Walt complete number patterns and find the rule for each pattern Success Criteria I can understand the sequence of the pattern given and make up a rule

1 For each of the following number patterns:
i Describe in words how the pattern is formed.
ii Write down the next three numbers in the pattern.
a $2,4,6,8$,
b $4,7,10,13$,
c $27,23,19,15$,
d $30,28,26,24$, $\qquad$ e $90,80,70,60$, $\qquad$ f $3,6,12,24$, $\qquad$
g $2,6,18,54$,_-
h $3,30,300,3000$, $\qquad$ i $1,0.1,0.01,0.001$, $\qquad$
j $128,64,32,16$,
2 Find the missing numbers in the following patterns.
a 3,5 , $\qquad$ 9 ,
b $2,5, \ldots, 11$, $\qquad$ c $4, \ldots, 10, \ldots, 16$
d 30,26 , $\qquad$ 18,
e 51 , $\qquad$ $47, \ldots, 43$
h 625,125 , $\qquad$ 5,
f 2,10 , __, 250, $\qquad$
g $2, \ldots, 8, \ldots, 32$
j 3 , 300 $\qquad$ 30000

Walt Build patterns and create a rule
Success Criteria I know I can create a pattern and a rule associated with the pattern.
All patterns have a sequence that can predict future patterns.

## EXAMPLE 1

Form a sequence of numbers by using each rule given.
Some number patterns need
a Start with 5 and add 3. more than one operation.
b Start with 1000 and divide by 2 .
c Start with 2 , multiply by 3 and then add 1 .

| 1st term | 2nd term | 3rd term | 4th term |
| :---: | :---: | :---: | :---: |
| 5 | $5+3=8$ | $8+3=11$ | $11+3=14$ |

So the sequence is $5,8,11,14, \ldots$
b

| 1st term | 2nd term | 3rd term | 4th term |
| :---: | :---: | :---: | :---: |
| 1000 | $1000 \div 2=500$ | $500 \div 2=250$ | $250 \div 2=125$ |

So the sequence is $1000,500,250,125, \ldots$

c|c|c|c| | 1 st term | 2 nd term | 3rd term |
| :---: | :---: | :---: |
| 2 | $2 \times 3+1=7$ | $7 \times 3+1=22$ |

So the sequence is $2,7,22,67, \ldots$

1 Using the rule given, find the first four terms of each number sequence.
a Start with 2 and add 3.
b Start with 5 and add 2 .
c Start with 1 and add 4 .
d Start with 100 and subtract 10 .
e Start with 45 and subtract 3 .
f Start with 50 and subtract 2 .
g Start with 3 and double the preceding term.
h Start with 7 and multiply by 10 .
i Start with 1 and multiply by 3 .
j Start with 64 and divide by 2 .
k Start with 2 and divide by 10 .
1 Start with 1 , multiply by 4 and then add 1 .
m Start with 3 , multiply by 2 and then add 1 .
n Start with 5, multiply by 2 and then subtract 4 .
0 Start with 2, multiply by 4 and then subtract 5 .
p Start with 7 , multiply by 2 and then subtract 9 .
2 If 1 L of paint covers approximately $16 \mathrm{~m}^{2}$, what area could be covered by:
a 1 L ?
b 2 L ?
c 3 L ?
d 4 L ?
e 5 L ?

3 The height of a candle decreases by 1.5 cm every hour. If the candle is originally 10 cm high, what will be its height after:
a 1 h ?
b 2 h ?
c 3 h ?
d 4 h ?
e 5 h ?
ly $16 \mathrm{~m}^{2}$, what


4 The cost of hiring a taxi is $\$ 5$ plus $\$ 3.50$ for each kilometre travelled. How much does it cost to travel:
a 1 km ?
b 2 km ?
c 3 km ?
d 4 km ?
e 5 km ?

5 The time taken to roast a piece of meat is 20 min plus an extra 15 min for each $\frac{1}{2} \mathrm{~kg}$ of meat. How long will it take to roast a piece of meat that weighs:
a $\frac{1}{2} \mathrm{~kg}$ ?
b 1 kg ?
c $1 \frac{1}{2} \mathrm{~kg}$ ?
d 2 kg ?
e $2 \frac{1}{2} \mathrm{~kg}$ ?

## Check your answers

1 a i Starting with 2 , each number is 2 more than the number before it.
ii $10,12,14$
b i Starting with 4 , each number is 3 more than the number before it.
ii $16,19,22$
c i Starting with 27 , each number is 4 less than the number before it.
ii $11,7,3$
d i Starting with 30 , each number is 2 less than the number before it.
ii $22,20,18$
e i Starting with 90 , each number is 10 less than the number before it.
ii $50,40,30$
f i Starting with 3 , each number is 2 times the number before it.
ii $48,96,192$
g i Starting with 2 , each number is 3 times the number before it.
ii $162,486,1458$
h i Starting with 3, each number is 10 times the number before it.
ii $30000,300000,3000000$
i i Starting with 1 , each number is $\frac{1}{10}$ of (or 0.1 times) the number before it.
ii $0.0001,0.00001,0.000001$
j i Starting with 128 , each number is $\frac{1}{2}$ of the number before it.
ii $8,4,2$

2 a 7,11
d 22, 14
b 8, 14
c 7,13
g 4, 16
e 49,45
f 50,1250
j 30,3000

## Exercise 14し

1 a $2,5,8,11, \ldots$
b $5,7,9,11, \ldots$
c $1,5,9,13, \ldots$
e $45,42,39,36, \ldots$
d $100,90,80,70, \ldots$
g $3,6,12,24, \ldots$
f $50,48,46,44, \ldots$
i $1,3,9,27, \ldots$
h $7,70,700,7000, \ldots$
k 2, 0.2, 0.02, $0.002, \ldots$
j $64,32,16,8, \ldots$
m 3, 7, 15, 31, $\ldots$
l $1,5,21,85, \ldots$

- $2,3,7,23, \ldots$
n $5,6,8,12, \ldots$
p $7,5,1,-7, \ldots$
2 a $16 \mathrm{~m}^{2}$
b $32 \mathrm{~m}^{2}$
c $48 \mathrm{~m}^{2}$
d $64 \mathrm{~m}^{2}$
e $80 \mathrm{~m}^{2}$
3 a 8.5 cm
b 7 cm
c 5.5 cm
d 4 cm
e 2.5 cm

| 4 a $\$ 8.50$ | b $\$ 12$ | c $\$ 15.50$ |
| :--- | :--- | :--- |
| d $\$ 19$ | e $\$ 22.50$ |  |
| 5 a 35 min | b 50 min | c 65 min |
| d 80 min | e 95 min |  |

