## Stem-and-leaf plots

## WALT: Read and display stem and leaf plots

## Success Criteria: I can ....

- Represent numerical data
- Split numbers into two parts when there are two digits
- Understand that each number is split into a stem (first digit) and a leaf (the last digit)


## Teacher Introduction



## Let's start: Test score analysis

In a class, students' results on two recent tests out of 50 are recorded.

> Test 1 results
> $43,47,50,26,38,20,25,20,50,44$,
> $33,47,47,50,37,28,28,22,21,29$

- For each test, try to find how many students:
- achieved a perfect score (i.e. 50)
- failed the test (i.e. less than 25)
- achieved a mark in the 40s.
- If there are 100 test results to analyse, would you prefer a list



## Key Ideas

- A stem-and-leaf plot is a way to display numerical data.
- Each number is split into a stem (the first digit or digits) and a leaf (the last digit).
For example:

$$
\begin{array}{rr|l} 
& \text { Stem } & \text { Leaf } \\
\cline { 2 - 3 } \text { The number } 7 \text { is } & 0 & 7 \\
\text { The number } 31 \text { is } & 3 & 1 \\
\text { The number } 152 \text { is } & 15 & 2
\end{array}
$$

- Leaves are aligned vertically, getting bigger as you move away from the stem.

Stem-andleaf plot A table that lists numbers in order, grouped in rows

1 Copy and complete:
In a stem-and-leaf plot the first digit(s) of a data value is called the $\qquad$ and the last digit is called the $\qquad$ —.

2 The number 52 is entered into a stem-and-leaf plot.
a Which digit is the stem?
b Which digit is the leaf?

3 What number is represented by the following combinations?
a $3 \mid 9$
b $2 \mid 7$
C $13 \mid 4$

4 In this stem-and-leaf plot, the smallest number is 35. What is the largest number?

| Stem | Leaf |  |  |  |
| ---: | :--- | :--- | :--- | :--- |
| 3 | 5 | 7 | 7 | 9 |
| 4 | 2 | 8 |  |  |
| 5 | 1 | 7 |  |  |
|  |  |  |  |  |

## Interpreting Stem and Leaf Plots

Average daily temperatures are shown for some different countries.
a Write out the temperatures as a list.
b How many countries' temperatures are represented?
c What are the maximum and minimum temperatures?
d What is the range of temperatures recorded?

| Stem | Leaf |  |  |  |  |  |  |  |  |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 3 | 6 | 6 |  |  |  |  |  |  |
| 2 | 0 | 0 | 1 | 2 | 5 | 5 | 6 | 8 | 9 |
| 3 | 0 | 2 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

e What is the median temperature recorded?

Solution
a $13,16,16,20,20,21,22,25,25,26$, 28, 29, 30, 32
b 14
c minimum $=13$
maximum $=32$
d range $=19$
e median $=23.5$

## Explanation

Each number is converted from a stem and a leaf to a single number.
For example, $1 \mid 3$ is converted to 13.

The easiest way is to count the number of leaves - each leaf corresponds to one country.

The first stem and leaf is $1 \mid 3$.
The last stem and leaf is $3 \mid 2$.
Range $=$ maximum - minimum $=32-13=19$
The middle value is halfway between the numbers $2 \mid 2$ and $2 \mid 5$, so median
$=\frac{1}{2}(22+25)=23.5$

5 This stem-and-leaf plot shows the ages of people in a group.
a Write out the ages as a list.
b How many ages are shown?
c Answer true or false to each of the following.
i The youngest person is aged 10 .

ii Someone in the group is 17 years old.
iii Nobody listed is aged 20.
iv The oldest person is aged 4.

6 For each of the stem-and-leaf plots below, state the range and the median. (See Example 8 parts $\mathbf{d}$ and e.)
a

c

| Stem | Leaf |  |  |  |  |  |  |  |  |  |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 3 | 1 | 1 | 2 | 3 | 4 | 4 | 8 | 8 | 9 |  |
| 4 | 0 | 1 | 1 | 2 | 3 | 5 | 7 | 8 |  |  |
| 5 | 0 | 0 | 0 |  |  |  |  |  |  |  |

b

| Stem | Leaf |  |  |  |  |  |  |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 4 | 8 |  |  |  |  |
| 2 | 1 | 2 | 4 | 4 | 6 | 8 |  |
| 3 | 0 | 3 | 4 | 7 | 9 |  |  |
| 4 | 2 |  |  |  |  |  |  |

7 Copy and complete the stem-and-leaf plot for this set of data.
$25,27,29,30,32,39,41,42,45,51$


## Creating Stem and Leaf Plot

Represent this set of data as a stem-and-leaf plot: $23,10,36,25,31,34,34,27,36,37,16,33$

## Solution

Sorted list: 10, 16, 23, 25, 27, 31, 33, 34, 34, 36, 36, 37

| Stem | Leaf |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 0 | 6 |  |  |  |
| 2 | 3 | 5 | 7 |  |  |
| 3 | 1 | 3 | 4 | 4 | 6 |

## Explanation

Sort the list in increasing order so that it can be put directly into a stem-and-leaf plot.
Split each number into a stem and a leaf. Stems are listed in increasing order. Leaves are written vertically, listed in increasing order across each row.

8 Show each of the following sets of data as a stem-and-leaf plot.
a $11,12,13,14,14,15,17,20,24,28,29,31,32,33,35$
b $20,22,39,45,47,49,49,51,52,52,53,55,56,58,58$
9 Show each of the following as a stem-and-leaf plot.
a $21,35,24,31,16,28,48,18,49,41,50,33,29,16,32$
b $32,27,38,60,29,78,87,60,37,81,38,11,73,12,14$
10 Show each of the following sets of data as a stem-and-leaf plot.
a $80,84,85,86,90,96,101,104,105,110,113,114,114,115,119$
b $401,420,406,415,416,406,412,402,409,418,404,405,391$, $411,413,413,408,395,396,417$

Remember, 101 is represented as $10 \mid 1$.

## Problem solving

## Back-to-back stem-and-leaf plots

13 Two radio stations poll their audience to determine their ages.

| Station 1 | Stem | Station 2 |
| :---: | :---: | :---: |
| 0 | 1 | 23345689 |
| 87 | 2 | 00124588 |
| 975433 | 3 | 112 |
| 7655441 | 4 | 8 |
| 9320 | 5 |  |

a Find the age difference between the oldest and youngest listener polled for:
i station 1 ii station 2
b One radio station plays modern music that appeals to teenagers. The other plays classical music and broadcasts the news. Which radio station is most likely to be the one that plays classical music and news?
c Advertisers want to know the age of the stations' audiences.


This lets them target their advertisements more effectively (e.g. to 38 to 58 year olds).
Give a 20 -year age range for the audience majority who listen to:
i station 1
ii station 2

Check your answers

-..-.-..----
1 a stem, leaf
2 a 5 b 2
$\begin{array}{llll}3 & \text { a } 39 & \text { b } 27 & \text { c } 134\end{array}$
457
5 a $8,9,10,11,13,15,17,18,21,24$ b 10
c i false ii true iii true iv false
6 a range $=20$, median $=17$
b range $=31$, median $=26$
c range $=19$, median $=40.5$

7 | Stem | Leaf |
| ---: | ---: |
| 2 | 579 |

3029

| 4 | 125 |
| :--- | :--- |
| 5 | 1 |

8 a Stem

| 1 | 1234457 |
| :--- | :--- |
| 2 | 0489 |
| 3 | 1235 |

b Stem | Leaf |  |
| ---: | :--- |
| 2 | 02 |
| 3 | 9 |
| 4 | 5799 |
| 5 | 12235688 |

9 a | Stem | Leaf |
| ---: | :--- |
| 1 | 668 |
| 2 | 1489 |
| 3 | 1235 |
| 4 | 189 |
| 5 | 0 |

10 a | Stem | Leaf |
| ---: | :--- |
|  | 0456 |
| 9 | 06 |
| 10 | 145 |
| 11 | 034459 |

b Stem | Leaf |  |
| ---: | :--- |
| 39 | 156 |
| 40 | 12456689 |
| 41 | 12335678 |
| 42 | 0 |

11 a 10
b 1
C 8
d 58

12a 15
b 13
c $a$ is 5 or $6, b$ is $0, c$ is 8 or $9, d$ is 0 .
13 a i 49 years ii 36 years b radio station 1
c i 33 to 53 years
ii 12 to 32 years

