

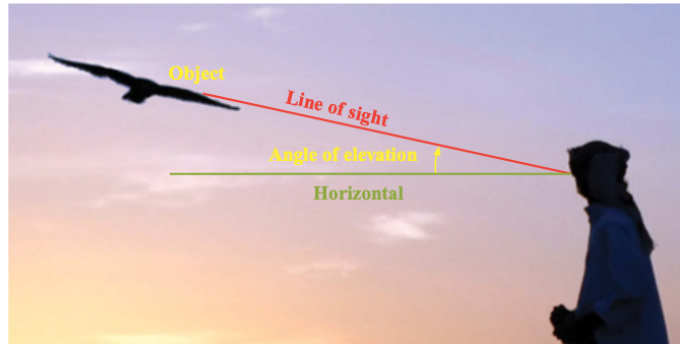
# Worded problems using trigonometry

WALT apply the angle of elevation and the angle of depression to solve trig problems  
 Success Criteria I know my trig ratios, I can draw a diagram and determine the sides and the ratio.

[Watch the video](#)

[How to make and use a clinometer](#)

The **angle of elevation** of an object from an observer is the angle between the horizontal and the line of sight *up* to the object.

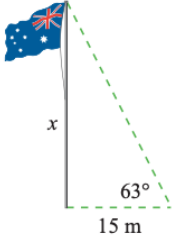


The **angle of depression** of an object from an observer is the angle between the horizontal and the line of sight *down* to the object.



## EXAMPLE 1

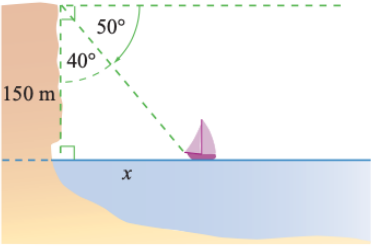
The angle of elevation of the top of a flagpole, as observed from a point 15 m from its base, is  $63^\circ$ . Draw a diagram and find the height of the flagpole.

Solve	Think	Apply
$\tan 63^\circ = \frac{x}{15}$ $x = 15 \tan 63^\circ$ $\approx 29.4$ <p>The flagpole is about 29 m high.</p>		<p>Elevation means looking upwards. The angle is at ground level.</p>

## EXAMPLE 2

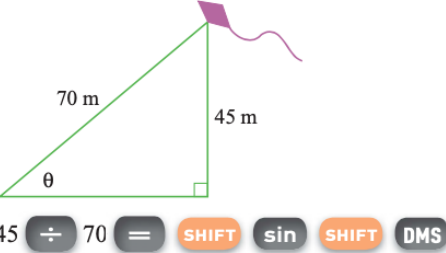
The angle of depression from the top of a vertical cliff, 150 m above sea level, to a boat below is  $50^\circ$ . Draw a diagram and find the distance of the boat from the base of the cliff.

We assume that the angle between the ground (or sea) and a building (or cliff) is always  $90^\circ$ .

Solve	Think	Apply
$\tan 40^\circ = \frac{x}{150}$ $x = 150 \tan 40^\circ$ $\approx 125.86$ <p>The boat is about 126 m out from the base of the cliff.</p>		<p>Depression means looking downwards. Either subtract from <math>90^\circ</math> to find the angle in the triangle or use parallel line properties to label the angle at the bottom as equal.</p>

## EXAMPLE 3

A kite is flying at a height of 45 m above the ground at the end of a string of length 70 m. Find, to the nearest minute, the angle of elevation from the ground to the string.

Solve	Think	Apply
$\sin \theta = \frac{45}{70}$ $\therefore \theta = 40.005\dots^\circ$ $= 40^\circ 0' 19''$ <p>The angle of elevation is <math>40^\circ 0'</math>.</p>		<p>Determine the sides required and select the correct ratio.</p>

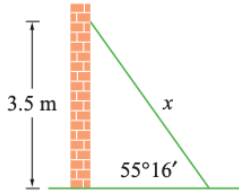
Draw a diagram for each of the following and find the unknown. For questions 1 to 5 give your answer to the nearest metre where necessary.

- The angle of elevation of the top of a flagpole from the ground, as observed from a point 50 m from its base, is  $38^\circ$ . Find the height of the flagpole.
- The angle of depression from the top of a cliff, 100 m above sea level, to a boat is  $65^\circ$ . Find the distance of the boat from the base of the cliff.
- From a point 35 m from the base of a vertical cliff, the angle of elevation to the top of the cliff is  $72^\circ$ . Find the height of the cliff.
- When looking down from the top of a building to a person standing in a park 150 m from the base of the building, the angle of depression is  $28^\circ$ . Find the height of the building.
- The top of a tree, when viewed 40 m from the base of the tree, has an angle of elevation of  $37^\circ$ . Find the height of the tree.
- A person is standing 200 m from a vertical cliff 265 m high. Find the angle of elevation to the top of the cliff to the nearest minute.

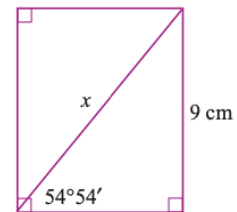


## EXAMPLE 4

A ladder leaning against a vertical wall reaches 3.5 m up the wall and makes an angle of  $55^{\circ}16'$  with the ground. Determine the length of the ladder.

Solve	Think	Apply
$\sin 55^{\circ}16' = \frac{3.5}{x}$ $\therefore x \sin 55^{\circ}16' = 3.5$ $x = \frac{3.5}{\sin 55^{\circ}16'}$ $= 4.25\dots$ $\approx 4.3$ <p>The ladder is 4.3 m long.</p>	<p>Use the opposite side and hypotenuse.</p>  <p>3.5 <math>\div</math> <math>\sin</math> 55 <math>\text{DMS}</math> 16 <math>\text{DMS}</math> <math>=</math></p>	<p>Identify the sides required and select the correct ratio.</p>

- 7 A rectangle has a longer side of 9 cm. The angle between the diagonal and the shorter side is  $54^{\circ}54'$ . Find the length of the diagonal.



- 8 A seesaw is 6.3 m long. When one end is resting on the ground it makes an angle of  $23^{\circ}35'$  with the ground. Find the height of the other end above ground level.



- 9 A rally driver travels 210 km on a bearing of  $145^{\circ}\text{T}$ . How far east of the starting position would the rally driver be now?



- 10 An isosceles triangle has height 13 cm and base 20 cm. Find the value of the base angles to the nearest minute.
- 11 A right-angled triangle has non-hypotenuse sides of length 12 cm and 17 cm. Find the value of the other angles in degrees and minutes.
- 12 An isosceles triangle has a base of length 12 cm and a vertical angle of  $70^{\circ}$ . Find the lengths of the equal sides.



# Extension

## Example 5

A ship sails 35 km from a port  $A$  on a bearing of  $318^\circ\text{T}$  to a buoy  $B$ . Find how far the ship is north and west of  $A$ .

Solve	Think	Apply
$\cos 42^\circ = \frac{\text{adjacent}}{\text{hypotenuse}}$ $= \frac{x}{35}$ $\therefore x = 35 \cos 42^\circ$ $\approx 26.01 \text{ (2 decimal places)}$ <p>The ship is 26 km north of <math>A</math>.</p> $\sin 42^\circ = \frac{\text{opposite}}{\text{hypotenuse}}$ $= \frac{y}{35}$ $\therefore y = 35 \sin 42^\circ$ $\approx 23.42 \text{ (2 decimal places)}$ <p>The ship is 23 km west of <math>A</math>.</p>	<p><math>\angle NAB = 360^\circ - 318^\circ = 42^\circ</math> Let <math>x</math> be the distance north and <math>y</math> be the distance west.</p>	<p>Always draw a diagram with north in the vertical direction of the page. Locate all the other bearings or distances.</p>

## EXAMPLE 6

Town  $A$  is 43 km east and 88 km south of town  $B$ . Find the bearing of  $A$  from  $B$ .

Solve	Think	Apply
$\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$ $= \frac{88}{43}$ $\therefore \theta \approx 64^\circ$ <p>The bearing of <math>A</math> from <math>B</math> is <math>90 + 64 = 154^\circ\text{T}</math>.</p>		<p>Draw a diagram showing all the information, then isolate the right-angled triangle.</p>

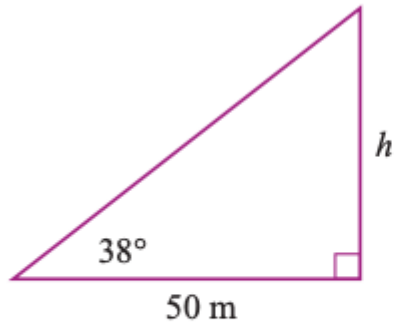
- 13 A ship sails 58 km from a port  $A$  on a bearing of  $262^\circ\text{T}$  to a buoy  $B$ . Find how far the ship is west and south of  $A$ .
- 14 A ship sails 83 km from a port  $O$  on a bearing of  $131^\circ$  to another boat  $X$ . Find how far the ship is east and south of  $O$ .
- 15 A ship sails from a port  $P$ . It travels 55 km west then 30 km south to an atoll  $A$ . Find the bearing of  $A$  from  $P$ .
- 16 Town  $X$  is 185 km west and 260 km north of town  $Y$ .
  - a Find the bearing of  $Y$  from  $X$ .
  - b Find the bearing of  $X$  from  $Y$ .
- 17 A plane flies 800 km north and 1250 km west. Find the bearing and distance of the plane from its starting point.
- 18  $A$  is 40 km due north of  $B$  and  $C$  is 100 km due east of  $B$ . Find the distance and bearing of  $C$  from  $A$ .
- 19 A kayaker paddles due west for 1.5 km, then turns due south and covers a further 800 m. How far and in what direction to the nearest degree must she travel to return to her starting point?



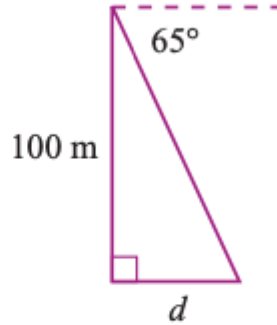
Remember Pythagoras. ! .....

# Check your answers

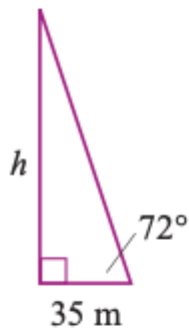
1  $h = 39$  m



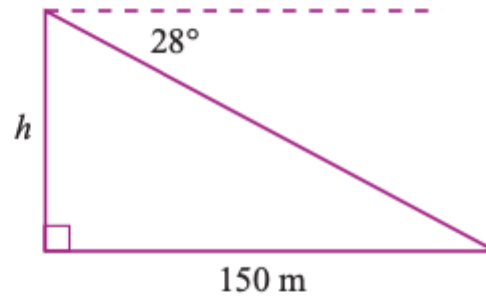
2  $d = 47$  m



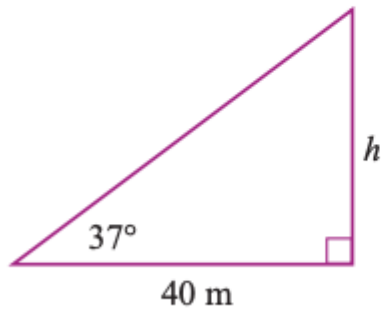
3  $h = 108$  m



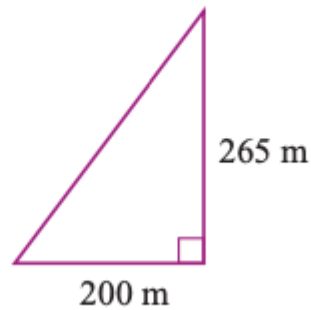
4  $h = 80$  m



5  $h = 30$  m



6  $52^\circ 27'$



7 11 cm

9 120 km

11  $35^\circ 13'$  and  $54^\circ 47'$

13 57 km W, 8 km S

15  $241^\circ$ T

16 a  $145^\circ$ T

17  $302^\circ 37'$ T, 1484 km

19 1.7 km,  $062^\circ$ T

8 2.5 m

10  $52^\circ 26'$

12 10.5 cm

14 63 km E, 54 km S

b  $325^\circ$ T

18  $111^\circ 48'$ T, 108 km