or its uniformity. (Distributions that are **skewed** have more points plotted on one side of the graph than on the other.)

**PEAKS:** Graphs often display peaks, or local maximums. It can be seen from the graph that the data count is visibly higher in certain sections of the graph.

1. one clear peak is called a *unimodal* distribution.
2. two clear peaks are called a *bimodal* distribution.

(Here, the term "mode" is used to describe a local maximum in a chart (such as the midpoint of the a peak interval in a histogram). It does not necessarily refer to the most frequently appearing score, as in the "central tendency mode".



3. single peak at the center is called *bell shaped* distribution.

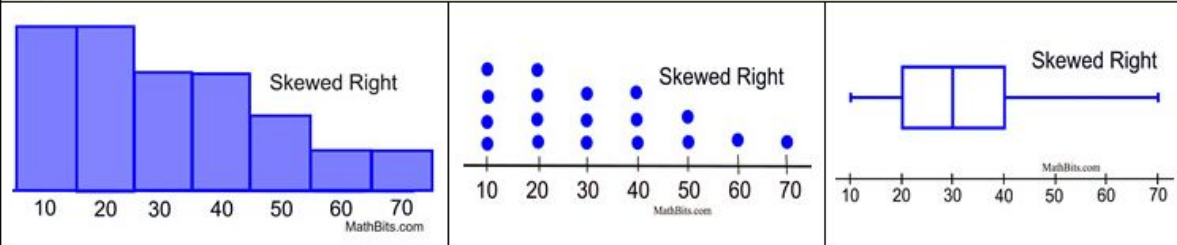
*Note:* A bell shaped graph (bell curve), is a frequency distribution that resembles the outline of a bell when plotted on a graph.



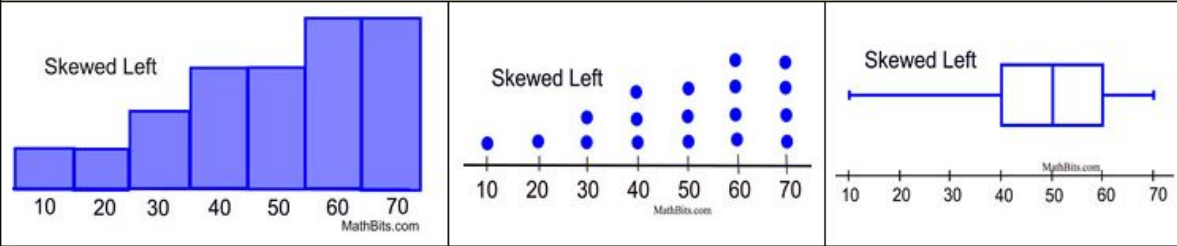
| Histograms  | Dot Plots                      | Box Plots        |
|---|--------------------------------|------------------|
| <p><i>Note:</i> The graphs shown below demonstrate the <i>shapes</i> of various sets of data. The histogram, dot plot and box plot in each separate section represent the same data set.</p>  |                                |                  |
| <p><b>Symmetric (bell shaped)</b> - when graphed, a vertical line drawn at the center will form mirror images, with the left half of the graph being the mirror image of the right half of the graph. In the histogram and dot plot, this shape is referred to as being a "bell shape" or a "mound". The <i>most typical</i> symmetric histogram or dot plot has the highest vertical column in the center. This shape is often referred to as being a "normal curve" (or <i>normal distribution</i>). Not all symmetric graphs, however, have this shape (see Symmetric U-shaped below).</p> |                                |                  |
| <p>Symmetric (bell shaped)</p>  | <p>Symmetric (bell shaped)</p> | <p>Symmetric</p> |
| <p><b>Symmetric (U-shaped)</b> - as mentioned above, a symmetric graph forms a mirror image of itself when reflected in its vertical center line. Unlike the previous graphs, these histograms and dot plots have more of a U shape.</p>  |                                |                  |
| <p>Symmetric U shaped</p>   | <p>Symmetric U - shaped</p>    | <p>Symmetric</p> |



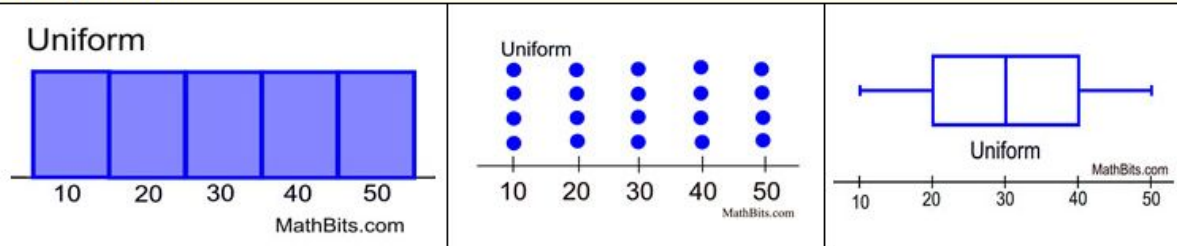
**Skewed Right (positively skewed)** - fewer data plots are found to the right of the graph (toward the larger numeric values). The "tail" of the graph is pulled toward higher positive numbers, or to the right. The mean typically gets pulled toward the tail, and is greater than the median. (There may be exceptions to the this last statement.)



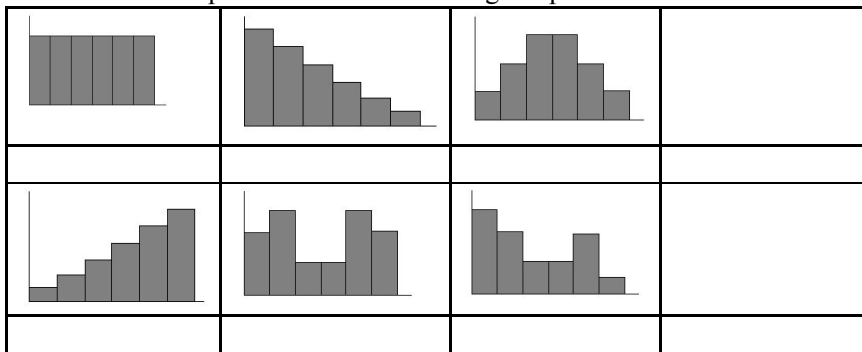
**Skewed Left (negatively skewed)** - fewer data plots are found to the left of the graph (toward the smaller numeric values). The "tail" of the graph is pulled toward the lower or negative numbers, or to the left. The mean typically gets pulled toward the tail, and is less than the median. (There may be exceptions to the this last statement.)

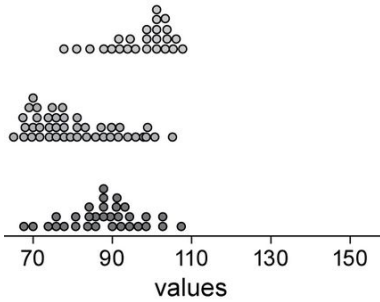


**Uniform** - The data is spread equally across the range. There are no clear peaks in these graphs, since each data entry appears the same number of times in the set. Notice in the boxplot how each section is of equal length: min to  $Q_1$ ,  $Q_1$  to median, median to  $Q_3$ , and  $Q_3$  to max. These graphs are also symmetric.



Place a suitable shape name for the following dot plot:





**Critical Thinking questions based on dot plot:**

Question 1:

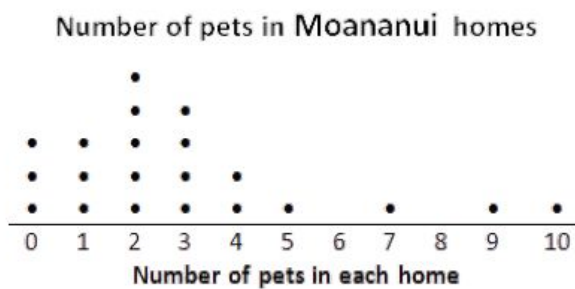
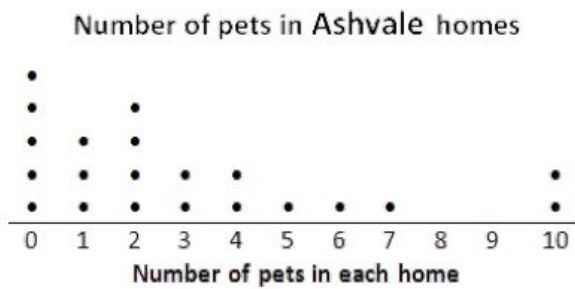
**People and their pets**

This resource is about comparing two dot plots.



I think homes in Ashdale usually have more pets than homes in Moananui.

Lena wants to find out if homes in Ashvale usually have more pets than homes in Moananui.



In which town do homes usually have more pets?

- a) Ashdale
- b) Moananui
- c) You cannot tell which town usually has more pets in each home
- d) Homes in Ashvale have about the same number of pets as homes in Moananui

Explain why you chose your answer. Hint: Look at the overall shape of each graph. How similar or different are they?

2. Make a frequency table that shows the number of sibling of each student in your maths class. Use the table to make a dot plot of the data, and describe the distribution.

|                    |           |                 |
|--------------------|-----------|-----------------|
|                    |           | Make a dot plot |
| Number of Siblings | Frequency |                 |
|                    |           |                 |
|                    |           |                 |
|                    |           |                 |
|                    |           |                 |

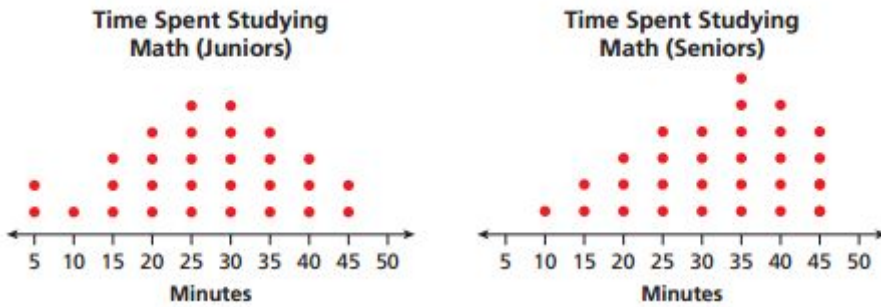
Describe the distribution.

Question 2:

Mrs Graham asked her junior and senior students how many minutes each of them spent studying math in one day, rounded to the nearest five minutes. The results are shown below.

| Time Spent Studying Math (min) | Frequency (Juniors) | Frequency (Seniors) |
|--------------------------------|---------------------|---------------------|
| 5                              | 2                   | 0                   |
| 10                             | 1                   | 1                   |
| 15                             | 3                   | 2                   |
| 20                             | 4                   | 3                   |
| 25                             | 5                   | 4                   |
| 30                             | 5                   | 4                   |
| 35                             | 4                   | 6                   |
| 40                             | 3                   | 5                   |
| 45                             | 2                   | 4                   |

She made a dot plot showing the data for juniors and a dot plot showing the data for seniors



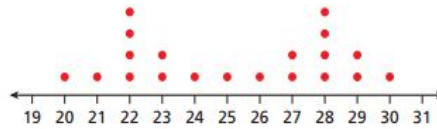
Describe the shape of each distribution

What does the shape of each distribution mean in terms of junior and senior students



Question 3:

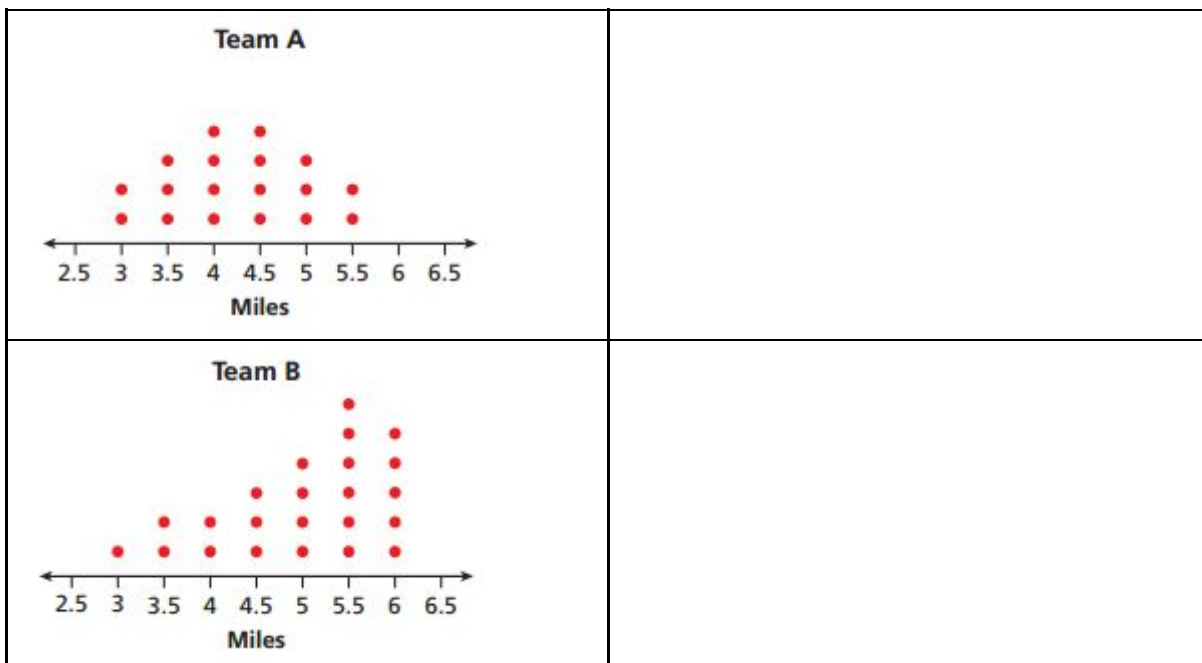
The data plot at right shows an example of a distribution. Why is this an appropriate name type of distribution?



bimodal  
for this

Question 4:

The dot plot shows the number of miles run by members of two track teams during one day. Using the dot plot below determine the type of distribution for each team. Explain what the distribution means for each



Data for team C members are shown below. Make a dot plot and determine the type of distribution. Explain what the distribution means.

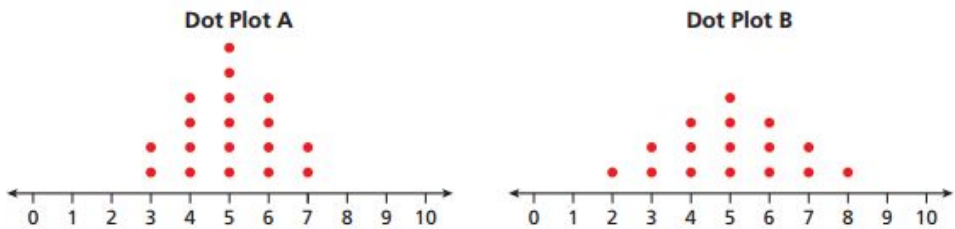
| Miles  | 3 | 3.5 | 4 | 4.5 | 5 | 5.5 | 6 |
|--------|---|-----|---|-----|---|-----|---|
| Team C | 3 | 2   | 2 | 2   | 3 | 2   | 2 |

|                              |                         |
|------------------------------|-------------------------|
| <p>Make a dot plot here:</p> | <p>Expected answer:</p> |
|------------------------------|-------------------------|

|  |  |
|--|--|
|  |  |
|--|--|

Question 5:

Magdalene and Peter conducted the same experiment. Both of their data sets had the same mean. Both made dot plots of their data that showed symmetric distributions, but Peter's dot plot shows a greater range than Magdalene's dot plot. Identify which plot below belongs to Peter and which belongs to Magdalene. Justify your findings.



Question 6:

Nutrition Julia researched grape juice brands to determine how many grams of sugar each brand contained per serving (8 fluid ounces = 1 serving).

| Grams of Sugar in Grape Juice (per serving) |    |    |    |    |    |
|---|----|----|----|----|----|
| 15  | 0  | 36 | 18 | 30 | 10 |
| 30  | 15 | 35 | 30 | 36 | 30 |
| 36  | 30 | 38 | 16 | 35 | 16 |

The data she collected is shown in the table.

- a) Identify any outlier(s) in the data set. (Expected answer =0)
- b) Make a dot plot for the data with the outlier(s) and a dot plot for the data without the outliers. What information you can get from each dot plot.

|                       |                          |
|-----------------------|--------------------------|
| Dot plot with outlier | Dot plot without outlier |
|-----------------------|--------------------------|

- c) Describe the distribution of data with or without outlier(s)
- d) How does excluding the outlier(s) affect the mean, median and mode of the data set?

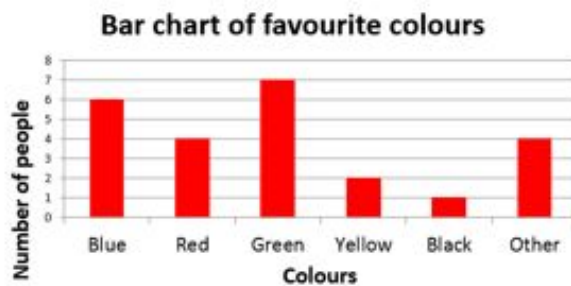


Extension:  
Gather data on the heights of people in your classroom. Separate the data for males from the data for females. Make

two dot plots representing the data collected for each group. Compare the dot plots and the distributions of the data.

Interpretation of bar graphs:

## What is this bar chart showing?

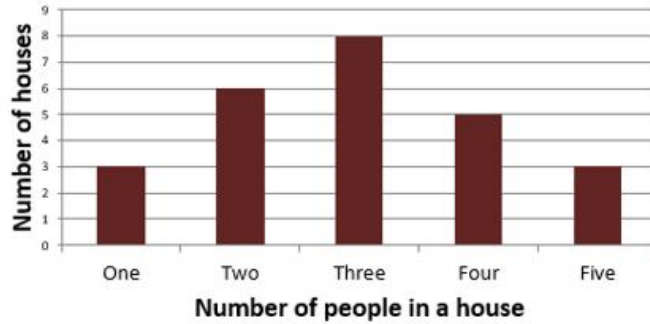


1. Which was the most popular colour?
2. How many people chose red as their favourite?
3. How many people were asked?



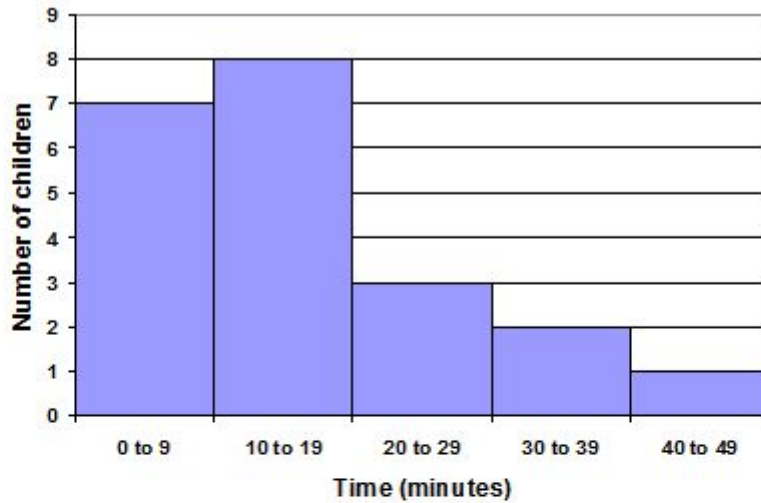
## One for you to try:

Number of people living in each house on a street



1. How many houses have two people living in them?
2. How many houses have more than 3 people living in them?
3. What is the modal number of people living in a house?
4. How many houses are there on the street?

Time to get to school:



**Nisha**

Most children took less than 10 minutes to get to school.



**Jason**

Most of the class took 10 to 19 minutes to get to school.



**Tim**

Most children took more than 20 minutes to get to school.



**Abby**

Most children took less than 30 minutes to get to school.

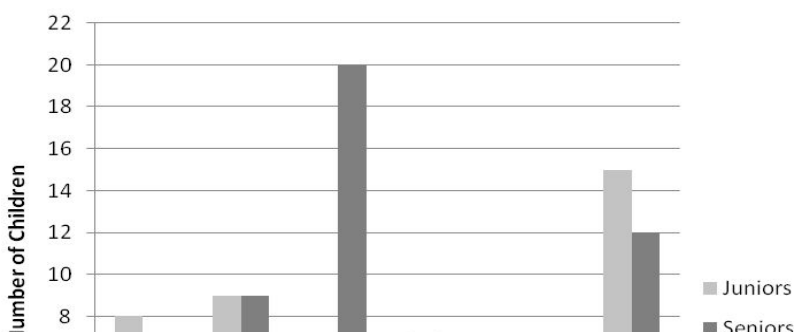
This graph shows the time it took the children in Room 8 to get to school one day. Which person made a correct statement about the graph?

- a) Nisha
- b) Jason
- c) Tim
- d) Abby
- e) They all made correct statements

Explain why you decided on your answer.

1. The teachers at Sunshine school wanted to know where the most children play at lunchtime. After one lunchtime they asked all the children where they had spent most of the lunchtime and made a bar graph.

**Lunchtime Places for Children**



Read the following statements and write down if you agree with the statement, disagree with the statement or can't tell from the results. Justify your answer by referring to the graph.

a) The library is equally popular with juniors and seniors.

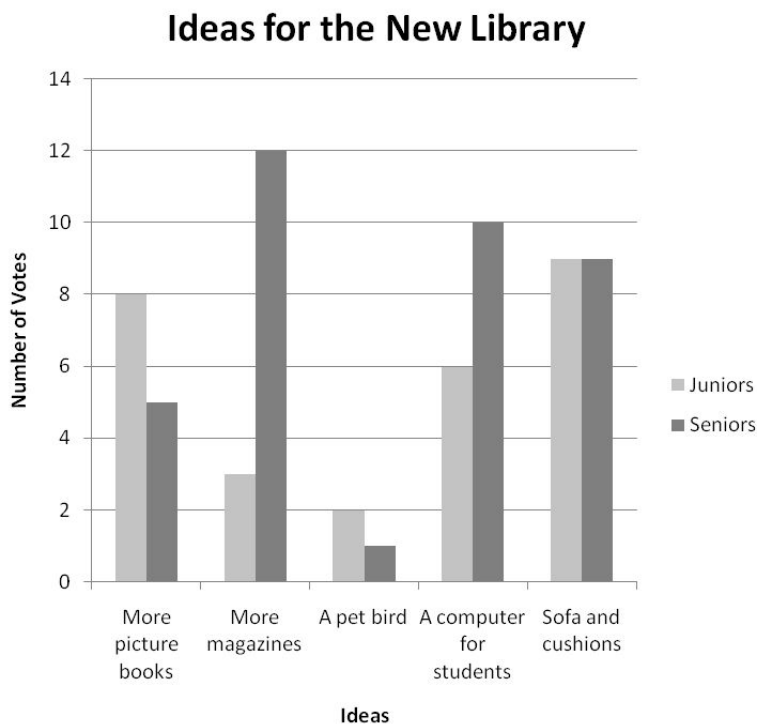
b) Everyone's favourite is the adventure playground.

c) The juniors play on the concrete because the seniors take over the sports field.

d) The tree house doesn't hold many people.

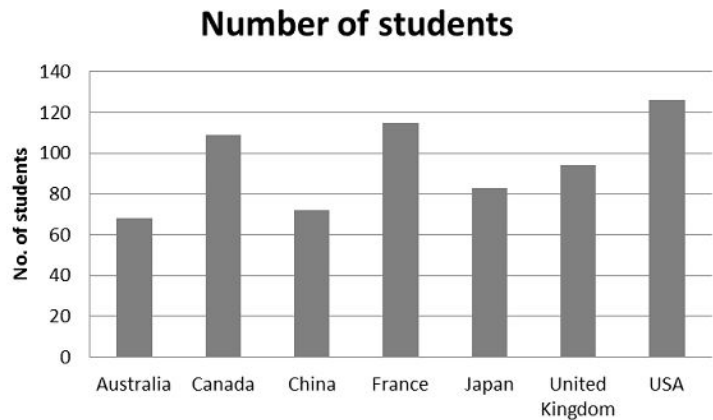
e) The sandpit is more popular with juniors.

2. Write at least 3 recommendations based on the survey results shown in the bar graph alongside. Share your recommendations with the person you are sitting next to and discuss whether you agree with each other's recommendations. Remember to back up your statements by referring to the graph.



3. The table below shows the number of students from various countries who attend an international school.

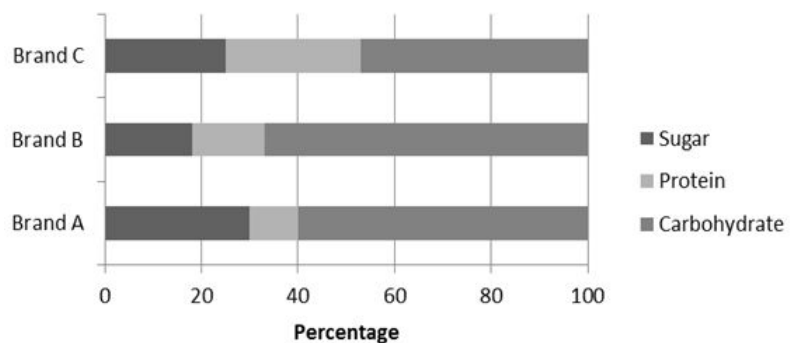
| Country        | Number of students |
|----------------|--------------------|
| Australia      | 68                 |
| Canada         | 109                |
| China          | 72                 |
| France         | 115                |
| Japan          | 83                 |
| United Kingdom | 94                 |
| USA            | 126                |



- Give a reason as to why a bar graph is the most appropriate display for this data.
- Which country has the fewest students attending the international school?
- How many students attend the international school?
- What is the difference in numbers attending from China and Japan?

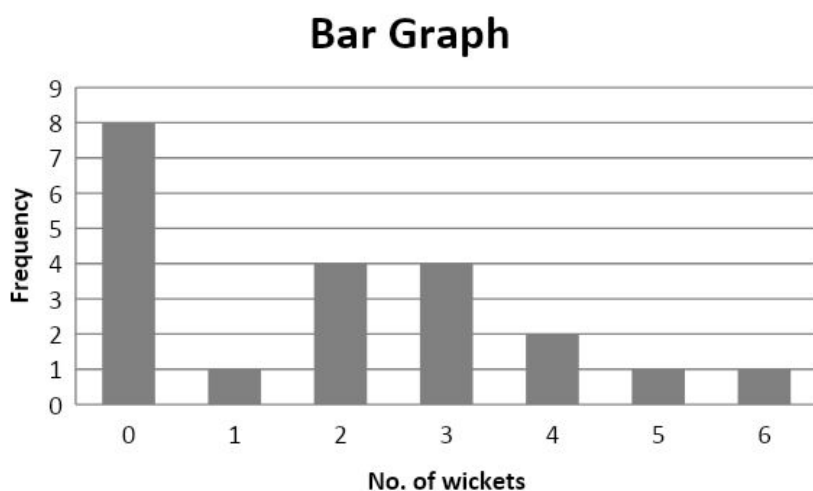
4. This graph compares 3 different brands of muesli bars with their sugar, protein and carbohydrate content.

**Composite Strip Graph comparing 3 brands of muesli bars**



- Which brand of muesli bar has the least sugar?
- Rank the muesli bars from the one with the lowest protein content to the one with the most protein content.
- Which muesli bar do you think is the most healthy to eat. Justify your answer by referring to the graph.






5. Danny Morrison played cricket for New Zealand as a fast bowler. The following display shows the number of wickets he took in each innings in test matches from November 1994 to March 1997.



How many times did Danny Morrison take

- four wickets in an innings?
- three wickets in an innings?
- no wickets in an innings?
- What was the highest number of wickets Danny Morrison took in any innings?
- How many wickets did Danny Morrison take most often?

6. Dipak Patel also played cricket for New Zealand. He was a spin bowler and the number of wickets he took in test matches over the same period is shown in the table below:

|   |   |   |
|---|---|---|
| <i>No.<br/>of<br/>wic<br/>ket<br/>s</i> | 0 |  |
|   | 1 |  |
|   | 2 |  |
|   | 3 |  |
|   | 4 |  |



| No. of wickets in an inning | Frequency |
|-----------------------------|-----------|
| 0                           | 6         |
| 1                           | 3         |
| 2                           | 8         |
| 3                           | 1         |
| 4                           | 2         |

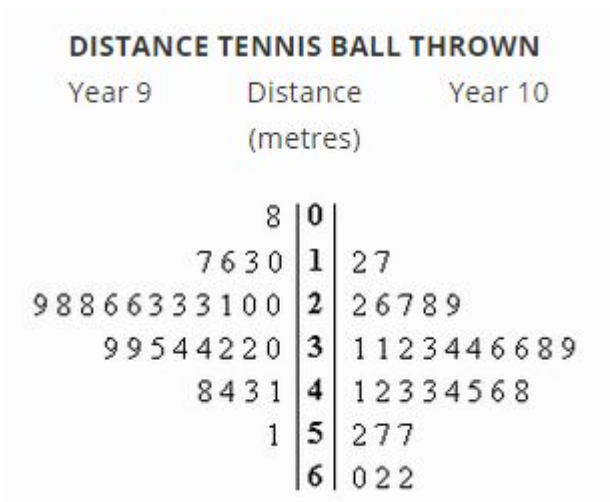
- a) Above (right) is Daniel's attempt at a pictograph for Dipak Patel's bowling, but it is not drawn correctly. Give at least 2 things that need to be corrected.
- b) Who is the better bowler? Justify your answer.

## Interpretation of stem and leaf graphs:

### Tennis ball throw:

At Defoe College, the Year 9 students challenged the Year 10 students to a ball throwing contest. Each student threw a tennis ball and this distance was measured and recorded to the nearest metre.

Their results are plotted on the back-to-back stem-and-leaf graph below.



- a) What was the distance of the:
- i) longest throw? \_\_\_\_\_ metres
  - ii) shortest throw? \_\_\_\_\_ metres
- b) What was the median distance thrown by:

- i) Year 9 students? \_\_\_\_\_ metres
- ii) Year 10 students? \_\_\_\_\_ metres

c) i) Tamiti said that Year 10 students threw the ball the furthest.  
Is he correct? YES / NO (circle one)

ii) Explain your answer.

2. Two groups underwent a simple fitness test and their heart rates were measured after one minute of exercise. The results are shown in the back-to-back stem-and-leaf plot.

| <i>Heart rates</i> |             |                |
|--------------------|-------------|----------------|
| <i>Group 1</i>     | <i>Stem</i> | <i>Group 2</i> |
| 7 5 5              | 11          |                |
| 9 9 9 9 8 8 7 7 6  | 12          | 5 5 6          |
| 6 6 4 4 0          | 13          | 4 6 8 8        |
| 4 2 0              | 14          | 2 3 6 6 7 8 8  |
|                    | 15          | 3 5 5 7        |
|                    | 16          | 2 4            |

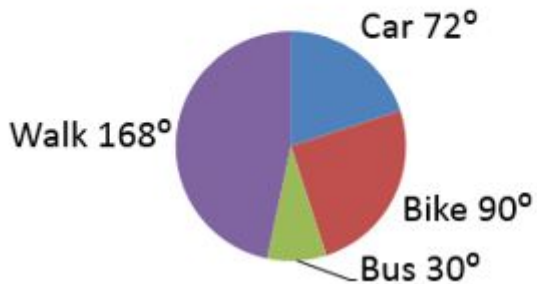
a) What does the shape of the stem-and-leaf plot suggest about the data?

a) Calculate the median and interquartile range for each group and use them to compare the results for each group.

## Interpretation of pie graphs:

1. Can you answer these questions?

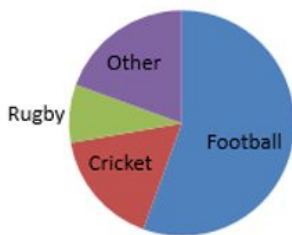
### Pie chart showing how pupils get to school



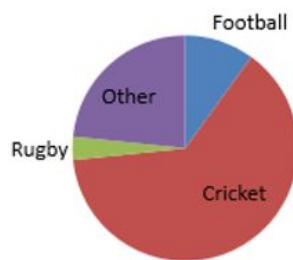
- What is the most popular way for pupils to get to school?
- If 15 people ride their bike, how many are driven by car?
- How many people were surveyed?

2. Can you compare these two pie graphs?

#### Favourite sports in the UK

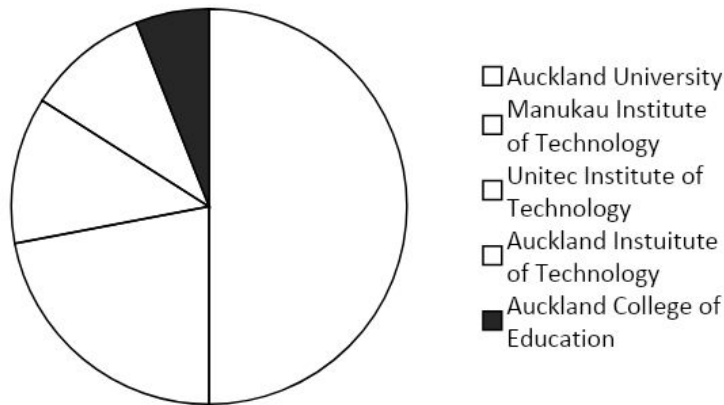


#### Favourite sports in India



- In which country was cricket is most popular sports?
- Which country had the most people who prefer football?

1. This pie graph was constructed from the amounts owed by students from 5 of Auckland's tertiary institutions in 1995.

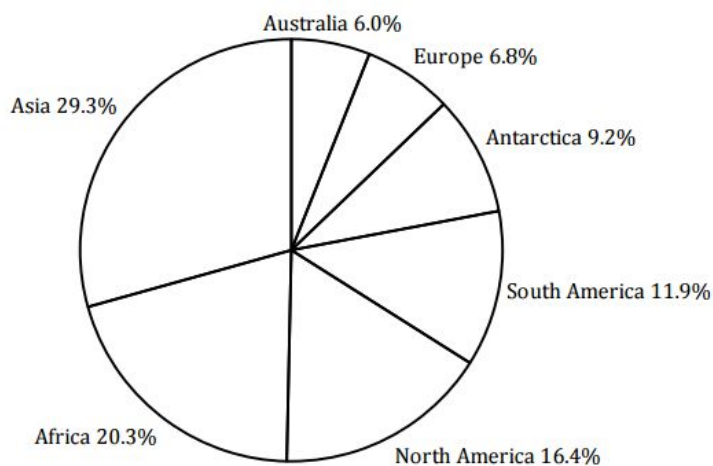


- b) Use the pie graph to complete the following sentences:  
 Students from \_\_\_\_\_ owe the most money, about \_\_\_\_\_% of the total amount owed. Students from \_\_\_\_\_ owe the second largest amount, about \_\_\_\_\_% of the total amount. Students from \_\_\_\_\_ owe the smallest amount.
- c) The total amount owed by the students at these five places was \$99.1 million. Students at Unitech owed \$12.3 million. Explain why the angle at the centre of the Unitec sector is  $45^\circ$ , to the nearest degree.

2)

### Land Area of Continents

As a percentage of the total land area of the Earth.



Source of data: <http://en.wikipedia.org/wiki/Continents>

- a) What are the largest and smallest continents?
- b) What percentage of the world's land area is made up of the Americas?

- c) Which is larger: Africa or Australia, Europe and Antarctica put together?
- d) If the land area of Africa is about 30 million square kilometres, what is the approximate land area of the Earth?
- e) Is the size of the continent related to the number of people who live on that continent? Explain your answer.

## Interpretation of line graphs and time series graphs:

### What are time series?

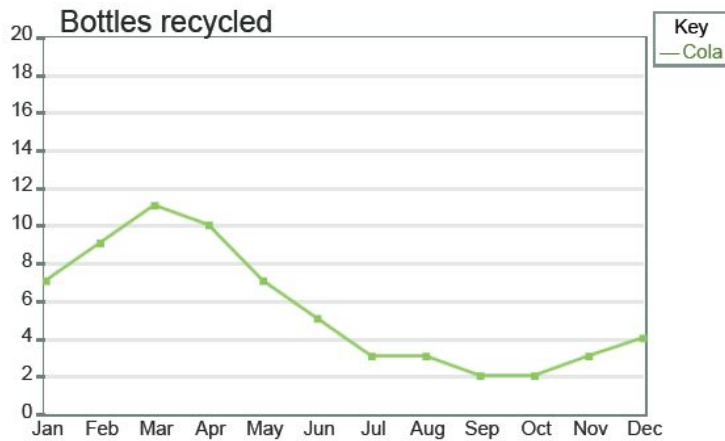
Time series show trend.

They plot results over periods of time – hence the name.

They are used to predict what could happen in the future.

Question one:

The graph below shows the number of Cola bottles recycled per household each month, over a one year period.



- a) In which month were the most cola bottles recycled?  
\_\_\_\_\_
- b) In which month were the least cola bottles recycled?  
\_\_\_\_\_
- c) How many cola bottles were recycled in August?  
\_\_\_\_\_
- d) Why do you think the number of cola bottles recycled starts decreasing after March?  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

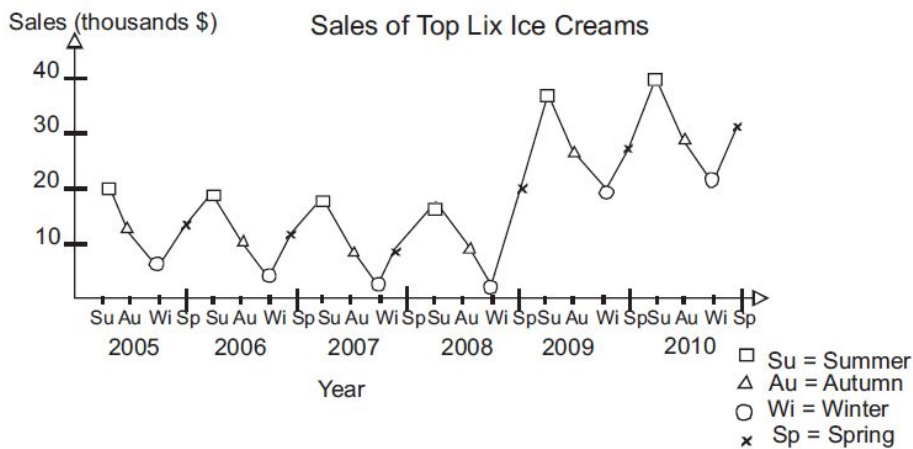
e) Why do you think the number of cola bottles recycled starts increasing after October?

f) \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_

g) Describe what this graphs shows you about cola bottles being recycled over a year and justify why this might be:

\_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_  
 \_\_\_\_\_

2. This graphs shows Top Lix Ice cream Truck’s sales (in thousands of dollars) for each season from 2005-2010.



a) In which year and month were the most Top Lix ice cream sales?

\_\_\_\_\_

b) In which year and month were the least Top Lix ice cream sales?

\_\_\_\_\_

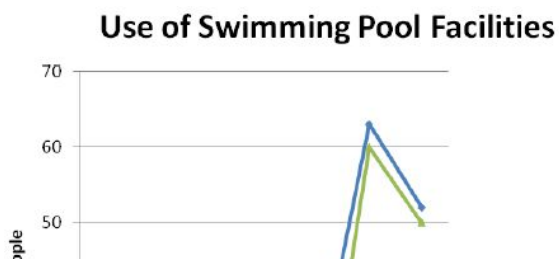
c) Are Top Lix ice cream sales increasing or decreasing or decreasing over time? Give reasons for your answer from the graph.

\_\_\_\_\_  
 \_\_\_\_\_

d) Describe the effect that the seasons have on the sale of Top Lix ice cream, justify your answer with evidence from the graph.

\_\_\_\_\_  
 \_\_\_\_\_

3. The graph below shows the average number of people who use each area of a swimming pool facility over the course of one week.



a) Which day of the week represents a peak in the graph for the recreational pool and many people used the recreational pool this day?

\_\_\_\_\_

b) On which day do the least number of people use the Hydroslide and how many people used the hydroslide this day?

\_\_\_\_\_

c) On which day do two of the areas have the highest number of people using them? Why do you think this might be?

\_\_\_\_\_  
\_\_\_\_\_

d) Can you describe the **trend** for the number of people using the Recreational Pool and Hydroslide over one week and explain why this may be:

\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

e) Can you describe the **trend** for the number of people using the Lane Swimming pool over one week and explain why this may be:

\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

4. The graph below shows the number of people who died on New Zealand roads from 1921 to 2013.

**Number of road deaths 1921 to 2013**



a) Which year had the most road deaths in NZ and approximately how many were there?

b) How many NZ road deaths were there (approximately) in 1951?

c) Are the number of deaths on NZ roads increasing or decreasing from 1921-1972? Can you think of a reason why this might be?

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d) Describe what happens to the number of deaths on NZ roads after 1987. What do you think the reason is behind this trend?

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e) What do you think the trend for the number of NZ road deaths will be in the long-term future? Give reasons for your answer.

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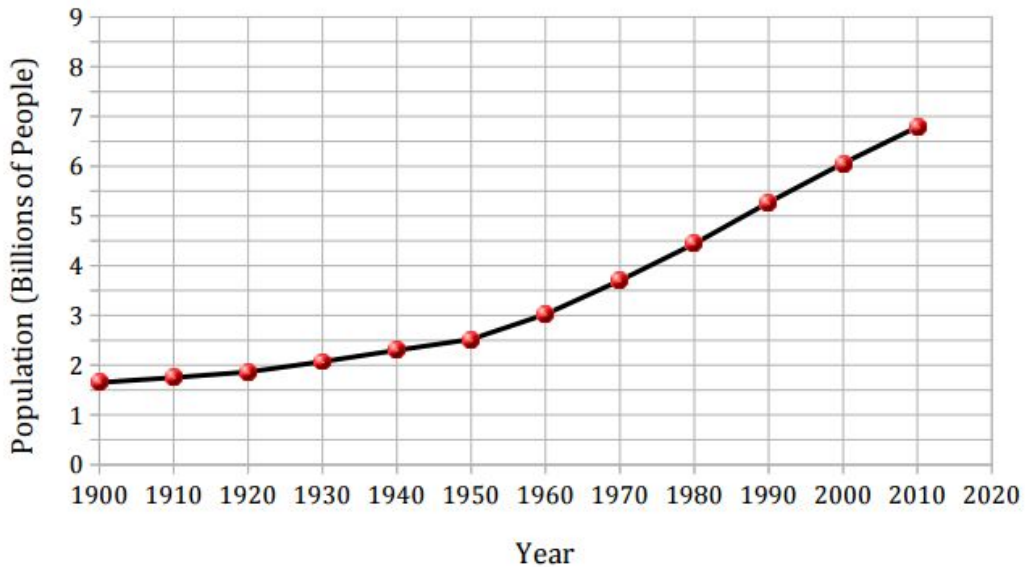
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5.



## Estimated World Population 1900 to 2000 by Decade

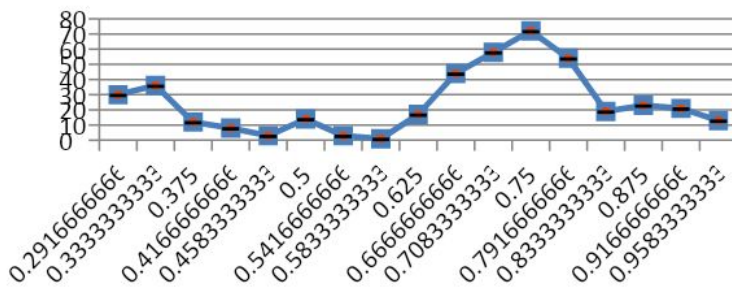


Source of data: <http://www.un.org/esa/population/publications/sixbillion/sixbilpart1.pdf>

- Estimate the population of the world in 1970 based on this graph.
- In what decade did the population increase the least?
- In what decade did the population increase the most?
- Estimate what the population will be in 2020 and extend the graph.
- In what years did the population reach 2, 3, 4, 5 and 6 billion people?

6. The graph below shows the number of year 9's that were recorded as logging onto facebook during a certain day

## Facebook logons



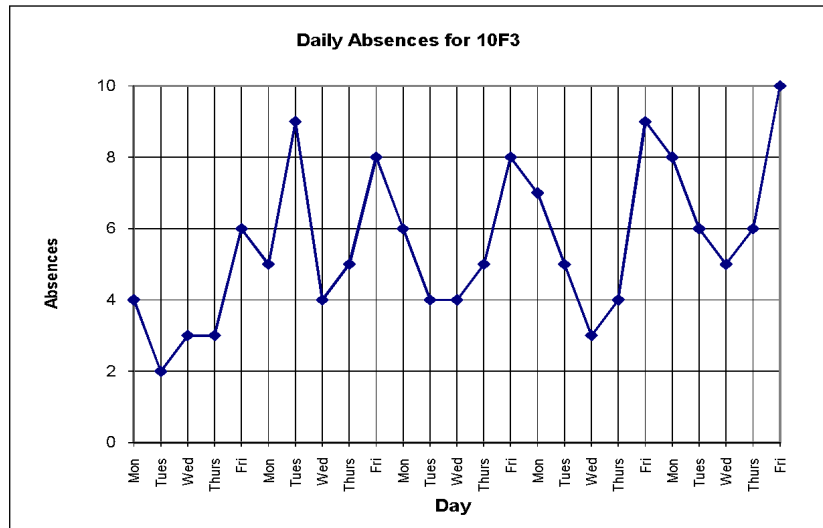
- At about what time was the highest number of logons?
- How many logons were there at 12:00?
- Would you expect this to be a weekday or a weekend day? Why?

- d) Describe what this graph shows you about facebook logons during this day and justify why this may be?

7. The number of absences for a tutor class each day over a period of five weeks at the start of the year is presented on the time series graph below.

Use the graph to answer the following:

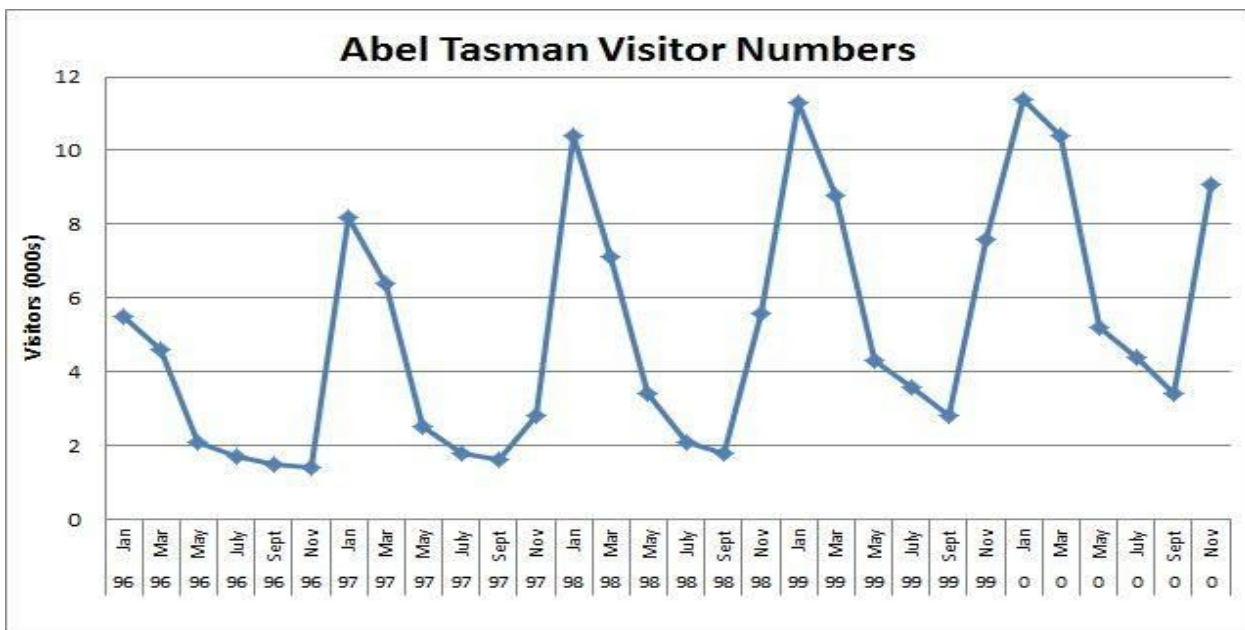
- a) What is the long term trend in the number of absences?



- b) Describe the seasonal pattern in the time series data.

- c) Use the graph to estimate how many absences there would be on Tuesday of week 6.

8. The graph below shows the number of visitors to Abel Tasman from 1996 to 2000.



- a) Which time period had the most visitors and how many were there?

- b) How many visitors were there approximately during May '96?
- c) Describe the short term and long term trends of this graph.

9.

## How do you draw them?

Below is a table showing the sales made by a small scarf company:

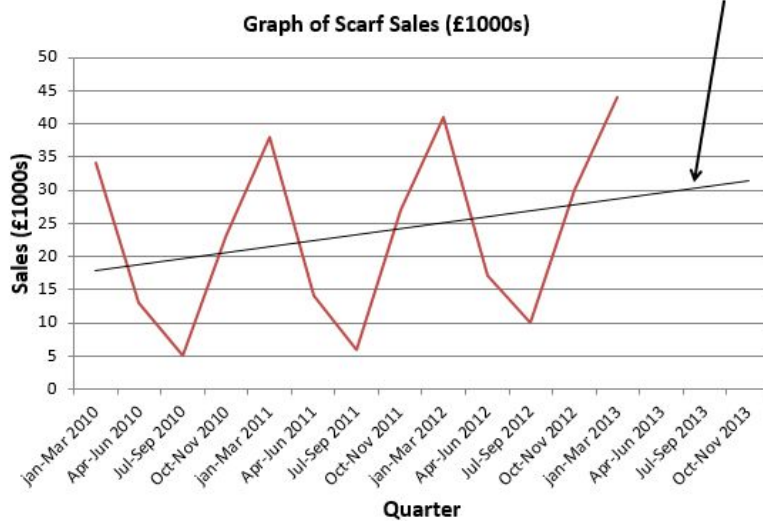
| Quarter        | Jan-Mar 2010 | Apr-Jun 2010 | Jul-Sep 2010 | Oct-Dec 2010 | Jan-Mar 2011 | Apr-Jun 2011 | Jul-Sep 2011 | Oct-Dec 2011 |
|----------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
| Sales (£1000s) | 34           | 13           | 5            | 23           | 38           | 14           | 6            | 27           |
| Quarter        | Jan-Mar 2012 | Apr-Jun 2012 | Jul-Sep 2012 | Oct-Dec 2012 | Jan-Mar 2013 | Apr-Jun 2013 | Jul-Sep 2013 | Oct-Dec 2013 |
| Sales (£1000s) | 41           | 17           | 10           | 30           | 44           | ?            | ?            | ?            |

Are sales on the increase?

It's difficult to tell, but a time series graph should show the sales' trend.

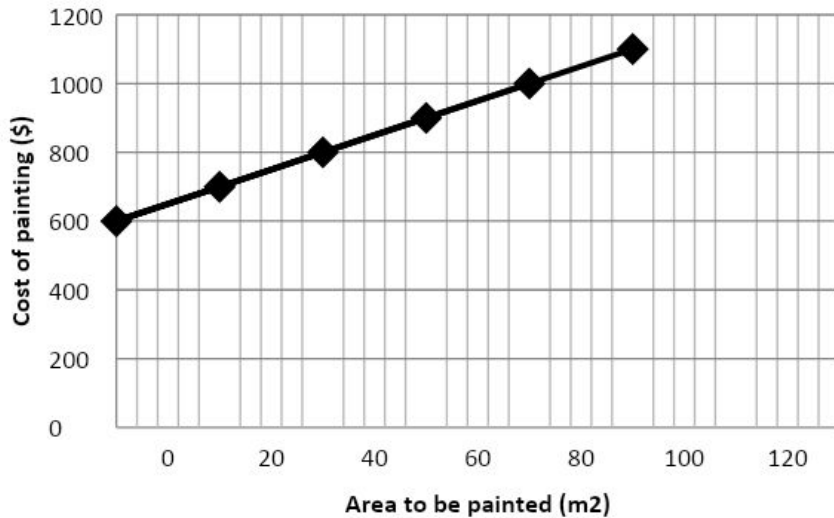
### Here's the graph:

The trend line shows that sales are increasing



Write a description about the sales made a small scarf company:

## Mixed graphs Interpretation:



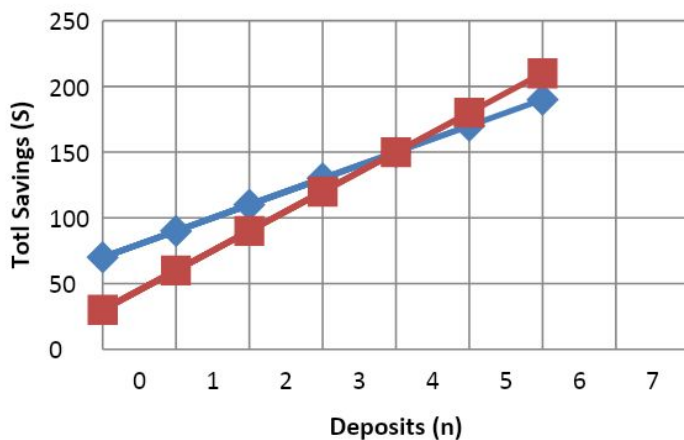
1. Kingdom Decorators charge a

fixed rate of \$600 and then \$50 for every 10m<sup>2</sup> for painting a house. The graph of the charges is shown:

- Use the graph to work out the cost of painting 70m<sup>2</sup>.
- The firm quotes \$1000 for a painting job. What area are they expecting to paint?

On the other hand, Quality Painters have a fixed charge of \$400 and then \$200 for every 20m<sup>2</sup> they paint.

- How much will they charge for an area of 60m<sup>2</sup>?
- Graph the line for Quality Painters.
- What is the area that can be painted where both companies charge the same amount? How is this shown on your graph?



2. Harry and Cath both have jobs delivering

newspapers to save money to use while on holiday at Christmas time. At the beginning of each



Employee number: \_\_\_\_\_

Dodgycereals Limited, your employer, believes students don't eat breakfast because the options parents buy are for old people. We have developed a new chocolate flavoured cereal block 'Chocolicious' for the young discerning intelligent gorgeous teenager.

Please ask your teenager the following questions:

- 1) Age \_\_\_\_\_
- 2) Gender: male/female
- 3) Do you eat breakfast Yes (go to Qu. 5)  
No (go to Qu. 4)
- 4) Why don't you eat breakfast? a) The cereal my parents buy is for old people  
b) It's too messy in a bowl, I'd rather eat a block of cereal  
c) I am too rushed in the morning to sit down and eat
- 5) Would you eat a chocolate flavoured block for breakfast? Yes/No

Thank you for completing this survey.

Dodgycereals Limited got their data from a single survey they conducted. All the 8 company employees who had teenagers took the survey home.

These tables show the results of the survey:

| Gender | Do you eat breakfast? |    |
|--------|-----------------------|----|
|        | Yes                   | No |
| Female | 6                     | 11 |
| Male   | 4                     | 9  |
| Total  | 10                    | 20 |

| Age   | Why don't you eat breakfast?                |  |  | Total |
|-------|---|--|--|-------|
|       | The cereal my parents buy is for old people | It's too messy in a bowl, I would rather eat a block of cereal | I am too rushed in the morning to sit down and eat |       |
| 9     | 1   | 1  | 1  | 3     |
| 10    | 2   | 1  | 1  | 4     |
| 11    | 2   | 1  | 0  | 3     |
| 12    | 4   | 1  | 1  | 6     |
| 13    | 3   | 0  | 0  | 3     |
| 15    | 1   | 0  | 0  | 1     |
| Total | 13  | 4  | 3  | 20    |

1. Which population did Dodgycereals claim to have investigated?

\_\_\_\_\_

2. Why do you think it is important to have more than one teenager in your sample?

\_\_\_\_\_

\_\_\_\_\_

3. Do you think 30 teenagers is a large enough sample to represent all the teenagers in New Zealand? Remember to give reasons.

\_\_\_\_\_

\_\_\_\_\_

Dodgycereals Limited got their data from a single survey they conducted. All the 8 company employees who had teenagers took the survey home.

4. Do you think this is a representative or biased sample of New Zealand teenagers?

Justify your answer. \_\_\_\_\_

Questions can also be biased if they try to influence the answers people give.

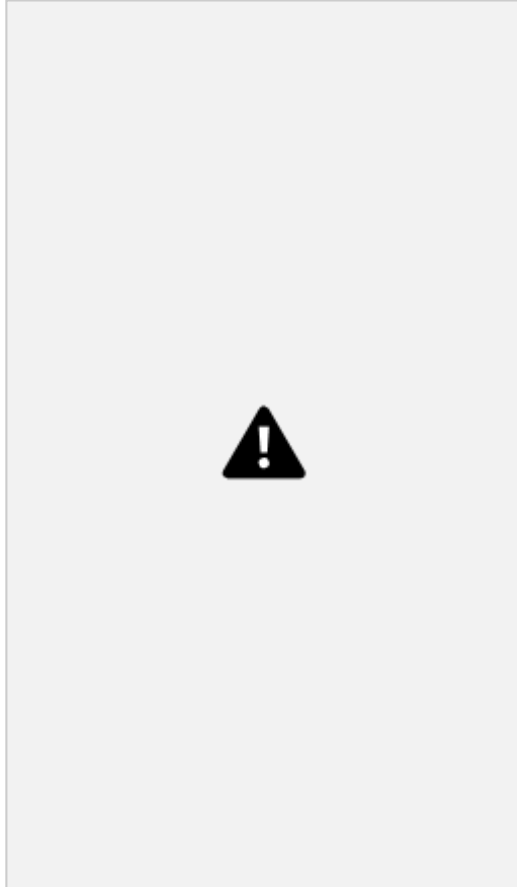
5. Do you think this survey is fair or biased? Justify your answer.

\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

### Analysis



Here are the graphs and the claims that Dodgycereals Limited made.



- Hardly any teenagers eat breakfast - especially intelligent males.
- Females are more discerning than males because more of them don't eat breakfast.
- Females are also more gorgeous than males

#### Do you eat breakfast? (Graph 1)

6. What do you think about this graph and these claims?

\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

7. What effect has the sample size, the way the teenagers were chosen to be in the sample and the survey questions had on the results?

\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_



Dodgycereals Limited used this graph to claim that:

- ☆ Almost all teenagers don't eat breakfast because the cereal their parents buy is for old people.
- ☆ Younger teenagers are more disorganised than older teenagers as they are too rushed to eat breakfast in the morning.
- ☆ All 13-15 year old teenagers didn't eat breakfast because the cereal their parents buy is for old people.

**Reasons why students don't eat breakfast (Graph 2)**

8. What is misleading about this graph? (hint: check the data table for the older teenagers) \_\_\_\_\_

\_\_\_\_\_

**Conclusion**

You are now ready to answer the question we asked at the beginning of the work sheet.



**Are the claims provided by Dodgycereal correct or are they misleading?**

Remember to give reasons based on what you found out about the sample and the analysis.

Remember to use some statistical language in your conclusion.

\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

**Reflection**

**1. Name two different ways Dodgycereal used graphs to mislead the reader.**

\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

**2. Give one reason why the sample of 30 students from 8 employees is not representative of all NZ teenagers.**

\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_



**Extension activity**

The Dodgycereal survey suggests that 2/3 of students don't eat breakfast. Explore this finding using a sample from census at school. Go to [www.censusatschool.org.nz/2007/questions/](http://www.censusatschool.org.nz/2007/questions/) to see the 2007 question on breakfast. Go to [www.censusatschool.org.nz/2007/table-maker/](http://www.censusatschool.org.nz/2007/table-maker/)  
Variable 1: breakfastnone  
Variable 2: gender

This will give you the total numbers that clicked the option "nothing" in the breakfast question and as well the number who selected "nothing" as an option for breakfast for each gender.

Go to [www.censusatschool.org.nz/2007/sampler](http://www.censusatschool.org.nz/2007/sampler) to select a sample of students to explore further the types of breakfasts students had.

**Reflection:**

**Based on your reflection which skills could you improve in the future:**