## Do Now

WALT expand algebraic expressions using the distributive law

Success Criteria I know everything inside the bracket gets multiplied by the term outside the bracket.

Lets check your understanding " This is a basic practice for people who missed out working on this in year $9^{\prime}$


Expanding expressions explained

2 The rectangle shown has height 4 and width $5+3$.
a What is the area of the yellow rectangle?
b What is the area of the blue rectangle?
c What is the total combined area?


## Example 12 Expanding brackets by simplifying repeated terms

Write the expression $3(2 m+5)$ in full without brackets and simplify the result.

## Solution

$$
\begin{aligned}
3(2 m+5) & =2 m+5+2 m+5+2 m+5 \\
& =6 m+15
\end{aligned}
$$

Explanation
Three repeats of the expression $2 m+5$.
Simplify by collecting the like terms.

3 The expression $3(a+2)$ can be written as $(a+2)+(a+2)+(a+2)$.
a Simplify this expression by collecting like terms.
b Write $2(x+y)$ out in full without brackets and simplify the result.
c Write $4(p+1)$ out in full without brackets and simplify the result.
d Write $3(4 a+2 b)$ out in full without brackets and simplify the result.
4 The area of the rectangle shown can be written as $4(x+3)$.
a What is the area of the green rectangle?
b What is the area of the red rectangle?
c Write the total area as an expression without using brackets.
d Fill in the blank: The expressions $4(x+3)$ and $4 x+12$ are $\qquad$ expressions.


## Example 14 Expanding using the distributive law

Expand the following expressions.
a $5(x+3)$
b $3(a-4)$
c $2(3 p-7 q)$

Solution
a $5(x+3)=5 x+5 \times 3$

$$
=5 x+15
$$

b $3(a-4)=3 a-3 \times 4$

$$
=3 a-12
$$

c $2(3 p-7 q)=2 \times 3 p-2 \times 7 q$

$$
=6 p-14 q
$$

## Explanation

Using the distributive law
$5(x+3)=5 x+5 \times 3$
Simplify the result.
Using the distributive law
$3(a-4)=3 a-3 \times 4$
Simplify the result.
Using the distributive law $2(3 p-7 q)=2 \times 3 p-2 \times 7 q$
Simplify the result, remembering $2 \times 3 p=6 p$ and $2 \times 7 q=14 q$.

6 Use the distributive law to expand the following.
a $6(y+8)$
b $7(l+4)$
c $9(a+7)$
d $2(t+6)$

7 Use the distributive law to expand the following.
a $2(m-10)$
b $8(y-3)$
c $3(e-7)$
d $7(e-3)$

8 Use the distributive law to expand the following.
a $10(6 g-7)$
b $5(3 e-8)$
c $5(7 w+10)$
d $5(2 u+5)$
e $7(8 x-2) \quad$ f $3(9 v-4)$
g $7(2 q-4)$
h $4(5 c-v)$
i $4(2+5 x) \quad$ j $3(7+2 y)$ k $8(9-3 x)$

9 Fill in the missing number in the following expansions.
a $4(x+5)=4 x+\square$
b $3(x+2)=3 x+$ $\qquad$

## Challenge

10 The perimeter of a rectangle is given by the expression $2(l+w)$ where $l$ is the length and $w$ is the width. What is an equivalent expression for this?

11 Expand the brackets in the following and then simplify the result.
a $3(x+2)+4 x$
b $4(a+3)-2 a$
You can combine like terms.
c $5(3 b-2)+10$
d $6(2 c+4)-2 c$
12 Write an expression for each of the following and then expand it.
a A number $x$ has 3 added to it and the result is multiplied by 5 .
b A number $b$ has 6 added to it and the result is doubled.
c A number $z$ has 4 subtracted from it and the result is multiplied by 3 .
d A number $y$ is subtracted from 10 and the result is multiplied by 7 .
13 When expanded, $4(2 a+6 b)$ gives $8 a+24 b$. Find two other expressions that expand to $8 a+24 b$.

## Bigger expansions

14 The diagram below helps to demonstrate that $(a+2)(b+3)=a b+2 b+3 a+6$.


Use a diagram like the one above to expand the following expressions.
a $(a+4)(b+2)$
b $(x+3)(y+5)$
c $(2 a+5)(3 c+2)$
d $(4 a+1)(5 b+3)$

## More practice

## Exercise 110

1 Complete the following to expand the expressions.
a $5(d+4)=$ $\qquad$ $\times d+$ $\qquad$ $\times 4$
b $4(y-3)=$
$\qquad$ $+$
$\qquad$ $\times y=$ $\qquad$ $\times 3$
$=$ $\qquad$ -
c $3(6-m)=$ $\qquad$ $\times 6-$ $\qquad$ $\times m$
$=$ $\qquad$ $-$
d $2(q+7)=2 \times \ldots+2 \times$
$=$ $\qquad$ $+$
e $6(b-2)=6 \times \ldots-6 \times$
$=$ $\qquad$
$\qquad$


2 Expand the following expressions.
a $4(b+3)$
b $12(k+8)$
c $7(c-5)$
d $6(d-3)$
e $2(y-11)$
f $9(a+10)$
g $10(j+9)$
h $8(m+2)$
i $7(q-2) \quad$ j $5(l-6)$
k $4(2-c)$
l $3(r+6)$
m $9(7-t)$
n $4(v+12)$
o 6(8-n)
p $6(x-2)$

3 Complete the following to expand.
a $4(3 z+2)=$ $\qquad$ $\times 3 z+$ $\qquad$ $\times 2$
$=\ldots+$ $\qquad$
c $3(6+4 k)=3 \times \ldots+3 \times$ $\qquad$
$=$ $\qquad$ $+$ $\qquad$

4 Expand the following expressions.
a $3(2 m+6)$
b $5(4 d+5)$
c $9(3 p+8)$
d $7(5 c-4)$
e $10(2 p-2)$
f $12(4 c-3)$
g $6(6 k+10)$
h $2(13 n+5)$
i $10(7 a-6)$
j $8(7 l-3)$
k $11(2 h+8)$
l $4(15 k-5)$
m $13(6 x+2)$
n $7(10 w-9)$
o $5(11 j+7)$
p $3(9 q-4)$

5 Explain the difference between each pair of expressions.
a $2 x+1$ and $2(x+1)$
b $5 p-8$ and $5(p-8)$

6 Complete the following to expand.
a $m(m+3)=$ $\qquad$ $\times m+$ $\qquad$ $\times 3$
b $p(q-r)=$ $\qquad$ $\times q-$ $\qquad$ $\times r$
$\qquad$ $+$
$=$ $\qquad$ -

7 Expand the following expressions.
a $x(x+5)$
b $q(q+13)$
c $a(a+8)$
d $z(z+11)$
e $t(t-6)$
f $m(m-10)$
g $d(3-d)$
h $r(r-17)$
i $a(c-4)$
j $b(d+a)$
k $x(y-z)$
$1 m(n+c)$
$\mathrm{m} j(k-h)$
n $d(f+g)$
$0 \quad e(c-d)$
p $r(x-y)$

8 Complete the following to expand.
a $4 t(t-3)=$ $\qquad$ $\times t-$ $\qquad$ $\times 3$
$\qquad$
$\qquad$
b $3 x(2 y+5 z)=$ $\qquad$ $\times 2 y+$ $\qquad$ $\times 5 z$ $=\ldots+$

9 Expand the following expressions.
a $8 m(m+3)$
b $5 c(c+6)$
c $3 r(11+r)$
d $11 q(q-1)$
e $4 x(2-x)$
f $10 a(7-a)$
g $4 a(2 a+7)$
h $9 b(11 b+5)$
i $5 f(4-4 f)$
j $6 d(d-f)$
k $3 k(8-4 k)$
$l 12 l(3-2 l)$
m $5 p(2 p-3 n)$
n $7 c(5 c+2 d)$
o $6 n(6 m-5 n)$
p $4 x(4 x-3 z)$

10 Complete the following to simplify.
a $3(x+5)+2 x-7$
$=\ldots \times x+\ldots \times 5+2 x-7$
$=\ldots x+\ldots+2 x-7$
$=$
$\qquad$ $+$

11 Expand and simplify by collecting like terms.
a $7(a+8)+5 a$
b $9(p-5)-3$
c $6(c+8)+4 c$
d $8(d-7)-4 d$
e $5(q+4)+10 q$
f $11(m-7)+15$
g $4(n+6)+3 n-10$
h $2(b-7)+3 b+12$
i $3 x-19+3(5-2 x)$
j $7 w-8+5(w+1)$
k $9(f-3)+8-6 f \quad$ l $6 n-10+2(n-7)$
m $10 y+22+2(y-10)+3 y$
n $7 c+3(6-4 c)+11-2 c$
o $4(y-6)-3+5 y$

12 Expand and simplify by collecting like terms.
a $2(x+7)+4(x+8)$
b $4(d+5)+3(d-2)$
c $8(n-3)+7(n-4)$
d $3(q-6)+9(q-7)$
e $7(f-8)+2(f-9)$
f $10(c-6)+2(c-2)$
g $x(x+5)+2(x-4)$
h $y(y-6)+4(y+2)$
i $w(w-8)+w(w-9)$
j $5(2 m+7)+3(4 m-8)$
k $4(3 t+6)+3(2 t+4)$
l $9(2 a-1)+10(4 a+7)$
m $10(4 a-2)+2 a(3 a-5)$
n $6 c(c-7)+2 c(c+8)$
o $4 d(3-2 d)+3 d(2 d+1)$

13 Complete the following to expand.
a $-4(y+3)$
$=(-\quad) \times y+($ $\qquad$ ) $\times 3$
$=-4 y+(-12)$
$=$ $\qquad$ -
b $-x(x-y)$
$=\left(\_\right) \times x-($ $\qquad$ ) $\times y$
$\qquad$
$=$
$\qquad$ $+$ $\qquad$
c $-(4 k+3 m)$
$=\left(\_\right) \times 4 k+\left(\_\right) \times 3 m$
$=$ $\qquad$ $+(-\quad)$
$=$ $\qquad$
$\qquad$

## Extension

14 Expand the following.
a $-6(a+10)$
b $-4(b+8)$
c $-9(k+9)$
d $-3(c-3)$
e $-5(f-7)$
f $-10(d-6)$
g $-7(m+5)$
h $-2(n+10)$
i $-11(h+11)$
j $-10(2 p-7)$
k $-8(3 m-3)$
$1-5(7 q-8)$

15 Expand the following.
$\begin{array}{ll}\mathrm{a} & -p(p+7) \\ \mathrm{e} & -x(x-6) \\ \mathrm{i} & -k(m+10)\end{array}$
b $-w(w+8)$
c $-d(d+11)$
d $-s(s-3)$
f $-f(f-14)$
g $-m(n+5)$
h $-a(y+2)$
j $-3 t(2 t-p)$
k $-4 y(5 y-c)$
$1-8 n(8 n-4 m)$

16 Expand the following.
$\begin{array}{ll}\mathrm{a} & -(x+2) \\ \mathrm{e} & -(g-5) \\ \mathrm{i} & -(l+13)\end{array}$
b $-(y+3)$
c $-(a+7)$
d $-(n-11)$
g $-(6+g)$
h $-(3+k)$
k $-(5 n-8)$
$1-(10 d-11)$

17 Expand and collect like terms.
a $5(p+7)+3 p$
b $12(c-8)+29$
c $4 x+7(x-5)+10$
d $6(d-1)+2 d$
e $3(q-4)+2 q+9$
f $15+2(m-7)-5 m$
g $10(n+8)-(6 n-3)$
h $9 a+14+2(a-9)$
i $16 s-17-5(s-4)+6$
j $9(x-8)-(x+12)$
k $11(w+2)-(w-2)$
l $3(z+12)-(z+18)$
$\mathrm{m} 2(d-7)+5(d-8)$
n $4(k+2)-2(k+3)$
0 $8(p-6)-3(p-10)$
p $y(y+8)-y(y-9)$
q $n(n-3)-2(n-6)$
r $w(w+4)-5(w-7)$
s $5 c(2 c-6)-3 c(c-7)$
t $8 a(2 a-1)-2 a(3 a+4)$
u $10 d(d+2)-7 d(2 d-4)$
v $4 f-7(f+6)-3(f-10)$
w $5 c(c+7)-8(c-9)$
x $12+3(n-1)-2(n-6)$

18 Expand and simplify each expression by collecting like terms.
a $4(x+7)-3(x-5)+2(x-9)$
b $2(c+13)-5(c+4)+9(c-6)$
c $8(n-6)+12-5 n-4(n-14)$
d $12 f+30+4(f-12)+11-9 f$
e $-5(d-11)-8(d+7)-2(d-5)$
f $-(p-7)-3(p+5)+17-10 p$
g $-7 y(y-4)-6 y(2 y+8)+12 y$
h $2 a(a-3)+5 a(a+6)-3 a(9-2 a)$
i $\quad-9 k+15+3 k(4-2 k)-6 k(7+2 k)$
j $4 b(2 c+8 b)-2 c(5 b-7 c)+2 b(9 c-3 b)$

## Check your answers

| 1 a 36 b 20 | c 35 |
| :---: | :---: |
| 2 a 20 b 12 | c 32 |
| 3 a $3 a+6$ b $2 x+2 y$ | c $4 p+4$ d $12 a+6 b$ |
| 4 a $4 x \quad$ b 12 | c $4 x+12$ d equivalent |
| 5 a $4(x+2)=4 x+8$ | b $3(a+1)=3 a+3$ |
| c $4(k+7)=4 k+28$ | d $3(b+5)=3 b+15$ |
| 6 a $6 y+48$ b $7 l+28$ | c $9 a+63$ d $2 t+12$ |
| 7 a $2 m-20$ b $8 y-24$ | c $3 e-21$ d $7 e-21$ |
| 8 a $60 g-70$ b $15 e-40$ | c $35 w+50$ d $10 u+25$ |
| e $56 x-14$ f $27 v-12$ | g $14 q-28$ h $20 c-4 v$ |
| i $8+20 x$ j $21+6 y$ | k $72-24 x$ I $22-44 k$ |
| 9 a 20 b 6 | c 10 d 14 |
| $102 l+2 w$ |  |
| 11 a $7 x+6$ b $2 a+12$ | c $15 b$ d $10 c+24$ |
| 12 a $5(x+3)=5 x+15$ | b $2(b+6)=2 b+12$ |
| c $3(z-4)=3 z-12$ | d $7(10-y)=70-7 y$ |
| $132(4 a+12 b)$ and 8(a+3b). Others possible. |  |
| 14 a $a b+4 b+2 a+8$ | b $x y+3 y+5 x+15$ |
| c $6 a c+15 c+4 a+10$ | d $20 a b+5 b+12 a+3$ |


|  |  |
| :---: | :---: |
|  | 17 a $8 p+35$ b $12 c-67$ <br> c $11 x-25$ d $8 d-6$ <br> e $5 q-3$ f $-3 m+1$ <br> g $4 n+83$ h $11 a-4$ <br> i $11 s+9$ j $8 x-84$ <br> k $10 w+24$ $12 z+18$ <br> m $7 d-54$ n $2 k+2$ <br> o $5 p-18$ p $17 y$ <br> q $n^{2}-5 n+12$ r $w^{2}-w+35$ <br> s $7 c^{2}-9 c$ t $10 a^{2}-16 a$ <br> u $-4 d^{2}+48 d$ v $-6 f-12$ <br> w $5 c^{2}+27 c+72$ x $-n+21$ <br> 18 a $3 x+25$ b $6 c-48$ <br> c $n+20$ d $7 f-7$ <br> e $-15 d+9$ f $-14 p+9$ <br> g $-19 y^{2}-8 y$ h $13 a^{2}-3 a$ <br> i $-18 k^{2}-39 k+15$ j $26 b^{2}+14 c^{2}+16 b c$ |

After completing your basic practice Discuss in Week 5

We can show what things are multiplied together

- using arrows

$$
(a+b)(c+d) \quad \text { or }
$$

- using the word FOIL where

F stands for Firsts
0 stands for Outers
I stands for Inners
L stands for Lasts.


## Brample 9

Expand and simplify: a $(x+2)(x+3) \quad$ b $(x+7)(x+11)$

$$
\begin{aligned}
& (x+2)(x+3) & & (x+7)(x+11) \\
= & x \times x+x \times 3+2 \times x+2 \times 3 & = & x \times x+x \times 11+7 \times x+7 \times 11 \\
= & x^{2}+3 x+2 x+6 & = & x^{2}+11 x+7 x+77 \\
= & x^{2}+5 x+6 & = & x^{2}+18 x+77
\end{aligned}
$$

## EXERCISE 11B

1 Expand and simplify:
a $(x+2)(x+4)$
b $(x+3)(x+4)$
c $(x+2)(x+1)$
d $(x+1)(x+1)$
e $(x+4)(x+5)$
f $(x+4)(x+4)$
g $(x+3)(x+5)$
h $(x+1)(x+6)$
| $(x+7)(x+2)$

## Frample 10

Expand and simplify: a $(x+2)(x-5) \quad$ b $(x-3)(x-4)$

$$
\text { a } \begin{aligned}
& (x+2)(x-5) \\
= & (x+2)(x+-5) \\
= & x \times x+x \times-5+2 \times x+2 \times{ }^{-} 5 \\
= & x^{2}-5 x+2 x-10 \\
= & x^{2}-3 x-10 \\
& \\
& (x-3)(x-4) \\
= & (x+-3)(x+-4) \\
= & x \times x+x \times-4+{ }^{-} 3 \times x+{ }^{-} 3 \times-4 \\
= & x^{2}-4 x-3 x+12 \\
= & x^{2}-7 x+12
\end{aligned}
$$

2 Expand and simplify:
a $(x+1)(x-2)$
b $\quad(x+2)(x-10)$
c $(x-1)(x+3)$
d $(x-2)(x+5)$
e $(x-1)(x-3)$
f $(x-4)(x-4)$
g $\quad(x+3)(x-5)$
h $(x-3)(x+5)$
I $(x-3)(x-5)$

3 Expand and simplify:
a $\quad(a+3)(a+6)$
b $\quad(a+3)(a-6)$
c $(a-3)(a+6)$
d $(a-3)(a-6)$
e $(b+4)(b+7)$
f $(b-4)(b+7)$
g $\quad(b+4)(b-7)$
h $(b-4)(b-7)$
I $(2 c+1)(c+3)$

4 Expand and simplify:
a $\quad(2 x+1)(3 x+2)$
b $(5 x-1)(2 x+1)$
c $(x-4)(2 x+1)$
d $(1-x)(x+1)$
e $(1-2 x)(3+2 x)$
f $(3 x-2)(3 x-2)$

## Brample 11

Expand and simplify: a $(x+4)^{2} \quad$ b $(x-4)^{2}$

$$
\begin{array}{rlr} 
& (x+4)^{2} & \\
= & (x+4)(x+4) & \\
= & \left.x^{2}+4 x+4 x+16 \quad \text { \{using FOIL }\right\} \\
= & x^{2}+8 x+16 & \\
& & \\
& (x-4)^{2} & \\
= & (x-4)(x-4) & \\
= & \left.x^{2}-4 x-4 x+16 \quad \text { \{using FOIL }\right\} \\
= & x^{2}-8 x+16 &
\end{array}
$$

5 Expand and simplify:
a $(x+1)^{2}$
b $(x+3)^{2}$
c $(x-2)^{2}$
d $(x-5)^{2}$
e $(2+x)^{2}$
f $(2-x)^{2}$
g $(2 x+1)^{2}$
h $(2 x-1)^{2}$
I $(3 x+2)^{2}$
J $(3 x-2)^{2}$
k $(x+y)^{2}$
| $(x-y)^{2}$

## 7xample 12

Expand and simplify: $(x-3)(x+3)$

$$
\begin{aligned}
& (x-3)(x+3) \\
= & \left.x^{2}+3 x-3 x-9 \quad \text { \{using FOIL }\right\} \\
= & x^{2}-9
\end{aligned}
$$

6 Expand and simplify:
a $\quad(x-1)(x+1)$
b $\quad(x+4)(x-4)$
c $\quad(x+5)(x-5)$
d $(2 x+1)(2 x-1)$
e $(4-x)(4+x)$
f $(3-2 x)(3+2 x)$

7 Why did the $x$-terms disappear in the expansions of question 6?

## Answers

1 a $x^{2}+6 x+8$ b $x^{2}+7 x+12$
c $x^{2}+3 x+2$ d $x^{2}+2 x+1$
e $x^{2}+9 x+20$ f $x^{2}+8 x+16$
g $x^{2}+8 x+15 \quad$ h $\quad x^{2}+7 x+6$
i $x^{2}+9 x+14$
2 a $x^{2}-x-2$ b $x^{2}-8 x-20 \quad$ c $\quad x^{2}+2 x-3$
d $x^{2}+3 x-10$ e $x^{2}-4 x+3$ f $x^{2}-8 x+16$
g $x^{2}-2 x-15$ h $x^{2}+2 x-15$ i $x^{2}-8 x+15$
3 a $\quad a^{2}+9 a+18$ b $\quad a^{2}-3 a-18$
c $a^{2}+3 a-18$ d $a^{2}-9 a+18$
e $b^{2}+11 b+28$ f $b^{2}+3 b-28$
g $b^{2}-3 b-28$ h $b^{2}-11 b+28$
i $2 c^{2}+7 c+3$
4 a $6 x^{2}+7 x+2$ b $10 x^{2}+3 x-1$
c $2 x^{2}-7 x-4 \quad$ d ${ }^{-} x^{2}+1 \quad \mathbf{e}^{-} 4 x^{2}-4 x+3$
f $9 x^{2}-12 x+4$
5 a $x^{2}+2 x+1$ b $x^{2}+6 x+9$ c $x^{2}-4 x+4$
d $x^{2}-10 x+25$ e $4+4 x+x^{2}$ f $4-4 x+x^{2}$
g $4 x^{2}+4 x+1$ h $4 x^{2}-4 x+1$ i $9 x^{2}+12 x+4$
j $9 x^{2}-12 x+4 \quad \mathbf{k} \quad x^{2}+2 x y+y^{2}$
l $x^{2}-2 x y+y^{2}$
6 a $x^{2}-1$ b $x^{2}-16$ c $x^{2}-25$
d $4 x^{2}-1$ e $16-x^{2}$ f $9-4 x^{2}$
7 When expanded, the positive $x$ term was matched by a negative $x$ term.

