## A Complete Guide to ...



Utilising the objectives as written in
MATHEMATICS in the New Zealand CURRICULUM for

## Level 5

This resource contains:
$\square$ Table of contents
$\square$ Teaching notes
$\square$ In class activity sheets involving

- worked examples
- basic skills
- word problems
- problem solving
- group work

$\square$ Homework / Assessment activity sheets
$\square$ Answers

These resources are supplied as PHOTOCOPY MASTERS
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Note from the author:
This resource ...

## *A Complete Guide to Number

is one of a series of FIVE resources written utilising the objectives as stated in
Mathematics in the New Zealand Curriculum for Level 5.
With my experiences as a specialist mathematics teacher, I enjoyed mathematics as a subject, but I am aware that not all teachers feel the same way about mathematics. It can be a difficult subject to teach, especially if you are unsure of the content or curriculum and if resources are limited.

This series of resources has been written with you in mind. I am sure you will find this resource easy to use and of benefit to you and your class.

## Resources in this series:

## *A Complete Guide to Number

written utilising the objectives as stated in

## A Complete Guide to Measurement

written utilising the objectives as stated in
Resource Code: L5MM
Mathematics in the New Zealand Curriculum for Level 5.

## A Complete Guide to Geometry

written utilising the objectives as stated in
Mathematics in the New Zealand Curriculum for Level 5.

## A Complete Guide to Algebra

written utilising the objectives as stated in
Mathematics in the New Zealand Curriculum for Level 5.

## A Complete Guide to Statistics

written utilising the objectives as stated in
Mathematics in the New Zealand Curriculum for Level 5.

Resource Code: L5MS

For more information about these and other resources, please contact ...


This resource has been divided into EIGHT sections as listed below. Although there are no page numbers, the sections follow in sequential order as listed.

Note: 'In-class’ Worksheets Masters are lesson by lesson reuseable worksheets that can be photocopied or copied on to an OHP.

Homework / Assessment Worksheets Masters can be used as homework to reinforce work covered in class or they can be used for pupil assessment.


Number
The following are the objectives for Number, Level 5, as written in the MATHEMATICS in the New Zealand Curriculum document, first published 1992. [Refer Page 48]

## Exploring number

Within a range of meaningful contexts, students should be able to:

- N1 convert numbers expressed in standard form to ordinary form, and vice versa;
- N2 round numbers sensibly;
- N3 express the values of square roots in approximate and exact forms;


## Exploring computation and estimation

Within a range of meaningful contexts, students should be able to:

| - | N4 | make sensible estimates and check the reasonableness of results; |
| :--- | :--- | :--- |
| - | $\mathbf{N 5}$ | solve practical problems involving decimals and percentages; <br> - <br> solve problems involving positive and negative numbers, using practical activities or <br> models if needed; |
| - | N7 | express one quantity as a percentage of another; <br> increase and decrease quantities by given percentages, including mark up, discount, <br> and GST; |
| - N8 | N9are quantities in given ratios. |  |

At the top of each 'In-class' worksheet and Homework I Assessment worksheet, the Number objective(s) being covered has been indicated. EXAMPLE: N1 means objective 1, N2 means objective 2, etc.


The Mathematical Processes Skills: Problem Solving,
Developing Logic \& Reasoning,
Communicating Mathematical Ideas,
are learned and assessed within the context of the more specific knowledge and skills of number, measurement, geometry, algebra and statistics. The following are the Mathematical Processes Objectives for Level 5.
Problem Solving Achievement Objectives [Refer page 24]

| - | MP1 | pose questions for mathematical exploration; |
| :--- | :--- | :--- |
| - | MP2 | effectively plan mathematical exploration; |
| - | MP3 | devise and use problem-solving strategies to explore situations mathematically; |
| - | MP4 | find, and use with justification, a mathematical model as a problem-solving strategy; |
| - | MP6 | use equipment appropriately when exploring mathematical ideas. |

Developing Logic and Reasoning Achievement Objectives [Refer page 26]

| - | MP8 | classify objects, numbers and ideas; |
| :--- | :--- | :--- |
| - | MP9 | interpret information and results in context; |
| - | MP10 | make conjectures in a mathematical context; |
| - | MP11 | generalise mathematical ideas and conjectures; |
| - | MP15 | use words and symbols to describe and generalise patterns. |

## Communicating Mathematical Ideas Achievement Objectives [Refer page 28]

| - | MP16 | use their own language and mathematical language and diagrams to explain mathematical ideas; |
| :--- | :--- | :--- |
| - | MP17 | devise and follow a set of instructions to carry out a mathematical activity; |
| - | MP20 | record information in ways that are helpful for drawing conclusions and making generalisations; |
| - | MP21 | report the results of mathematical explorations concisely and coherently. |

[^0] to PAGES 23-29 of the CURRICULUM DOCUMENT]

## 'In-class’ Number Worksheets

Table of Worksheet Number / Objectives Covered
See the opposite page for details of each objective.

|  | Number Objectives |  |  |  |  |  |  |  |  |  | Mathematical Processes Objectives |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Worksheet Number | R | $N$  <br> 1  | N 2 | N 3 | N <br> 4 | N 5 | N 6 | $N$ 7 | (N <br> 8 | N 9 | MP | MP | MP <br> 3 | MP | MP 6 | MP | ${ }_{\text {MP }}^{\text {MP }}$ | MP | MP <br> 11 | \|r| | MP | MP <br> 17 | 10 <br> 20 | MP |
| 1 | * |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | * |  |  |  |  |  |  |  |
| 2 | * |  |  |  |  |  |  |  |  |  | * |  | * |  |  |  | * |  |  |  |  |  |  |  |
| 3 | * |  |  |  |  |  |  |  |  |  | * |  | $\times$ |  |  |  | $\times$ |  |  |  |  |  |  |  |
| 4 | * |  |  |  |  |  |  |  |  |  | $\times$ |  | * |  |  |  | * |  |  |  |  |  |  | * |
| 5 | * |  |  |  |  |  |  |  |  |  | $\times$ |  | * |  |  |  | * |  |  |  |  | * |  |  |
| 6 |  | * |  |  |  |  |  |  |  |  | $\times$ |  | $\times$ |  |  |  | * |  |  |  |  | $x$ |  |  |
| 7 |  |  | * |  | * |  |  |  |  |  | * |  | * |  |  |  | * |  |  |  |  | $\times$ |  |  |
| 8 |  |  | $\times$ |  | $x$ |  |  |  |  |  | * |  | * |  |  |  | * |  |  |  |  | * |  |  |
| 9 |  |  | * | $\times$ | * |  |  |  |  |  |  |  | * |  |  |  | * |  |  |  |  |  |  |  |
| 10 | * |  |  |  |  |  |  |  |  |  |  |  | $\times$ |  |  |  | * |  |  |  |  | $\times$ |  |  |
| 11 | * |  |  |  |  |  |  |  |  |  |  |  | * |  |  |  | * |  |  |  |  | $\times$ |  |  |
| 12 |  |  |  |  |  | * |  |  |  |  | * |  | $\times$ |  |  |  | * |  |  |  |  | $\times$ |  |  |
| 13 |  |  |  |  |  | $\times$ |  |  |  |  | $\times$ |  | $\times$ |  |  |  | * |  |  |  |  | $\times$ |  |  |
| 14 |  |  |  |  |  |  | * |  |  |  | $\times$ |  | $\times$ |  |  |  | * |  |  |  |  |  |  |  |
| 15 |  |  |  |  |  |  | * |  |  |  | $\times$ |  | $\times$ | $\boldsymbol{x}$ |  |  | * |  |  |  | * |  |  |  |
| 16 |  |  |  |  |  |  | * |  |  |  | $\times$ |  | $\times$ | * |  |  | $\times$ |  |  |  |  |  |  |  |
| 17 |  |  |  |  |  |  |  | * |  |  | * |  | * |  |  |  | * |  |  |  |  | $\times$ |  |  |
| 18 |  |  |  |  |  |  |  |  | * |  | $x$ |  | * |  |  |  | * |  |  |  |  | $x$ |  |  |
| 19 |  |  |  |  |  |  |  |  |  | $\times$ | $x$ |  | * |  |  |  | * |  |  |  |  | $\times$ |  |  |
| 20 |  |  |  |  |  |  |  |  |  | $\times$ | $x$ |  | $\times$ |  |  |  | * |  |  |  |  | $\times$ |  |  |
| 21 |  |  |  |  |  |  |  |  |  |  | $\times$ |  | $\times$ |  |  |  | * |  |  |  |  | $\times$ |  |  |
| 22 |  |  |  |  |  |  |  |  |  | * | * |  | * |  |  |  | * |  |  |  |  | * |  |  |

## Table of Contents for the 'In-class' Worksheet Masters for Number, Level 5

| Worksheet Number | Topic | Number Objective(s) |
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| 2 | Special numbers | Revision |
| 3 | Order of operations | Revision |
| 4 | Word problems involving order of operations | Revision |
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| 7 | Approximations, estimations \& rounding using decimal places | N2 / N4 |
| 8 | Approximations, estimations \& rounding significant figures | N2 / N4 |
| 9 | Finding squares and estimating square roots | N2 / N3 / N4 |
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| 18 | Increasing and decreasing by a given percentage | N8 |
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| 20 | Sharing quantities by a given ratio | N9 |
| 21 | Creating equivalent fractions and simplifying fractions | N9 |
| 22 | Improper fractions and mixed numbers / Adding and subtracting fractions | N9 |
|  | Teaching Notes / Answers | \| |



## Adding and subtracting whole numbers:

The ability to add and subtract with speed and accuracy is a useful skill.
Setting out is important, especially when a calculator is not being used.
Example: $6231+736$ could be written as ... 6231 and 2018-437 could be written as ...
2018
$+736$
-437

## Task 1



1. Copy this 'number cross' into the squares of your maths book.
2. Use the clues for across and down to complete the number cross by working out these addition and subtraction problems.

## Clues across

1. $532+294$
2. 2335-485
3. 8020-475
4. $497+1735$
5. 4037-1528
6. 1542-749
7. 300-203
8. $247+516$
9. $1000-436$
10. $345+567$
11. 100000-7959

Clues down

1. $5243+2919$
2. $400-333$
3. $7523+8227$
4. $514-218$
5. $4127+5443$
6. $10000-4261$

7. $1689+4233$
8. $34905+37546$
9. $8000-2571$
10. 700-306

## Multiplying and dividing whole numbers:

The ability to multiply and divide with speed and accuracy is also a useful skill.
Setting out is important, to help avoid making mistakes.
Example: $294 \times 23$ could be written as ...

```
294
and 6412\div4 could be written as ... 4 }\lcm{6412
```


## Task 2



1. Copy this number cross into the squares of your maths book.
2. Use the clues for across and down to complete the number cross by working out these multiplication and division problems.

## Clues across

| 1. | $259 \times 3$ | 3. | $197 \times 9$ |
| :--- | :--- | :--- | :--- |
| 5. | $9638 \div 2$ | 7. | $392 \div 7$ |
| 9. | $540 \div 12$ | 11. | $1209 \times 5$ |
| 13. | $1914 \div 6$ | 15. | $1500 \div 12$ |
| 16. | $4625 \times 7$ | 19. | $85418 \times 5$ |

Clues down

1. $3575 \div 5$
2. $444 \div 6$
3. $93 \times 8$
4. $2568 \div 3$
5. $4210 \times 12$
6. $46260 \div 9$
7. $1116 \div 12$
8. $319 \times 6$
9. $592 \times 11$
10. $48 \times 7$
11. $780 \div 15$


## Task 3

Create an Addition \& Subtraction number-cross and a Multiplication \& Division number-cross as above, including clues and answers. Exchange each number-cross with a classmate and compare answers when completed.


## Special numbers:

"Is the number 7 a prime number?" asked Tracy.
"Can you list the first five multiples of 9?" asked Rangi.
"Can you list the factors of 15?" asked Abby.
Prime numbers, multiples, factors and prime factors are all special types of numbers.
Discuss what makes these numbers special.


## Task 4

Copy each sentence below about these special numbers, replacing the a with one of the words listed below.

1. A number can only be divided by two numbers, itself and 1.
2. The $n$ of a number are found by multiplying the number by $1,2,3,4,5$, etc and recording the answers.
3. A a of a given number is a whole number that divides exactly into the given number. There is no remainder.
4. $A \backsim$ is a factor that is a prime number.
```
    factor
        multiples
            prime
prime factor
```

Working with prime numbers.
5. List the first 15 prime numbers.
6. List the prime numbers between 70 and 90 .
7. Which numbers in this list are prime numbers? $3,9,12,13,19,21,25,29,33,37,43,49,53,81,93$

The number 12 can be written as two prime numbers. Example: $5+7=12$.
Write these numbers as two prime numbers. There may be more than one correct answer for each.

| 8. | 18 | 9. | 24 | 10. | 30 | 11. | 36 | 12. | 42 | 13. | 44 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 14. | 48 | 15. | 50 | 16. | 54 | 17. | 60 | 18. | 66 | 19. | 70 |

Working with multiples.
List the first 10 multiples of these numbers.
20. 7
21. 12
22. 14
23. 17
24. 20
25. 30
26. List the multiples of 9 that are less than 50 .
27. List the multiples of 11 that are between 40 and 80 .
28. List the multiples of 15 that are between 50 and 100.
29. List the multiples of 18 that are between 40 and 110.
30. List the multiples of 25 that are between 80 and 160.

Working with factors.
List the factors of these numbers.
31. 12
32. 20
33. 36
34. 48
35. 66
36. 72

The number 14 can be written as two prime factors. Example: $2 \times 7=14$
Write these numbers as two prime factors.
37. 15
38. 39
39. 55
40. 91
41. 119
42. 143

## Task 5

Guess the number game: Read the clues in the box below and then work out the number.
1.

2.

4. Create 5 similar 'Guess the number' questions, where there is only one correct answer.
Exchange your questions with a classmate.


## Order of operations:

When working out answers with questions involving a mixture of operations, the order in which they are done will affect the answer. The letters BODMAS or BEDMAS will hlep you to remember the order.
$B=$ brackets
$O=$ of $(E=$ exponents $)$
$D=$ division
$M=$ multiplication
$A=$ addition
$S$ This order means that you work out the brackets first, followed by ...
multiplying and dividing in the order they appear from left to right, followed by ...
adding or subracting in the order they appear from left to right.

Examples:

$$
\begin{aligned}
& 7 \times 8+11 \\
= & 56+11 \\
= & 67
\end{aligned}
$$

$$
\begin{aligned}
& 19+5 \times 4 \\
= & 19+20 \\
= & 39
\end{aligned}
$$

|  | $72 \div 8-5$ |
| :--- | :--- |
| $=$ | $9-5$ |$\quad 40-36 \div 30 子$| $=$ | $40-12$ |
| :--- | :--- |
|  | $=$ |



## Task 6

Calculate the following.

1. $9 \times 8+23$
2. $10 \times 8-43$
3. $25+9 \times 8$
4. $40 \div 8+15$
5. $65 \div 5-9$
6. $5 \times 12+27$
7. $19+54 \div 6$
8. $67-12 \times 4$
9. $59-7 \times 6$
10. $112 \div 7+24$
11. $12 \times 9-59$
12. $84 \div 12+27$
13. $4 \times 12+18$
14. $24+63 \div 7$
15. $27+63 \div 9$
16. $57-13 \times 3$
17. $12 \times 11-77$
18. $12 \times 7+46$
19. $46+99 \div 11$
20. $95 \div 5-11$
21. $53-6 \times 7+24$
22. $13 \times 4+19$
23. $13 \times 5+38$
24. $144 \div 12+37$
25. $10 \times 9+43$
26. $102 \div 3-27$
27. $47+36 \div 3+24$
28. $29+9 \times 7-57$
29. $24+52 \div 13-17$
30. $9 \times 8 \div 6+37$
31. $55 \div 5 \times 7-19$
32. $29+9 \times 4 \div 12$
33. $81-32 \div 8 \times 12$
34. $12 \times 8-9 \times 7$
35. $8 \times 5+21 \div 3$
36. $7 \times 13-9 \times 9$
37. $35 \div 7+3 \times 15$

Problems involving brackets.
Example: $4(6+4)$ means $4 \times(6+4)=4 \times 10=40$

$$
6(24-3 \times 7)=6(24-21)=6 \times 3=18
$$

Use order of operation rules to work out the answers for these questions involving brackets.

| 41. | $3(5 \times 4+5)$ | 42. | $5(6 \times 6-19)$ | 43. | $6(29-4 \times 6)$ | 44. | $5(36 \div 9+9)$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 45. | $6(55 \div 5-7)$ | 46. | $7(8 \times 4+9)$ | 47. | $4(30 \div 6+11)$ | 48. | $9(58-7 \times 6)$ |
| 49. | $4(6 \times 6-19)$ | 50. | $6(36-3 \times 9)$ | 51. | $15(36 \div 9+6)$ | 52. | $8(6 \times 3+7)$ |
| 53. | $40-3(18 \div 3+2)$ | 54. | $15+3(2 \times 8+4)$ | 55. | $11+2(19-2 \times 7)$ | 56. | $50-4(5+20 \div 4)$ |
| 57. | $17+2(27-3 \times 8)$ | 58. | $40-3(18 \div 3+2)$ | 59. | $54-6(3 \times 8-18)$ | 60. | $13+9(27-3 \times 8)$ |

Copy and complete each statement by replacing the with + , -, $\times$ or $\div$ to make each statement true.

| 61. | 2 - 3 - $5=17$ | 62. | $5-3$ 6 $=21$ | 63. | 10 - 4 2 $=8$ | 64. | 12 - 3 - $7=28$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 65. | $9 \bullet 10$ 2 = 14 | 66. | $23-4 \bullet 5=3$ | 67. | $18 \bullet 6 \bullet 9=12$ | 68. | 8 - 3 - $7=31$ |
| 69. | $21-18$ - $3=15$ | 70. | $27 \bullet 9 \bullet 7=10$ | 71. | $7 \bullet 4 \bullet 6=31$ | 72. | 19 -36 12 = 16 |

73. Create 10 questions as above, where the operation signs are missing.

Exchange your questions with a classmate and have him / her add signs to make each statement true.


## Word problems involving order of operations:

Example: Sharon went to the shop bought five C.D.'s worth $\$ 19.95$ each and two tapes worth $\$ 11.50$ each.
Write an expression for this information, then calculate the total cost of this purchase.


Answer: $\quad$ Total cost of purchase $=5 \times \$ 19.95+2 \times \$ 11.50=\$ 99.75+\$ 23.00=\$ 122.75$

## Task 7

Calculate the cost of buying the follwoing number of C.D.'s and tapes.

1. 2 C.D.'s \& 3 tapes
2. 5 C.D.'s \& 7 tapes
3. $9 C . D$. 's \& 1 tape
4. 
5. 3 C.D.'s \& 10 tapes
6. 7 C.D.'s \& 5 tapes
7. 1 C.D. \& 6 tapes
8. 6 C.D.'s \& 4 tapes
9. 10 C.D.'s \& 8 tapes
10. If Karen has $\$ 90.00$, how many C.D.'s can she buy?
11. If John has $\$ 60.00$ and buys 3 tapes, how much change does he get?
12. If Rebecca has $\$ 100$ and buys 2 C.D's and 4 tapes, how much change does she get?

beans
$\$ 2.90 / \mathrm{kg}$

cheese $\$ 5.40$ / 1kg block

| List A |
| :---: |
| 2 kgs of carrots |
| 12 corn cobs |
| 1 dozen eggs |
| 1 kg of mushrooms |
| 1 kg block of cheese |
| 2 kgs of beans |


List D


| List H |
| :---: |
| 2 kgs of mushrooms |
| $11 / 2 \mathrm{kgs}$ of beans |
| 3 kgs of bananas |
| 15 corn cobs |
| 6 kgs of potatoes |
| 2 kgs of cheese |
| 3 kgs of carrots |



## Multiplying and dividing by powers of 10:

Some of the powers of 10 and the numbers they represent are listed below.

$$
10^{1}=10,10^{2}=100,10^{3}=1000,10^{4}=10000
$$

To multiply by the powers of 10 is not as difficult as it might seem.
Examples: $3.7 \times 10000=37000,78.3 \times 100=7830,236.9 \div 100=2.369,1.2 \div 1000=0.0012$


In each example, the digits have remained the same, but the decimal point has moved.

## Task 8

Calculate the following.

1. $6.9 \times 10$
2. $2.3 \times 10000$
3. $84 \times 100$
4. $0.6 \times 1000$
5. $2.3 \times 100$
6. $4.09 \times 1000$
7. $94.3 \times 1000$
8. $8.05 \times 10000$
9. $963 \times 1000$
10. $0.08 \times 100$
11. $3.84 \times 100000$
12. $0.059 \times 100$
13. $3.7 \times 10^{5}$
14. $\quad 6.7 \times 10^{4}$
15. $4.3 \times 10^{7}$
16. $5.2 \times 10^{5}$
17. Look at the answers for the questions above involving multiplication. Can you describe a simple method for working out the answers without having to actually do the calculation?

Calculate the following.
18. $9.6 \div 100$
19. $1.3 \div 1000$
20. $63 \div 100000$
21. $934 \div 1000$
22. $4.1 \div 10$
23. $4.37 \div 100$
24. $672.8 \div 100$
25. $18.63 \div 10000$
26. $952 \div 1000$
27. $0.85 \div 100000$
28. $4.09 \div 1000$
29. $0.096 \div 10$
30. $7.6 \div 10^{5}$
31. $6.9 \div 10^{3}$
32. $6.3 \div 10^{6}$
33. $2.5 \div 10^{3}$
34. Look at the answers for the questions above involving division. Can you describe a simple method for working out the answers without having to actually do the calculation?

Use your methods described above to answer these questions.
35. $2.59 \times 10^{4}$
36. $4.37 \div 10^{3}$
37. $7.21 \times 10^{6}$
38. $\quad 6.074 \div 10^{3}$
39. $9.07 \div 10^{5}$
40. $\quad 7.361 \times 10^{7}$
41. $5.42 \div 10^{5}$
42. $4.021 \times 10^{6}$


Seats in an ice hockey stadium are in rows of 100 seats.
43. Calculate the number of seats in 36 rows.
44. How many rows of seats are filled if 1275 tickets have been sold for Saturday's game?

A school sells pens and note books to its pupils.
45. Calculate the cost of buying 100 pencils at 18 cents each.
46. If 1000 school note books cost $\$ 540.00$, what would it cost to buy one note book?


A brick fence is to be built using 100000 bricks.
47. Calculate the cost of the bricks, if each brick costs 19 cents.
48. If 10000 bricks cost $\$ 2300.00$, calculate the cos $\dagger$ of one brick.

A national supermarket chain sold about 100000 1L cartons of milk during the year.
49. If milk sells for $\$ 1.25$ per 1 L carton, what is the total value of milk sales for the year?

The supermarket also sold 10000 cartons of flavoured milk, for total sales of $\$ 16500$.
50. What was the cost of the each carton of flavoured milk?


A local power company sells power at a rate of 12.330 cents per unit.
51. Calculate the cost (\$) if 100000 units of power have been used.

52. After a price increase, 10000 units of power cost $\$ 1275$.

What is the new price per unit for the power?


## Standard form $\Leftrightarrow$ decimal form:

A number such as $1.2 \times 10^{3}$ is said to be written in standard form. Numbers written in standard form consist of two parts, a decimal number and a power of 10 .

The decimal number ALWAYS has just one non-zero digit before the decimal point.
Such as, 2.3, 5.35, 8.369, etc.
Example: $3.6 \times 10^{3}, 6.86 \times 10^{5}, 8.6 \times 10^{-3}, \& 9.347 \times 10^{-5}$.

Answers: $3.6 \times 1000=3600,6.86 \times 100000=686000$,

$$
8.6 \times 0.001=0.0086,9.347 \times 0.00001=0.00009347
$$

## Task 9

Convert these standard form numbers to decimal or whole numbers.

1. $9.0 \times 10^{2}$
2. $6.0 \times 10^{-2}$
3. $\quad 5.3 \times 10^{4}$
4. $6.6 \times 10^{-3}$
5. $2.7 \times 10^{-3}$
6. $9.3 \times 10^{5}$
7. $1.9 \times 10^{-3}$
8. $2.4 \times 10^{5}$
9. $3.24 \times 10^{3}$
10. $1.93 \times 10^{-4}$
11. $3.47 \times 10^{5}$
12. $9.12 \times 10^{-3}$
13. $7.63 \times 10^{-6}$
14. $5.34 \times 10^{5}$
15. $\quad 9.04 \times 10^{-4}$
16. $7.35 \times 10^{5}$
17. $\quad 9.4 \times 10^{-4}$
18. $3.06 \times 10^{-3}$
19. $1.26 \times 10^{6}$
20. $3.93 \times 10^{-4}$
21. $3.101 \times 10^{5}$
22. $6.327 \times 10^{-4}$
23. $4.106 \times 10^{-5}$
24. $6.318 \times 10^{5}$

Convert these decimal or whole numbers to standard form numbers.

| 25. | 2500 | 26. | 0.042 | 27. | 42500 | 28. | 0.0056 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 29. | 584000 | 30. | 2351 | 31. | 0.00034 | 32. | 63150000 |
| 33. | 586.2 | 34. | 0.0000254 | 35. | 956.63 | 36. | 0.000039 |
| 37. | 0.0000045 | 38. | 85620000 | 39. | 0.004126 | 40. | 9635.45 |
| 41. | 952300000 | 42. | 0.00002105 | 43. | 0.00000931 | 44. | 37920.68 |
| 45. | 0.00003625 | 46. | 30049500 | 47. | 120450400 | 48. | 0.00000000069 |

49. Calculate the number of seconds in 1 day, 1 week and 1 year. Convert your answers to standard form.

50. An aeroplane has travelled approximately $3.5 \times 10^{5} \mathrm{~km}$ in the past 6 months. Convert this distance to an ordinary number. An aeroplane makes 3 return trips daily between two cities that are 850 km apart.
51. Calculate the distance the plane travels in 1 day, 1 week and 1 year.

Convert your answers to standard form.

At a milk treatment plant, one litre containers of milk are filled at a rate of 120 per hour.
52. Calculate the number of containers filled in 12 hours.
53. If the milk treatment plant operates 12 hours a day for five days a week, how many litres of milk would be produced in a 4 week period? Convert your answer to standard form.
54. In 50 hours of production, $6.5 \times 10^{3} 1 \mathrm{~L}$ containers of milk were produced.

What was the hourly rate of production?

55. If $2.315 \times 10^{5}$ Christmas cards were posted in 5 days, what is the average number of Christmas cards posted each day?
56. At a local Post Office, an average of 1250 letters are posted each week of the year. Calculate the number of letters posted in one year. Convert your answer to standard form


## Approximations, estimations \& rounding using decimal places:

When calculating or taking measurements, approximations can be used. One way to approximate a number is to round it off to a certain number of decimal places (d.p.).
Example: $\quad 5.32=5.3$ rounded to 1 decimal place, $\quad 5.329=5.33$ ( 2 d.p.)
Round 9.65 to 1 d.p.
Answer: 9.7 (1 d.p.)


When rounding a number to a certain number of decimal places, count the required digits from the decimal point. If the next number is 5 or above, add 1 to the last digit. If the next digit is below 5 , leave it as it is.

## Task 10

Round each number to 1 decimal place ( 1 d.p.), 2 decimal places (2 d.p.) and 3 decimal places ( 3 d.p.)

| 1. | 1.2364 | 2. | 3.6041 | 3. | 9.7532 | 4. | 10.6347 | 5. | 0.05643 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6. | 23.5067 | 7. | 18.4629 | 8. | 53.4219 | 9. | 143.8891 | 10. | 6.3851 |
| 11. | 0.09578 | 12. | 9.2596 | 13. | 186.0709 | 14. | 1.0006 | 15. | 56.7561 |
| 16. | 5602.7034 | 17. | 0.05295 | 18. | 6.40932 | 19. | 67.1596 | 20. | 0.9637 |
| 21. | 2.71999 | 22. | 9058.0975 | 23. | 0.008694 | 24. | 9.46209 | 25. | 702.96420 |
| 26. | 0.000529 | 27. | 4.6009 | 28. | 0.9999 | 29. | 56 | 30. | 132 |

Work out each question then round your answers to 1 d.p. and 2 d.p.

| 31. | $19.953+4.485$ | 32. | $75.032-49.966$ | 33. | $2.53 \times 1.2$ | 34. | $45.5 \div 9$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 35. | $36.8 \div 7$ | 36. | $0.9 \times 4.986$ | 37. | $3.039+12.968$ | 38. | $10.969-3.854$ |
| 39. | $23.689+4.485$ | 40. | $63.7 \div 9$ | 41. | $120.635-89.966$ | 42. | $6.742 \times 1.2$ |
| 43. | $23.6+1.03 \times 3.4$ | 44. | $5.32 \times 1.2+9.564$ | 45. | $1.95+2.65 \div 4$ | 46. | $15.6 \div 8+4.906$ |
| 47. | $16-39.1 \div 8$ | 48. | $42.63 \div 6+2.98$ | 49. | $8.3-3.05 \times 0.9$ | 50. | $3.8 \times 2.34-2.499$ |
| 51. | $3.64+9.25 \div 8$ | 52. | $27.561 \div 5-1.94$ | 53. | $6.74 \times 2.2+6.37$ | 54. | $26.3-64.404 \div 12$ |

In a 1 km track cycle race, the top 10 competitors' times were recorded in seconds to 3 decimal places.

$$
68.237,71.632,69.048,75.396,71.284,68.956,70.653,69.378,72.564,69.637
$$

55. List these times in order of fastest to slowest. 56. Round each time to 2 d.p.

In a computer car racing game, the top 10 fastest lap times were as follows ...
$1 \mathrm{~min} 56.35 \mathrm{sec}, 1 \mathrm{~min} 45.72 \mathrm{sec}, 1 \mathrm{~min} 63.79 \mathrm{sec}, 1 \mathrm{~min} 50.27 \mathrm{sec}, 1 \mathrm{~min} 49.93 \mathrm{sec}$,
$1 \mathrm{~min} 49.76 \mathrm{sec}, 1 \mathrm{~min} 51.63 \mathrm{sec}, 1 \mathrm{~min} 52.09 \mathrm{sec}, 1 \mathrm{~min} 48.74 \mathrm{sec}, 1 \mathrm{~min} 51.95 \mathrm{sec}$
57. List these times in order of slowest to fastest.
58. Round each time to 1 d.p.

A machine is used to filled juice container.
59. Calculate the total volume of juice if 125 containers were filled, with an average volume of 1002.16 mL per container. Answer in mL and L .
60. Round your answer in litres to 1 d.p.
61. If each container of juice sells for $\$ 1.75$ each, calculate the cost to buy 125 containers of juice.

62. Create your own questions that involve decimal calculation. Exchange your questions with a classmate so that she / he can work out the answers, rounding the answers to 1 d.p. and 2 d.p.


## Approximations, estimations \& rounding significant figures:

When calculating or taking measurements a second way to approximate an answer is to round off to a certain number of significant figures (s.f.).
Example: $\quad 634=600$ rounded to 1 significant figure, $\quad 634=630$ (2 s.f.)

Round 2762 to 2 s.f.
Round 0.00056 to 1 s.f.

Answer: 2800 (2 s.f.)
Answer: 0.0006 ( 1 s.f.)


When rounding a number to a certain number of significant figures, count the required number of digits from the first non-zero digit. If the next number is 5 or above, add 1 to the previous digit. If the next digit is below 5 , leave it as it is. Remember to add the zeros needed to keep place values correct.

## Task 11

Round each number to 1 significant figure (1 s.f.), 2 significant figures ( 2 s.f.) and 3 significant figures ( 3 s.f.)

| 1. | 4263 | 2. | 93721 | 3. | 43968 | 4. | 7592 | 5. | 645056 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6. | 0.05236 | 7. | 0.008532 | 8. | 0.0004647 | 9. | 0.48596 | 10. | 3.6984 |
| 11. | 0.09578 | 12. | 9.2596 | 13. | 186.0709 | 14. | 1.0006 | 15. | 56.7561 |
| 16. | 5602.7034 | 17. | 0.05295 | 18. | 6.40932 | 19. | 167.1596 | 20. | 0.9637 |
| 21. | 2.71999 | 22. | 58.0975 | 23. | 0.008694 | 24. | 9.46209 | 25. | 322.969 |
| 26. | 0.030529 | 27. | 4.6009 | 28. | 485.321 | 29. | 27 | 30. | 0.65 |

Work out each question then round your answers to 1 s.f. and 2 s.f.
31. $5261+369$
32. 7845-3659
33. $2531 \times 25$
34. $369 \div 4$
35. $963.4 \div 7$
36. $0.9 \times 639.48$
37. $593.9+12.96$
38. 968.5-86.34
39. $1968.9+586.5$
40. $56.97 \div 8$
41. 69.853-51.966
42. $\quad 0.053 \times 1.5$
43. $968+25 \times 9$
44. $856 \times 8+349$
45. $98.6+43.8 \div 4$
46. $\quad 89.4 \div 8+96.87$
47. $685-245 \div 8$
48. $658.6 \div 6+981$
49. $1859-56 \times 7$
50. $5.6 \times 2.5-2.76$
53. $9.45 \times 2.2+12.53$
54. $37.3-82.236 \div 12$

The distance a delivery truck travels each day for two weeks has been recorded below.
$126 \mathrm{~km}, 263 \mathrm{~km}, 189 \mathrm{~km}, 215 \mathrm{~km}, 462 \mathrm{~km}, 97 \mathrm{~km}, 378 \mathrm{~km}, 235 \mathrm{~km}, 167 \mathrm{~km}, 81 \mathrm{~km}$
55. Estimate the total distance travelled by first rounding each distance to 2 significant figures.
56. Calculate the actual distance travelled.
57. What is the difference between the estimated distance and actual distance travelled?


The weekly crowd attendance of people watching a rugby match for the first 10 rounds of the competition are recorded below.

## 12432, 9865, 13462, 11251, 10065, 9963, 11523, 10364, 12678, 9562

58. Estimate the total crowd attendance by first rounding each number to 2 significant
 figures.
59. Calculate the actual crowd attendance.
60. What is the difference between the estimated crowd numbers and actual crowd numbers?
61. Create your own questions that involve whole number calculations. Exchange your questions with a classmate so that she / he can work out the answers, rounding the answers to 1 s.f. and 2 s.f.


## Finding squares and estimating square roots:

When a number is multiplied by itself, such as ... $1 \times 1,2 \times 2,3 \times 3,4 \times 4,5 \times 5,6 \times 6,7 \times 7,8 \times 8$ etc. ...
the answers that are created, are numbers known as squares. That is, $1,4,9,16,25,36,49,64, \ldots$
These can be written as $1^{2}, 2^{2}, 3^{2}, 4^{2}, 5^{2}$, etc., where the small number 2 is called a power.
The opposite of squaring a number is to find the square root. The symbol for square root is $\sqrt{ }$. Example: If $9^{2}=81$, then $\sqrt{81}=9$.

The square root of a number can be estimated, by a trial and error method and using a calculator.
 Example: Find $\sqrt{60} \quad 7^{2}=49$ and $8^{2}=64$,

$$
\begin{array}{ll}
\text { try } 7.8^{2} & \text { answer: } 60.84 \text { too high } \\
\text { try } 7.75^{2} & \text { answer: } 60.0625 \text { close enough? }
\end{array}
$$

This trial and error method can be repeated several times until you get a more accurate answer.

## Task 12

Calculate the squares of these numbers, accurate to 1 d.p.

1. $6.3^{2}$
2. $8.6^{2}$
3. $\quad 10.5^{2}$
4. $11.7^{2}$
5. $12.6^{2}$
6. $\quad 18.3^{2}$
7. $46.8^{2}$
8. $59.7^{2}$
9. $\quad 96.4^{2}$
10. $112.8^{2}$

Calculate the squares of these numbers, accurate to 2 d.p.
11. $2.36^{2}$
12. $6.95^{2}$
13. $4.98^{2}$
14. $9.73^{2}$
15. $9.65^{2}$
16. $7.13^{2}$
17. $0.36^{2}$
18. $9.61^{2}$
19. $8.65^{2}$
20. $3.096^{2}$

Estimate the square root of these numbers to 2 d.p. accuracy. (Do not use the $\sqrt{ }$ key on your calculator.)

| 21. | 20 | 22. | 27 | 23. | 40 | 24. | 55 | 25. | 60 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 26. | 69 | 27. | 75 | 28. | 80 | 29. | 85 | 30. | 110 |
| 31. | 130 | 32. | 150 | 33. | 168 | 34. | 200 | 35. | 250 |
| 36. | 9.7 | 37. | 12.9 | 38. | 33.9 | 39. | 42.9 | 40. | 76.8 |
| 41. | 0.95 | 42. | 56.78 | 43. | 139.4 | 44. | 563.9 | 45. | 862.7 |

46. Use the $\sqrt{ }$ key on your calculator to find the exact square root of each number above, accurate to 4 d.p.


A courtyard 10 metres by 10 metres is made up of 256 square cobble stones.
47. Calculate the number of cobbles along each side of the courtyard.
48. Calculate the dimensions of one cobblestone.
49. If cobble stones cost $\$ 1.25$ each, what did it cost to cobble this courtyard?

A new kitchen measures 3.6 m by 3.6 m . The floor is to be covered with square floor tiles, that measure 30 cm by 30 cm .
50. Calculate the number of floor tiles needed to go along one side of the kitchen.
51. Calculate the number of floor tiles needed to tile the kitchen floor.
52. If floor tiles cost $\$ 0.65$ each, what is the cost of tiling the kitchen floor?
53. A second room in this house has been tiled using 64 tiles. If this room is shaped like a square, how many tiles along one side of the room?

54. What is the dimension of this room? Give your answer in metres.


## Expressing a fraction as a decimal:

The top number of a fraction is called the numerator. The bottom number is called the denominator. Example: In the fraction $\frac{5}{8}, 5$ is the numerator and 8 is the denominator.

Fractions can be converted into decimals by dividing the numerator by the denominator.
Example: Convert $\frac{5}{8}$ to a decimal.


Answer: The fraction $\frac{5}{6}$ converted to a decimal is 0.625 .
Some fractions can be simplified by dividing the numerator and denominator by the same number.
Example: $50 / 100$ (divide by 10 ) $=5 / 10$ (divide by 5$)=1 / 2$ This will make the conversion to a decimal easier.
Some fractions create interesting decimals, with a recurring pattern of digits.
Example: $\quad 2 / 9=0.2222^{\prime}$ This small dot means that the 2's go on forever.
$3 / 11=0.272 \cdot 7<$ Both the digits 2 and 7 repeat in this decimal.

## Task 13

Convert these fractions to decimals. Some fractions can be simpified first. Example: $8 / 10=4 / 5$

| 1. $1 / 5$ | 2. | $1 / 8$ | 3. | $3 / 10$ | 4. | $3 / 5$ | 5. | $7 / 8$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6. | $8 / 14$ | 7. | $6 / 100$ | 8. | $5 / 6$ | 9. | $4 / 8$ | 10. | $6 / 10$ |
| 11. | $7 / 12$ | 12. | $6 / 8$ | 13. | $4 / 12$ | 14. | $9 / 10$ | 15. | $6 / 12$ |
| 16. $6 / 24$ | 17. | $10 / 16$ | 18. | $8 / 18$ | 19. | $9 / 12$ | 20. | $7 / 15$ |  |
| 21. $9 / 27$ | 22. | $5 / 20$ | 23. | $7 / 28$ | 24. | $12 / 20$ | 25. | $5 / 25$ |  |

Investigate the patterns created when you convert these fractions ...
26.
$1 / 11,2 / 11,3 / 11,4 / 11,5 / 11,6 / 11,7 / 11,8 / 11,9 / 11$ and $10 / 11$ to decimals.
27.
$1 / 9,2 / 9,3 / 9,4 / 9,5 / 9,6 / 9,7 / 9$ and $8 / 9$ to decimals.
28.
$1 / 7,2 / 7,3 / 7,4 / 7,5 / 7$ and $6 / 7$ to decimals.

## Expressing a decimal as a fraction:

Decimals can be expressed as special fractions, with denominators of 10, 100, 1000 etc. Example: Convert 0.7, 0.42 and 0.127 to fractions.
Answers: One digit after the decimal point, therefore 10 is the denominator, $7 / 10$ Two digits after the decimal point, therefore 100 is the denominator, ${ }^{42} / 100$
Three digits after the decimal point, therefore 1000 is the denominator, ${ }^{127} / 1000$


## Task 14

Convert these decimals to fractions, then simplify if you can.

| 1. | 0.8 | 2. | 0.07 | 3. | 0.006 | 4. | 0.28 | 5. | 0.015 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6. | 0.36 | 7. | 0.4 | 8. | 0.85 | 9. | 0.56 | 10. | 0.2 |
| 11. | 0.275 | 12. | 0.0125 | 13. | 0.425 | 14. | 0.6 | 15. | 0.96 |
| 16. | 0.9 | 17. | 0.785 | 18. | 0.5 | 19. | 0.106 | 20. | 0.0004 |
| 21. | 0.87 | 22. | 0.09 | 23. | 0.903 | 24. | 0.72 | 25. | 0.825 |
| 26. 0.012 | 27. | 0.7 | 28. | 0.64 | 29. | 0.048 | 30. | 0.009 |  |



## Expressing a decimal as a percentage:

Fractions which are out of 100 are commonly known as percentages.
Example: 30 out of 100 could be written as the fraction ${ }^{30} / 100$ or as a percentage $30 \%$, which is read as " 30 per cent".
To convert a decimal to a percentage, multiply the decimal by 100. Example: $0.3 \times 100=30 \%, 0.09 \times 100=9 \%, 1.35 \times 100=135 \%$

## Task 15

Convert these decimals to percentages.


1. 0.26
2. 0.08
3. 0.012
4. 0.74
5. 0.4
6. 0.75
7. 0.267
8. 0.37
9. 0.085
10. 0.6
11. 0.036
12. 2.1
13. 3.45
14. 0.27
15. 0.029
16. 0.52
17. 0.87
18. 0.9
19. 0.7
20. 0.403
21. 0.02
22. 0.041
23. 0.083
24. 1.86
25. 0.69

## Expressing a percentage as a decimal:

Percentages are out of 100 and can be written as a fraction. To convert a fraction to a decimal we divide the numerator by the denominator. For all percentages written as fractions, the denominator is 100.
Therefore to convert a percentage to a decimal, divide the percentage by 100.
Example: Convert $60 \%$ to a decimal.
Answer: $\quad 60 \%$ is the same as $60 / 100$, therefore $60 \div 100=0.6$
To convert a percentage to a decimal, divide the percentage by 100.

## Task 16

Convert these percentages to decimals.

| 1. | $65 \%$ | 2. | $50 \%$ | 3. | $9 \%$ | 4. | $15 \%$ | 5. | $45 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6. | $87 \%$ | 7. | $55 \%$ | 8. | $100 \%$ | 9. | $17 \%$ | 10. | $5 \%$ |
| 11. | $52 \%$ | 12. | $40 \%$ | 13. | $93 \%$ | 14. | $80 \%$ | 15. | $23 \%$ |
| 16. | $75 \%$ | 17. | $66 \%$ | 18. | $30 \%$ | 19. | $37.5 \%$ | 20. | $80.5 \%$ |
| 21. | $1.8 \%$ | 22. | $140 \%$ | 23. | $0.6 \%$ | 24. | $137 \%$ | 25. | $306 \%$ |
| 26. | $0.9 \%$ | 27. | $3.95 \%$ | 28. | $96 \%$ | 29. | $54.8 \%$ | 30. | $84.9 \%$ |

## Converting between fractions, decimals and percentages:

## Task 17

Copy this table of commonly used fractions, decimals and percentages.
Complete the table by filling in the gaps using the fractions, decimals and percentages from the box at the right.

| Fraction | Decimal | Percentage |
| :---: | :---: | :---: |
| $1 / 4$ |  |  |
|  | 0.3 |  |
|  |  | $40 \%$ |
| $1 / 2$ |  |  |
|  |  | $66.6 \%$ |
|  | 0.75 |  |



## Finding a percentage of a quantity:

Finding a percentage of a quantity can be done several ways.
Example: Find $30 \%$ of $\$ 600$.


One way this could be done is by finding $10 \%$ of the quantity first, then multiply by 3 as $3 \times 10 \%=30 \%$. Example: $10 \%$ of $\$ 600$ is $\$ 60$, therefore $30 \%$ would be $\$ 60 \times 3=\$ 180$.

A second way would be to convert the percentage to a decimal, then multiply the quantity by the decimal.
Example: $30 \%=0.3$, therefore $\$ 600 \times 0.3=\$ 180$.
Which way do you think is easier? Can you think of other ways of finding the percentage of a quantity?

## Task 18

Calculate the following percentages of these whole numbers.

1. $50 \%$ of 60
2. $10 \%$ of 75
3. $10 \%$ of 48
4. $20 \%$ of 45
5. $40 \%$ of 110
6. $40 \%$ of 120
7. $60 \%$ of 56
8. $60 \%$ of 90
9. $70 \%$ of 96
10. $60 \%$ of 50
11. $25 \%$ of 144
12. $75 \%$ of 96
13. $75 \%$ of 60
14. $45 \%$ of 88
15. $60 \%$ of 54
16. $95 \%$ of 80
17. $15 \%$ of 50
18. $65 \%$ of 48 .
19. $120 \%$ of 90
20. $210 \%$ of 70


A new computer will cost $\$ 2350$ and can be purchased with a deposit.
25. Calculate the deposit if $15 \%$ is required.
26. How much is left to pay after the deposit has been paid?
27. If a deposit of $\$ 470$ was paid, what percentage of the total price is that?


During the past 120 days, the weather conditions were recorded.
28. On $30 \%$ of the days it was cloudy. Calculate the number of days it was cloudy.
29. On $45 \%$ of the days it was sunny. Calculate the number of sunny days.
30. If it rained on 12 days, what percentage of the total days is that?

During the holidays, Richard has been camping with his friends.
31. On the first day they spent $20 \%$ of the day fishing. Calculate the number of hours they spent fishing.
32. On the second day, they spent $40 \%$ of the day sailing. Calculate the number of hours they spent sailing.

33. If Richard spent 6 hours one day tramping, what percentage of a day is that?


A school cross country race is run over a distance of 7200 m .
34. If Rangi has completed $72 \%$ of the course, calculate how far he has run so far.
35. How far does Rangi have left to run? Convert your answer to a percentage of the total distance of the race.

A 54 m long fence around a swimming pool is to be painted.
36. If $55 \%$ of the fence has already been painted, calculate the length of the fence that has been painted.
37. How much of the fence is left to paint? Convert your answer to a percentage of the total length of the fence.


In the school library there are 840 books.

38. If $45 \%$ of the books are suitable for pupils 9 years old or younger, calculate how many books that is.
39. If $20 \%$ of the books are fiction, calculate how many books that is?
40. If 126 books are nature books, what percentage is this?
41. Create word problems involving finding percentages of a quantity.

Exchange your questions with a classmate and compare answers.



## Multiplying and dividing decimals:

When multiplying or dividing using decimals, setting out the question correctly is important, especially when a calculator is not being used.
Example: $2.38 \times 0.9$ could be rewritten as ... and

$$
3.65 \div 0.5 \text { could be rewritten as ... }
$$



The decimal point is moved to the right, the same number of places in both numbers, so that you are dividing by a whole number.
That is, 0.5 becomes 5 , and 3.65 becomes 36.5 .

## Task 19

Calculate the following, setting out the questions correctly to avoid mistakes. (Try to do this WITHOUT a calculator)

1. $2.953 \times 12$
2. $7.94 \div 0.2$
3. $136.64 \div 0.04$
4. $8.75 \times 3.6$
5. $96.84 \div 1.2$
6. $50.616 \div 0.9$
7. $5634 \times 0.008$
8. $3.951 \times 75$
9. $50.853 \div 0.011$
10. $7.605 \times 0.034$
11. $0.236 \times 0.08$
12. $723.87 \div 0.09$
13. $\quad 96.75 \times 1.2$
14. $435.65 \div 0.5$
15. $80.375 \div 0.05$
16. $153.4 \times 0.25$
17. $\quad 109.42 \times 2.5$
18. $88.56 \div 0.9$
19. $0.087 \times 32.8$
20. $\quad 3.444 \div 0.004$
21. $22.743 \div 0.07$
22. $0.946 \times 0.018$
23. $0.2168 \div 0.0004$
24. $26.851 \times 0.009$

A school is going to buy some new computers that will cos $\dagger \$ 2150.90$ each.
25. Calculate the cost of buying 4, 7 and 12 computers.


A school is charged 1.4 cents per copy, for photocopying A4 sized paper.

26. Convert 1.4 cents to dollars.
27. Calculate the cost of copying 800, 1200 and 2700 copies.

State your answers in dollars.
28. If the school paid $\$ 70, \$ 105$ and $\$ 156.80$ in photocopy charges, how many copies did they do each time?

A travelling salesman recorded the distances he travelled each day for a week, including the weekend.
29. If he travelled 1646.40 km during this week, calculate the average (mean)
distance he travelled each day of the week.
30. If he averaged 167.5 km each day for 15 days,
calculate the total distance he would travel during this time.
31. If he used 102.5 L of petrol, at a cost of $\$ 0.95 / \mathrm{L}$, calculate the total cost of petrol he used.
32. If petrol costs $\$ 0.95$ / L and an empty tank costs $\$ 47.50$ to fill, how much petrol does the tank hold?

A motor cycle race is being raced around a local street course that is 4.25 km per lap.

33. Calculate the total distance of a 25 lap, 60 lap and 120 lap race? Answer in kilometres.
The average time taken per lap is 85.75 seconds.
34. Calculate the time taken to complete a 75 lap race. Answer in seconds.
35. Convert the race time to minutes.
36. If a rider takes 1 hr 56 min 52.5 sec to complete a 75 lap race, calculate his average lap time. Give your answer in seconds.
37. Create word problems involving the multiplication and division of decimals.

Exchange your questions with a classmate and compare answers.


## Understanding negative numbers:

Examples: Last night there was a 5 degree frost.
A building has two car park levels beneath the ground floor.
A diver went 30 metres below the surface of the sea.
John's bank account is in overdraft by the sum of $\$ 200$.
In these examples, the numbers mentioned could be written as negative numbers.


Answers: $a^{-} 5^{\circ} \mathrm{C}$ frost, car park levels -1 and $-2,-30 \mathrm{~m}$ below the surface, and $-\$ 200$ bank balance.
Positive numbers are above zero and the positive sign does not have to be shown.
Negative numbers are below zero, and the small negative sign must be shown.

## Task 20

A new highrise office block has been built, with some additional levels below ground level.

1. How could you label the floors of this building if there were 10 floors above ground and 3 floors below? Let $G=$ ground floor.
2. Brian has an office on the 6th floor and drops 8 floors to get to his car. On which floor is his car?
3. Pauline parks her car 3 floors below the ground floor and takes the lift up 7 levels to her office. On which floor is her office?

| $?$ |
| :--- |
| $?$ |
| $?$ |
| $?$ |
| $?$ |
| $?$ |
| $?$ |
| $?$ |
| $?$ |
| $?$ |
| $\mathbf{G}$ |
| $?$ |
| $?$ |
| $?$ |



This diagram shows a sailing ship, a diver, some birds and some fish. The sea level is at zero on the scale drawn.
4. How high is the mast above the sea level?
5. How far below the surface is the boat's keel?
6. State the height of each bird above the sea level as positive numbers.
State the depth of the 4 fish below sea level as negative numbers.
8. State the depth of the diver below sea level as a negative number.

A bird is flying 8 metres above the sea,
then drops 11 metres straight down.

9. State the depth the bird reaches below the surface of the sea, as a negative number.

The temperature scale is one of the most commonly used scales that uses negative numbers, especially when recording maximum and minimum daily temperatures.
10. What is the temperature on this diagram of a thermometer?

Use the thermometer scale to calculate the new temperatures after the following changes ...
11. Starting temperature $9^{\circ} \mathrm{C}$, drops $5^{\circ} \mathrm{C}$
13. Starting temperature $6^{\circ} \mathrm{C}$, drops $9^{\circ} \mathrm{C}$
15. Starting temperature $-3^{\circ} \mathrm{C}$, rises $7^{\circ} \mathrm{C}$
17. Starting temperature $-2^{\circ} \mathrm{C}$, drops $6^{\circ} \mathrm{C}$
19. Starting temperature $5^{\circ} \mathrm{C}$, drops $10^{\circ} \mathrm{C}$
21. Starting temperature $-8.7^{\circ} \mathrm{C}$, rises $5.2^{\circ} \mathrm{C}$
23. Starting temperature $-7.2^{\circ} \mathrm{C}$, rises $5.9^{\circ} \mathrm{C}$
12. Starting temperature $4^{\circ} \mathrm{C}$, rises $4^{\circ} \mathrm{C}$
14. Starting temperature $4^{\circ} \mathrm{C}$, drops $11^{\circ} \mathrm{C}$
16. Starting temperature $0^{\circ} \mathrm{C}$, drops $7^{\circ} \mathrm{C}$
18. Starting temperature $-5^{\circ} \mathrm{C}$, rises $9^{\circ} \mathrm{C}$
20. Starting temperature $-3^{\circ} \mathrm{C}$, drops $6^{\circ} \mathrm{C}$
22. Starting temperature $-4.3^{\circ} \mathrm{C}$, rises $8.7^{\circ} \mathrm{C}$
24. Starting temperature $-1.2^{\circ} \mathrm{C}$, rises $3.3^{\circ} \mathrm{C}$


## Understanding and using number lines:

Positive and negative numbers can be represented on a number line. A number line goes on forever, in both directions. Example:


A number line can be used to add positive and negative numbers together.


The first number of the question is the starting point on the number line.

When you add 12 on a number line, which direction do you move?
When you add ${ }^{-9}$ on a number line, which direction do you move?

Answer: Move 12 to the right.
Answer: Move 9 to the left.

## Task 21

Use the number lines below to add these positive and negative numbers together.
The first number for each problem has been marked with a dot on the number line.


Add or subtract these positive and negative numbers, using the number line above, if required.

| 7. | $-6+10$ | 8. | $5+-8$ | 9. | $-9+10$ | 10. | $7+-5$ | 11. | $-10+9$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 12. | $8+-11$ | 13. | $-11+8$ | 14. | $10+-13$ | 15. | $-9+15$ | 16. | $10+-14$ |
| 17. | $-8+17$ | 18. | $12+-19$ | 19. | $-13+20$ | 20. | $10+-16$ | 21. | $-12+15$ |
| 22. | $10+-19$ | 23. | $8+-19$ | 24. | $7+-18$ | 25. | $11+-19$ | 26. | $-9+17$ |
| 27. | $-8+18$ | 28. | $-15+9$ | 29. | $17+-9$ | 30. | $-5+4$ | 31. | $-7+6$ |
| 32. | $-7+17$ | 33. | $12+-17$ | 34. | $-9+21$ | 35. | $-19+15$ | 36. | $11+-17$ |
| 37. $19+-17$ | 38. | $-7+17$ | 39. | $-7+-4$ | 40. | $-8+-11$ | 41. | $-9+-13$ |  |
| 42. | $-15+-9$ | 43. | $-8--13$ | 44. | $-7--18$ | 45. | $-13--9$ | 46. | $-14--8$ |

## Task 22

Using a die (dice), play this game in small groups.
The odd numbers are negative, that is, $-1,-3 \&-5$. The even numbers are positive, that is, $2,4 \& 6$.
Roll the die 5 times, recording the numbers that appear, then add up the numbers.
Example: $4+-5+-3+2+-1=-3$.
Continue until each pupil has had 5 turns, then total your scores.
The winner is the pupil with the lowest combined score.


## More negative numbers:

Sally drew two differently coloured circles to represent positive and negative numbers.

Example: What numbers do these two groups of circles represent?
= positive $1=1$

Answer: 5 and -6
(Note: The positive sign is left off the 5)

If one positive circle and one negative circle cancel each other, what number do all the circles above represent?

Answer: $5+-6=-1$

## Task 23



Count the positive $\geqslant$ and Dnegative circles in each group below and write a simple mathematical sentence for each. Remember one positive circle cancels one negative circle. Example: $4+-9=-5$.
1.

2. $\geqslant \otimes(1) \geqslant$ $11 \geqslant \geqslant 3$ (1) $\otimes \geqslant \mathbb{1} \geqslant$

(1) (1) (1) (1)
3. $\geqslant \geqslant(1) \geqslant(1)$

(1) $\geqslant \otimes \mathbb{D} \geqslant$
(1) $\mathbb{1} \geqslant \mathbb{1} \mathbb{1} \otimes \mathbb{1}$
4.


Work out these questions involving adding positive and negative numbers.

| 5. | $-8+9$ | 6. | $11+-14$ | 7. | $-12+11$ | 8. | $23+-17$ | 9. | $-11+14$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 10. | $22+-19$ | 11. | $-24+17$ | 12. | $45+-29$ | 13. | $-38+53$ | 14. | $19+-19$ |
| 15. | $-27+18$ | 16. | $46+-37$ | 17. | $-51+37$ | 18. | $38+-49$ | 19. | $-24+27$ |
| 20. | $-41+-36$ | 21. | $-15--27$ | 22. | $31--17$ | 23. | $36--40$ | 24. | $-25--49$ |
| 25. | $-8.9+7.6$ | 26. | $11.6+-9.8$ | 27. | $15.6+-21.4$ | 28. | $-17.4+-25.8$ | 29. | $11.9+-27.3$ |
| 30. | $-42.3+-17.6$ | 31. | $-28.5+36.4$ | 32. | $17.3--41.6$ | 33. | $-54.4--35.9$ | 34. | $-37.1--41.9$ |

## Bank overdrafts:

When you spend more money than you have in your bank account, your bank account is said to be in overdraft.
The balance of your account could be written as a negative number.
Banks allow you to go into overdraft, so they can charge you interest on the negative balance.
Example: - $\$ 200$ means the account is $\$ 200$ in overdraft.


If Mr Keys has $\$ 150$ in the bank and withdraws $\$ 200$, what will his bank balance be? Answer: $-\$ 50$ ( $\$ 50$ in overdraft)

## Task 24

When money is deposited into an account or withdrawn from an account, it is called a transaction.
Copy this table below, then calculate the new balance of this bank account after each transaction.
1.

| Date | Withdrawals | Deposits | Balance |  |  |  |
| :---: | :--- | ---: | ---: | ---: | ---: | ---: |
| $1 / 3$ | Opening balance |  |  |  |  |  |
| $3 / 3$ | Purchased stereo | $\$ 185$ | 00 |  |  |  |
| $5 / 3$ | Wages from part-time job |  |  | $\$ 54$ | 60 |  |
| $8 / 3$ | Bought 9 C.D.'s | $\$ 69$ | 65 |  |  |  |
| $12 / 3$ | Wages from part-time job |  |  | $\$ 85$ | 80 |  |
| $15 / 3$ | Sold bike |  |  | $\$ 50$ | 00 |  |
| $18 / 3$ | Night out at movies | $\$ 25$ | 75 |  |  |  |
| $19 / 3$ | Wages from part-time job |  |  | $\$ 70$ | 20 |  |
| $21 / 3$ | Bought new bike | $\$ 199$ | 95 |  |  |  |


2. Create your own bank balance questions and exchange with a classmate.


## Expressing a quantity as a fraction or as a percentage of a whole:

Seven pupils in a class of 28 like playing rugby.
Ten out of 50 pupils were away from school today.
On 17 of the last 31 days it has rained.
In all of these statements there is information that can be expressed or written as a fraction or a percentage.
Examples: $6 / 24$ or $1 / 4$ or $25 \%$ of the pupils like playing hockey,
$4 / 20$ or $1 / 5$ or $20 \%$ of the pupils were away from school today,
On $10 / 20$ or $1 / 2$ or $50 \%$ of the last 20 days it has been raining.
Discuss events that could be expressed as fractions or percentages.


## Task 25

Express the shaded diagrams as a fraction and as a percentage of each group of diagrams.
1.

2.

3.

4.


Write the information in each question as a fraction and then convert your answers to percentages.
5. Joanne scored 65 out of 100 in a maths test.
7. Of 50 pets, 19 were cats.
9. 9 out of 25 pupils were away from school.
6. 35 pupils in a school of 100 are in Room 7.
8. It has rained during 17 days out of 20 days.
10. 3 out of 5 people watch the rugby test.

Mr Proctor's car has a 40L petrol tank. He goes on a long trip and then refills the tank.
11. If the refilling of the petrol tank takes 18L, what fraction of a full tank was used during the trip? Convert your answer to a percentage.
12. If the petrol costs $\$ 0.975 / \mathrm{L}$, how much did it cost to fill the tank?


A school cross country race is 5 laps around the school grounds.
13. If Karen has completed 3 laps, what fraction of the race has she completed so far? Convert your answer to a percentage.
14. What percentage of the race does she have left to run?

Convert your answer to a fraction.
15. If Scott takes about 3 min 20 sec for each lap, how long will he take to complete the race?

A brick fence is being constructed using 240 bricks.
16. If 150 bricks have been used so, what fraction of the fence has been completed? Convert your answer to a percentage.
17. If each brick costs $\$ 0.45$, how much will the bricks cos $\dagger$ to build this fence?


At a one day cricket match, 21000 tickets have been presold.
18. If there are 6500 seats still unsold, what is the largest possible crowd that could attend?
19. What fraction of the seats were presold? Convert your answer to a percentage.
20. What fraction of the seats are yet to be sold? Convert your answer to a percentage.
21. If the crowd attendance ended up being 25300, what percentage of a full stadium turned up to watch the game?
22. Create word problems involving fraction and percentage calculations.

Exchange your questions with a classmate and compare answers.



## Increasing and decreasing by a given percentage:

To increase or decrease by a given percentage, find the actual increase or decrease, then add or subtract..

Examples: Increase $\$ 40$ by $10 \%$.
Decrease $\$ 50$ by 20\%

Answer: $10 \%$ of $\$ 40=\$ 4, \$ 40+\$ 4=\$ 44$
Answer: $20 \%$ of $\$ 50=\$ 10, \$ 50-\$ 10=\$ 40$


## Task 26

Increase or decrease the following numbers as indicated.

1. increase 30 by $10 \%$ decrease 60 by $10 \%$
2. decrease 84 by $25 \%$
3. increase 120 by $15 \%$
4. decrease 20 by $35 \%$
5. increase 340 by $5 \%$
6. decrease 85 by $7.5 \%$
7. decrease 60 by $10 \%$
8. increase 108 by $25 \%$
9. decrease 90 by $15 \%$
10. increase 150 by $8 \%$
11. decrease 175 by $60 \%$
12. increase 27 by $12.5 \%$
13. decrease 80 by $20 \%$
14. decrease 60 by $40 \%$
15. increase 240 by $30 \%$
16. decrease 95 by $20 \%$
17. increase 265 by $45 \%$
18. decrease 164 by $9.5 \%$
19. increase 65 by $20 \%$
20. increase 48 by $50 \%$
21. decrease 110 by $5 \%$
22. increase 124 by $40 \%$
23. decrease 180 by $75 \%$
24. increase 475 by $2.5 \%$

A new computer will cost $\$ 2750$ and can be purchased with a deposit.
25. Calculate the deposit if $10 \%$ is required.
26. How much is left to pay after the deposit has been paid?


Car prices increased 5\% during the month of February. Calculate the new prices for the car prices listed below.
27. $\$ 19500, \$ 21950, \$ 25300, \$ 27900$ and $\$ 32450$.

The Goods and Services $\operatorname{Tax}$ (GST) is $12.5 \%$. Calculate the selling price for these items after GST has been added.

28. $\$ 350$

29. $\$ 88.80$

30. $\$ 177.73$

31. $\$ 2620$


A clothing shop is having a sale, with discounted prices. Calculate the new prices after the $\mathbf{2 0 \%}$ discount has been taken
off.
33.

Normal price: \$19.90
34.
 \$35.60
35.
 $\$ 47.90$
36.

Normal price: \$8.90
37.

Normal price: \$14.75

A retail shop purchases products at wholesale prices. The retail price is worked out by adding $40 \%$ to the wholesale price, then GST (12.5\%) is added to this price. Calculate the retail price of each item.
38.


Wholesale price: \$1200.00
39.

Wholesale price: $\$ 42.00$

Wholesale price: $\$ 230.00$

Wholesale price: $\$ 175.00$
42.

Wholesale price: $\$ 670.00$
43. Create word problems involving increasing or decreasing numbers by a given percentages. Exchange your questions with a classmate and compare answers.


## Writing and simplifying ratios:

Using a ratio is one way of describing how often something has happened.
Example: Three out of four pupils in Year 9 like going to the movies.
This statement can be written as a ratio of $3: 4$.
Write these statements as ratios.
3 out of 8 pupils play hockey in Room 7.
What is the ratio of girls to boys in Room 10 if there are 15 girls and 12 boys?
Jan and Stu shared some lollies in a ratio of two to three.


Answers: $3: 8,15: 12,2: 3$
A ratio can be simplified if all numbers of a ratio can be divided by the same number.
Example: $60: 50=6: 5$ (divide by 10), $18: 6: 12=3: 1: 2$ (divide by 6 )
Simplify these ratios. $25: 45, \quad 27: 36, \quad 24: 48: 36$
Answers: 5:9, $3: 4, \quad 2: 4: 3$

## Task 27

Write the information in each statement as a ratio, then simplify the ratio if possible.

1. On five out of seven days last week it was raining.
2. 40 out of 60 people watch TV 1 news each night.
3. At a concert there were 78 adults to 14 children.
4. In a class there were 15 boys and 18 girls.
5. 85 out of 600 pupils started school this year.
6. Jodie banked $\$ 5.00$ of every $\$ 20.00$ she earned.
7. On camp there are 3 teachers and 27 pupils.
8. 45 out of 90 households have a pet cat.
9. On 6 of the past 30 days it was very hot.
10. There were 32 children and 4 adults at a party.

Simplify these ratios.

| 11. | $5: 25$ | 12. | $20: 10$ | 13. | $21: 35$ | 14. | $18: 40$ | 15. | $36: 44$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 16. | $28: 7$ | 17. | $63: 45$ | 18. | $32: 56$ | 19. | $45: 25$ | 20. | $28: 63$ |
| 21. | $36: 48$ | 22. | $72: 24$ | 23. | $33: 88$ | 24. | $96: 36$ | 25. | $49: 84$ |
| 26. $9: 27: 18$ | 27. | $84: 36: 108$ | 28. | $26: 52: 13$ | 29. | $144: 60: 24$ | 30. | $240: 320: 640$ |  |

## Writing ratios as fractions:

Example: The ratio 4:5 can be written as the fraction $4 / 5$. The ratio $8: 3$ can be be written as the fraction $8 / 3=2 \frac{2}{3}$.
Write these statements as ratios and then as a fraction.
5 out of 8 pupils play soccer in Room 12
What is the ratio of girls to boys in Year 9 if there are 80 girls and 65 boys? Rhonda and Keith shared some pizza in a ration of 3 to 4 .

Answers: $\quad 5: 8=5 / 8,80: 65=80 / 65,3: 4=3 / 4$
Some ratios written as fractions can also be simplified to create the simplest equivalent fraction Example: 70 : $90=70 / 90=7 / 9$


## Task 28

Write these ratios as fractions and then simplify each fraction if possible.

| 1. | $14: 28$ | 2. | $15: 30$ | 3. | $24: 36$ | 4. | $15: 40$ | 5. | $33: 77$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6. | $12: 32$ | 7. | $21: 42$ | 8. | $27: 63$ | 9. | $45: 60$ | 10. | $30: 120$ |
| 11. | $50: 72$ | 12. | $84: 72$ | 13. | $56: 88$ | 14. | $108: 81$ | 15. | $49: 84$ |
| 16. | $120: 65$ | 17. | $150: 25$ | 18. | $26: 39$ | 19. | $72: 160$ | 20. | $96: 108$ |



## Sharing quantities by a given ratio:

| Example: A pizza is cut into 10 pieces and shared in a ratio of $2: 3$ between Auriol and Katie. |  |  |
| :--- | :--- | :--- |
|  | How many pieces of pizza does each friend eat? |  |
| Answer: | Add the ratio numbers | $2+3=5$ |
|  | Divide the quantity being shared by this answer. <br>  <br>  <br> Multiply each ratio number by this answer. | $10 \div 5=2$ |
|  | $2 \times 2=4$ and $3 \times 2=6$ |  |



Therefore, Auriol had 4 pieces of pizza and Katie had 6 pieces of pizza.
Discuss other ways of sharing a quantity by a given ratio.

## Task 29

What is the total number of parts if something is divided in the given ratios?

1. $2: 7$
2. $3: 4$
3. $5: 3$
4. $9: 5$
5. $11: 4$
6. $6: 13$
7. $6: 1$
8. $7: 8$
9. $11: 9$
10. $2: 9$
11. $13: 6$
12. $5: 18$
13. $13: 8$

Share these quantities by the given ratios.
16. Share $\$ 50$ in a ratio of $1: 4$
19. Divide 63 kg in a ratio of $3: 4$
17. Divide 27 mm in a ratio of $1: 2$.
18.
20. Share $\$ 84$ in a ratio of $2: 5$.
21. Divide 108 kg in a ratio of $7: 2$.
22. Share $\$ 117$ in a ratio of $4: 5$
23. Divide 96 mg in a ratio of $1: 11 . \quad 24$.

Share $\$ 88$ in a ratio of $3: 5$.
25. Divide 64 kL in a ratio of $5: 3$
26. Share $\$ 72$ in a ratio of $2: 7$.
27. Divide 56L in a ratio of $7: 1$.
28. Divide $\$ 143$ in a ratio of $11: 2$
29. Share 200 cm in a ratio of $3: 2$.
30.

Share $\$ 270$ in a ratio of $1: 2$.
31. 200 tickets were sold for a concert. If the ratio of tickets sold to adults to that of children was $4: 1$, how many children went to the concert?

32. Jenny and John paid for a new car in the ratio of $2: 3$. If the car cost $\$ 15000$, how much did Jenny pay towards the car?
33. Two charities raised $\$ 12500$ for a combined garage sale. If the money is to be divided in a ratio of $3: 5$, how much does each charity receive?

34. At a local rugby game between a Linwood and a St Albans club, Linwood supporters were out numbered in a ratio of $4: 3$. If 5964 people attended the game, how many were Linwood supporters?
35. For every dollar that Michael earns, he saves 20 cents. Write this information as a ratio in its simplest form.
36. If Michael earns $\$ 500$ a week, how much does he save?
37. If Michael saves at the same rate for 10 weeks, how much will he have saved?
38. How long would it take for Michael to save $\$ 2700$ ?

39. Karen is making 3 jackets of different sizes from a 3.6 m length of material If the material is to be divided up using a ratio of $1: 3: 2$, how much material is needed for each jacket?
40. A juice factory produces 2700 litres of juice per day in a ratio of 3 orange : 2 apple : 4 black currant. Calculate the number of litres of each flavour produced per day.
41. Create word problems involving sharing in a givien ratio. Exchange your questions with a classmate and compare answers.



## Creating equivalent fractions and simplifying fractions:

In all of these diagrams below, half of the diagram is shaded.


How many squares in each diagram are shaded?
Answers: $1 / 2,2 / 4,3 / 6,4 / 8,5 / 10,6 / 12$
All of these fractions are called equivalent fractions.
Equivalent fractions can be created by multiplying or dividing the top and bottom numbers of a fraction by the same number.
Example: $1 / 2 \times 8 / 8=8 / 16$
$15 / 20 \div 5 / 5=3 / 4$
When simplifying fractions, the aim is to find the simplest equivalent fraction by dividing the fraction until you have the smallest possible numbers, top and bottom.


## Task 30

Copy each diagram then shade in the fraction given for each.
1.

2. $\frac{3}{4}$

$\square$ 3. $\frac{4}{5}$
 4. $\frac{2}{7}$

5. $\begin{array}{rr}\frac{5}{8} & \square \square \square \square \\ & \square \square \square \square\end{array}$

What fraction of each digram is shaded? Simplify your answers if possible.
6.

7. $\square$ 园 $\square$ 国

8.

9.

10.


Find the missing numbers to complete these equivalent fractions.

| 11. | $1 / 2=4 / 14$ | 9 = ? | 12. | $1 / 2=4 / 50$ | \& = ? | 13. | $1 / 4=4 / 20$ |  | 14. | $1 / 4=4 / 60$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15. | $1 / 3=\boldsymbol{T} / 24$ | $\nabla=$ ? | 16. | $1 / 3=1 / 36$ | $\checkmark=$ ? | 17. | $3 / 4=\Upsilon / 24$ | $\nabla=$ ? | 18. | $3 / 4=9 / 40$ |
| 19. | $2 / 3=1 / 36$ | - = | 20. | $2 / 5=1 / 60$ | $\bullet=$ ? | 21. | $4 / 5=160$ | - = | 22. | $1 / 6=1 / 60$ |
| 23. | $5 / 6=4 / 66$ | A = ? | 24. | $7 / 8=9 / 64$ | $\uparrow=$ ? | 25. | $3 / 8=9 / 96$ | ¢ = ? | 26. | $3 / 11=4 / 88$ |
| 27. | $4 / 9=4 / 54$ | \% = ? | 28. | $3 / 11=4 / 99$ | * = ? | 29. | $7 / 12=4 / 84$ | 4 = ? | 30. | $8 / 13=4 / 65$ |

Find the simplest equivalent fraction for these fractions.

| 31. | $9 / 12$ | 32. | $10 / 15$ | 33. | $13 / 26$ | 34. | $12 / 36$ | 35. | $9 / 36$ | 36. | $30 / 45$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 37. | $8 / 48$ | 38. | $14 / 35$ | 39. | $27 / 36$ | 40. | $32 / 40$ | 41. | $24 / 60$ | 42. | $35 / 42$ |
| 43. | $22 / 110$ | 44. | $25 / 150$ | 45. | $40 / 240$ | 46. | $35 / 165$ | 47. | $42 / 210$ | 48. | $36 / 192$ |

Write the information in each question as a fraction, then simplify if possible.
49. Sally scored 65 out of 100 in a maths test.
51. 120 out of 200 people have a pet dog.
53. On 8 of the past 14 days it rained.
55. 24 out of 144 pupils were away from school today.
57. 122 pupils out of 156 enjoy swimming.
59. 220 cm of a 540 cm length of wood has been used up.
61. Jodie scored 44 out of 50 in an assignment.
63. 84 out of 124 cars had a driver only in them.
50. On 20 days in April it was sunny.
52. Of the 146 Year 9 pupils, 70 were girls.
54. 134 out of 152 pupils were wearing sweatshirts.
56. The 'All Blacks' won 14 out of the last 20 games.
58. Out of a class of 32,28 passed the last test.
60. 4 of the 100 desks have been damaged by pupils.
62. 23 of the 80 pages in a book had diagrams on them.
64. In a survey of 120 houses, 18 had open fires.


## Improper fractions and mixed numbers:

What is different about these fraction?
$5 / 2,7 / 3,9 / 7,13 / 8,27 / 5,{ }^{41} / 6,57 / 9$, etc.
Answer: The top number or numerator is larger than the bottom number or denominator.
This type of fraction is called an improper fraction.
An improper fraction can be converted to a mixed number by dividing the numerator by the denominator and recording the remainder as a fraction.


Example: ${ }^{25} / 7=34 / 7 \quad(24 \div 7=3+4$ remainder $)$
A mixed number can be converted to an improper fraction by multiplying the whole number by the denominator and adding on the numerator.

Example: $5 \frac{2}{3}={ }^{17} / 3 \quad(5 \times 3=15$ plus $2=17)$

## Task 31

Convert these improper fractions to mixed numbers, simplifying if possible.

1. $19 / 5$
2. $27 / 4$
3. $33 / 5$
4. $57 / 6$
5. $92 / 9$
6. $58 / 12$
7. $\quad 78 / 9$
8. $103 / 7$
9. $69 / 7$
10. $71 / 8$
11. $\quad 81 / 11$
12. $123 / 10$

Convert these mixed numbers to improper fractions.
13. $4^{3 / 5}$
14. $8 \frac{1}{2}$
15. $73 / 4$
16. $9^{2 / 3}$
17. $95 / 6$
18. $8 \frac{2}{5}$
19. $7 \frac{1}{6}$
20. $94 / 5$
21. $11 \frac{5}{8}$
22. $10 \frac{4}{9}$
23. $12^{7 / 9}$
24. $5 \frac{5}{12}$

## Adding and subtracting fractions:

To add or subtract fractions the denominators must be the same. This can be done by finding equivalent fractions. Example: $1 / 2+2 / 3=3 / 6+4 / 6=7 / 6=1 \frac{1}{6}$

If the answer is an improper fraction, it can be converted to a mixed number, as above.
When subtracting, if may be necesary to convert a mixed number to an improper fraction before subtracting.
Example: $21 / 4-1^{3} / 4=9 / 4-7 / 4=2 / 4=1 / 2$

## Task 32

Add and subtract these fractions, simplify your answers if possible.

1. $3 / 4+3 / 4$
2. $1 / 3+2 / 3$
3. $2 / 5+3 / 5$
4. $\quad 9 / 11+8 / 11$.
5. $\quad 4 / 7+5 / 7$
6. $4 / 5-1 / 5$
7. $7 / 8-3 / 8$
8. $8 / 9-5 / 9$
9. $11 / 12-7 / 12$
10. $9 / 11-5 / 11$
11. $3 / 4+2 / 3$
12. $2 / 3+1 / 5$
13. $3 / 4+3 / 5$
14. $4 / 5+1 / 3$
15. $43 / 5+3^{2} / 3$
16. $4 / 5-2 / 3$
17. $5 / 8-2 / 5$
18. $7 / 8-5 / 7$
19. $51 / 5-3^{3} / 5$
20. $71 / 5-3^{2} / 3$
21. If $3 / 8$ of a pizza has been eaten, how much is left to eat?
22. Two pizzas are bought. If $7 / 8$ of the first pizza is eaten, how much is left?
23. David eats $1 / 4$ of a pizza and Abby eats $1 / 5$ of the pizza. What fraction of the pizza has been eaten?
24. Paul has a piece of wood $5 \frac{1}{4}$ metres long. If he cuts $2^{3} / 4$ metres off one end, how long is the piece of wood that is left?
25. Two pieces of wood measured $3^{2} / 5$ metres and $4 / 3$ metres long. What is the combined length of these two lengths of wood?
26. Create word problems involving adding and subtracting fractions. Exchange your questions with a classmate and compare answers.


# 'In-class' Worksheet <br> Teaching Notes \& Answers 

How to use this section:
Teaching notes are enclosed in a box with a 'push-pin' at the top left corner. The teaching notes precede the answers for each worksheet / task. The teaching notes have been included to provide assistance and background information about each topic or unit of work.

## Introduction:

The topic of Number is concerned with exploring number, gaining an understanding of the meaning of negative numbers and special numbers such as prime numbers, factors, multiples, squares, square roots and other powers. The ability to convert between fractions, decimals and percentages is explored, plus activities involving the finding of fractions and percentages of a quantity. Being able to estimate quickly and accurately and checking the reasonableness of the answer is a useful skill that is explored. The setting out, and successful completion of addition, subtraction and multiplication problems involving decimals is also investigated, leading into the conventions for the order of operations.
The importance of gaining a good understanding of the 'basic number facts', the ability to add, subtract, divide and multiply with confidence, should not be underestimated, as all strands of mathematics involve some, if not all, of the four basic skills.

Adding and subtracting whole numbers: Multiplying and dividing whole numbers:
Special numbers:
In Tasks 1 \& 2, pupils are to copy two number crosses, then complete some addition or subtraction and multiplication or division problems as a revision activity. The copying of the number crosses is also an important skill.
In Task 3, pupils are to create his / her own addition / subtraction and multiplication / division number crosses to exchange with a classmates.

In Tasks 4 \& 5, pupils are to complete sentences about definitions of the special numbers; factors, multiples, prime numbers and prime factors. Pupils are then to work with each group to consolidate their understanding of the properties of these numbers.

## Task 1

1. \& 2 .


## Task 2

1. \& 2.


## Task 4



## Task 5

## 1. $55 \quad$ 2. $52 \quad 3.15$

## Order of operations:

## Word problems involving order of operations:

In Task 6, pupils are to use the order of operation convention to calculate answers. The letters
BODMAS or BEDMAS are a good way to remember the order of doing the calculation. At this level,
problems involving exponent (powers) have been left out.
The order implies the following ...

1. Look for brackets. If brackets are there, work out what is inside the brackets first.

Example: 21 + (4 + $3 \times 6$ )
2. Look for multiplication and division next and work out each one out, as you read from left to right. Both are of equal importance. The order in which they are written in BODMAS or BEDMAS DOES NOT imply that dividing should be done before multiplying. At this point, only adding and / or subtracting will be left.
3. Look for addition and subtraction next and work these out in the order they appear as you read from left to right. Both are of equal importance. The order in which they are written in BODMAS or BEDMAS DOES NOT imply that adding should be done before subtracting.
The final part of the task has questions where the operation signs have been left out and pupils are to work out the missing signs, using the convention of order of operations.
In Task 6, pupils are to utilise the order of operation rules to solve word problems.

## Task 6

| 1.95 | 2.37 | 3.97 | 4.20 | 5.4 | 6.87 | 7.28 | 8.19 | 9.17 | 10.34 | 11.66 | 12.33 | 13.40 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 14. 71 | 15.34 | 16.18 | 17.49 | 18.37 | 19.55 | 20.130 | 21.55 | 22.19 | 23.103 | 24.49 | 25.8 |  |
| 26. 24 | 27.133 | 28.7 | 29. 35 | 30.83 | 31.35 | 32.11 | 33.49 | 34.58 | 35.32 | 36.33 | 37.33 |  |
| 38. 47 | 39.10 | 40.50 | 41.75 | 42.85 | 43.30 | 44.65 | 45.24 | 46.287 | 47.64 | 48.144 |  |  |
| 49. 68 | 50.54 | 51.150 | 52.200 | 53.16 | 54.75 | 55.21 | 56.10 | 57.23 | 58.16 | 59.18 |  |  |
| 60.40 | $61.2+3 \times 5=17$ | $62.5 \times 3+6=21$ | $63.10-4+2=8$ | $64.12 \div 3 \times 7=28$ | 65. | $9+10 \div 2=14$ |  |  |  |  |  |  |

66. $23-4 \times 5=3 \quad 67.18 \div 6+9=12 \quad 68.8 \times 3+7=31 \quad 69.21-18 \div 3=15 \quad 70.27 \div 9+7=10$
67. $7+4 \times 6=31 \quad$ 72. $19-36 \div 12=16$
68. $\$ 66.50$
69. \$91
70. $\$ 80.50$
71. $\$ 161$
72. $\$ 157.50$
73. $\$ 147$
74. $\$ 168$
75. $\$ 175$
76. $\$ 259$
77. 5 C.D.'s 11. $\$ 28.50$ 12. $\$ 23$ 13. List A $-\$ 28.25$, List $B-\$ 27.20$, List $C-\$ 30.40$, List D - $\$ 49.70$,
List E - $\$ 54.15$, List $F-\$ 36.75$, List G $-\$ 50.93$, List H - $\$ 52.40$

## Worksheets 586

## Multiplying and dividing by powers of 10: <br> Converting between standard form and decimal form:

In Task 8, pupils are to multiply and divide by powers of 10. The aim is for pupils to come up with simple rules that involve moving the decimal point left or right, a number of spaces based on the number of zeros in the power of 10, therefore the actual calculation does not need to be done. Remind pupils where the decimal points are, if they are not shown. This task introduces the concept of standard form. Example: $1.2 \times 10^{4}, 3.93 \times 10^{-2}$ Word problems are included.
In Task 9, pupils are to convert between numbers written in standard form and as decimals. The aim is for pupils to be able to do this by moving the decimal point the required number of places to the right or left depending on whether it is a postive or negative power of 10. Remember that dividing by a postive power of 10 is the same as multiplying by a negative power of 10 . Example: $2.3 \div 10^{5}=2.3 \times 10^{-5}$

## Task 8

1. 69 2. 23000
2. 8400
3. 600
4. 230
5. 4090
6. 94300
7. 80500
8. 963000
9. 8 $\begin{array}{lllllll}\text { 11. } 384000 & 12.5 .9 & 13.370000 & 14.67000 & \text { 15. } 43000000 & 16.520000 & \text { 17. To multiply by } 10 \text { move }\end{array}$ decimal point 1 place to the right, to multiply by 100 move decimal point 2 places to the right and so on. 18.0 .096
$\begin{array}{lllllllll}\text { 19. } 0.0013 & \text { 20. } 0.00063 & \text { 21. } 0.934 & \text { 22. } 0.41 & 23.0 .0437 & 24.6 .728 & 25.0 .001863 & 26.0 .952\end{array}$ $\begin{array}{lllllll}\text { 27. } 0.0000085 & 28.0 .00409 & 29.0 .0096 & 30.0 .000076 & 31.0 .0069 & 32.0 .0000063 & 33.0 .0025\end{array}$
10. To divide by 10 move decimal point 1 place to the left, to divide by 100 move decimal point 2 places to the left and so $\begin{array}{lllllll}\text { on. } 35.25900 & 36.0 .00437 & 37.7210000 & 38.0 .006074 & 39.0 .0000907 & 40.73610000\end{array}$ 41. 0.0000542 42. 4021000 43. 3600 seats 44.12 .75 rows $45 . \$ 18.00 \quad$ 46. $\$ 0.54 \quad 47 . \$ 19000$ 48. $\$ 0.23$ 49. $\$ 125000$ 50. $\$ 1.65$ 51. $\$ 12330$ or 1233000 cents $\quad$ 52. $\$ 0.1275$ or 12.75 cents

## Task 9

$\begin{array}{lll}\text { 1. } 900 & \text { 2. } 0.06 & 3.53000\end{array}$
4. 0.0066
5. 0.0027 6. 930000
7. 0.0019
8. 240000
9. 3240
10. 0.000193 11. 347000
12. 0.00912
13. 0.00000763 14. 534000
15. 0.000904
16. 735000
17. 0.00094
18. 0.00306
19. 1260000 20. 0.000393
21. 310100
22. 0.000632
23. 0.00004106
$\begin{array}{lllllll}\text { 24. } 631800 & 25.2 .5 \times 10^{3} & \text { 26. } 4.2 \times 10^{-2} & 27.4 .25 \times 10^{4} & 28.5 .6 \times 10^{-3} & 29.5 .84 \times 10^{5} & 30.2 .351 \times 10^{3}\end{array}$
31. $3.4 \times 10^{-4} \quad 32.6 .315 \times 10^{7} \quad 33.5 .862 \times 10^{2} \quad 34.2 .5410^{-5} \quad 35.9 .5663 \times 10^{2} \quad 36.3 .9 \times 10^{-5}$
$\begin{array}{llllll}\text { 37. } 4.5 \times 10^{-6} & 38.8 .562 \times 10^{7} & \text { 39. } 4.126 \times 10^{-3} & 40\end{array} 9.63545 \times 10^{3} \quad 41.9 .523 \times 10^{8} \quad 42.2 .105 \times 10^{-5}$
43. $9.31 \times 10^{-6} \quad 44.3 .792068 \times 10^{4} \quad 45.3 .625 \times 10^{-5} \quad 46.3 .00495 \times 10^{7} \quad 47.1 .204504 \times 10^{8} \quad 48.6 .9 \times 10^{-9}$
49. 86400 sec in 1 day $=8.64 \times 10^{4}, 604800 \mathrm{sec}$ in 1 week $=6.048 \times 10^{5}, 31449600 \mathrm{sec}$ in 1 year $=3.14496 \times 10^{7}$
50. $350000 \mathrm{~km} \quad 51.5100 \mathrm{~km}$ in 1 day $=5.1 \times 10^{3} \mathrm{~km}, 35700 \mathrm{~km}$ in 1 week $=3.57 \times 10^{4} \mathrm{~km}, 1856400 \mathrm{~km}$ in 1 year $=$ $1.8564 \times 10^{6} \mathrm{~km} \quad 52.1440$ containers $\quad$ 53. 28800 litres $=2.88 \times 10^{4}$ litres 54.130 litres per hour 55. 46300 cards each day 56. 65000 letters $=6.5 \times 10^{4}$

Approximations, estimations and rounding using decimal places:

## Worksheets 7 \& 8

## Approximations, estimations and rounding using significant figures:

In Task 10, pupils are to round numbers to various decimal places as requested. Note that when rounding, 5's round up. Example: 2.15 rounds to 2.21 d.p., 9.235 rounds to 9.242 d.p. etc. All counting begins at the decimal point. Pupils are to calculate totals and round to the decimal place requested. Rounding / estimating is a useful skill, especially as pupils tend to believe answers they get on a calculator. By having an understanding of and the ability to estimate, calculator errors can be picked up. Word problems involving rounding using decimal places are included.
In Task 11 , pupils are to round numbers to various significant figures as requested. Counting begins from the first non-zero from the left, following the procedures outlined on Worksheet 8.

## Task 10

1. $1.2,1.24,1.236 \quad$ 2. $3.6,3.60,3.604 \quad$ 3. $9.8,9.75,9.753 \quad$ 4. $10.6,10.63,10.635 \quad$ 5. $0.1,0.06,0.056$
2. $23.5,23.51,23.507 \quad$ 7. $18.5,18.46,18.463 \quad$ 8. $53.4,53.42,53.422 \quad$ 9. $143.9,143.89,143.889 \quad 10.6 .4,6.39$, $6.38511 .0 .1,0.10,0.096 \quad 12.9 .3,9.26,9.260 \quad 13.186 .1,186.07,186.071 \quad 14.1 .0,1.00,1.001 \quad 15.56 .8$, $56.76,56.756$ 16. $5602.7,5602.70,5602.703$ 17. $0.1,0.05,0.053$ 18. 6.4, 6.41,6.409 19. $67.2,67.16,67.160$ 20. 1.0, 0.96, 0.964 21. 2.7, 2.72, 2.720 $\quad$ 22. $9058.1,9058.10,9058.098 \quad$ 23. $0.0,0.01,0.009$
$\begin{array}{llllll}\text { 24. } 9.5,9.46, ~ 9.462 ~ & 25.703 .0,702.96,702.964 & \text { 26. } 0.0,0.00,0.001 & \text { 27. } 4.6,4.60,4.601 & 28.1 .0,1.00,1.000\end{array}$
3. $56.0,56.00,56.000 \quad 30.132 .0,132.00,132.000 \quad 31.24 .4,24.44 \quad 32.25 .1,25.07 \quad 33.3 .0,3.04$
4. 5.1,5.06 $35.5 .3,5.26 \quad 36.4 .5,4.49 \quad 37.16 .0,16.01 \quad 38.7 .1,7.12 \quad 39.28 .2,28.17 \quad 40.7 .1,7.08$ 41. $30.7,30.67$ 42. $8.1,8.09 \quad 43.27 .1,27.10 \quad 44.15 .9,15.95$ 45. $2.6,2.61 \quad 46.6 .9,6.86 \quad 47.11 .1,11.11$ 48. $10.1,10.09 ~ 49.5 .6,5.56 \quad 50.6 .4,6.39 \quad 51.4 .8,4.80$ 55. $68.237,68.956,69.048,69.378,69.637,70.653,71.284,71.632,72.564,75.396 \quad 56.68 .24,68.96,69.05,69.38$, $69.64,70.65,71.28,71.63,72.56,75.40 \quad 57.1 \mathrm{~min} 63.79 \mathrm{sec}, 1 \mathrm{~min} 56.35 \mathrm{sec}, 1 \mathrm{~min} 52.09 \mathrm{sec}$,
$1 \mathrm{~min} 51.95 \mathrm{sec}, 1 \mathrm{~min} 51.63 \mathrm{sec}, 1 \mathrm{~min} 50.27 \mathrm{sec}, 1 \mathrm{~min} 49.93 \mathrm{sec}, 1 \mathrm{~min} 49.76 \mathrm{sec}, 1 \mathrm{~min} 48.74 \mathrm{sec}, 1 \mathrm{~min} 45.72 \mathrm{sec}$
$58.1 \mathrm{~min} 63.8 \mathrm{sec}, 1 \mathrm{~min} 56.4 \mathrm{sec}, 1 \mathrm{~min} 52.1 \mathrm{sec}, 1 \mathrm{~min} 52.0 \mathrm{sec}, 1 \mathrm{~min} 51.6 \mathrm{sec}, 1 \mathrm{~min} 50.3 \mathrm{sec}, 1 \mathrm{~min} 50.0 \mathrm{sec}$,
$1 \mathrm{~min} 49.8 \mathrm{sec}, 1 \mathrm{~min} 48.7 \mathrm{sec}, 1 \mathrm{~min} 45.7 \mathrm{sec} \quad 59.125270 \mathrm{~mL}, 125.27 \mathrm{~L} \quad 60.125 .3 \mathrm{~L} \quad 61 . \$ 218.75$

## Task 11

$\begin{array}{llllll}\text { 1. } 4000, ~ 4300, ~ & 4260 & \text { 2. } 90000,94000, ~ & 93700 & \text { 3. } 40000,44000,44000 & 4.8000,7600,7590\end{array}$ 5. 600000, $650000,645000 \quad 6.0 .05,0.052,0.0524 \quad$ 7. $0.009,0.0085,0.00853 \quad$ 8. $0.0005,0.00046,0.000465$ 9. $0.5,0.49,0.486 \quad 10.4,3.7,3.70 \quad 11.0 .1,0.096,0.0958 \quad$ 12. $9,9.3,9.26 \quad 13.200,190,186 \quad 14.1,1.0,1.00$ 15. $60,57,56.8 \quad 16.6000,5600,5600 \quad 17.0 .05,0.053,0.0530 \quad 18.6,6.4,6.41 \quad 19.200,170,167$ 20. $1,0.96,0.964 \quad 21.3,2.7,2.72 \quad$ 22. $60,58,58.1 \quad 23.0 .009,0.0087,0.00869 \quad 24.9,9.5,9.46 \quad 25.300$, 320,323 26. $0.03,0.031,0.0305 \quad$ 27. $5,4.6,4.60 \quad 28.500,490,485 \quad$ 29. $30,27,27.0 \quad 30.0 .7,0.65,0.650$ $\begin{array}{lllllll}31 . & 6000,5600 & 32.4000,4200 & 33.60000,63000 & 34.90,92 & 35,100,140 & 36.600,580 \\ 37.600,610\end{array}$ $\begin{array}{llllllll}38 . & 900,880 & 39.3000,2600 & 40.7 .1 & 41.20,18 & 42.0 .08,0.080 & 43.1000,1200 & 44.7000,7200\end{array}$ $\begin{array}{llllllll}45.100,110 & 46.100,110 & 47.700,650 & 48.1000,1100 & 49.1000,1500 & 50.10,11 & 51.5,4.8\end{array}$ 52. 4, 3.9 53. $30,33 \quad$ 54. $30,30.4 \quad$ 55. $130,260,190,220,460,97,380,240,170,81=2228 \mathrm{~km} \quad 56.2213 \mathrm{~km}$ 57. $15 \mathrm{~km} \quad 58.12000,9900,13000,11000,10000,10000,12000,10000,13000,10000=110900$ people 59. 111165 people 60.265 people

## Finding squares and estimating square roots:

## Worksheet 9

In Task 12, pupils are to square numbers, rounding to $1 \mathrm{~d} . \mathrm{p}$. or $2 \mathrm{~d} . \mathrm{p}$. The opposite of squaring a number is to find the square root of a number. This is first to be attempt using a trial and error method, find estimates accurate to $2 \mathrm{~d} . \mathrm{p}$. Using the square root key on a calculator, exact answers rounded to 4 d . $p$. are to be found. Word problems involving find square roots are included.

## Task 12

$\begin{array}{lllllllllll}\text { 1. } 39.7 & \text { 2. } 74.0 & 3.110 .3 & \text { 4. } 136.9 & 5.158 .8 & \text { 6. } 334.9 & \text { 7. } 2190.2 & \text { 8. } 3564.1 & 9.9293 .0 & 10.12723 .8\end{array}$ $\begin{array}{lllllllll}11.5 .57 & 12.48 .30 & 13.24 .80 & 14.94 .67 & 15.93 .12 & 16.50 .84 & 17.0 .13 & 18.92 .35 & 19.74 .82\end{array}$ 20. 9.5921 to 45 No answers supplied 46. $4.4721,5.1962,6.3246,7.4162,7.7460,8.3066,8.6603,8.9443$, $9.2195,10.4881,11.4018,12.2474,12.9615,14.1421,15.8114,3.1145,3.5917,5.8224,6.5498,8.7636,0.9747,7.5353$, $11.8068,23.7466,29.3718 \quad 47.16$ cobble stones $48.62 .5 \mathrm{~cm} \times 62.5 \mathrm{~cm} \quad 49$. $\$ 320 \quad 50$. 12 tiles 51. 144 tiles 52. $\$ 93.60 \quad$ 53. 8 tiles $54.2 .4 \mathrm{~m} \times 2.4 \mathrm{~m}$

## Expressing a fraction as a decimal:

Expressing a decimal as a fraction:
Expressing a decimal as a percentage:
Expressing a percentage as a decimal:

## Converting between fractions, decimals and percentages:

In Task 13, pupils are to convert fractions to decimals by dividing the numerator by the denominator. Setting out the division problem correctly is important and zeros are added after the decimal point, with the division continuing until there is no remainder or a repeating pattern is found, indicated by a small dot to the top right of the repeating digit(s).. Pupils are to explore the decimal patterns created when various fractions are converted to decimals.

In Task 14, pupils are to perform the opposite conversion, decimals to fractions, which is less difficult as the denominator will be $10,100,1000$, etc. depending on the number of digits after the decimal points. The fractions created will be either $1 / 10$ 's, $1 / 100$ 's, $1 / 1000^{\prime}$ s or $^{1 / 10000}$ 's etc.

Example: $0.5=5 / 10,0.05=5 / 100,0.005=5 / 1000,0.0005=5 / 10000$

In Task 15, pupils are to convert decimals to percentages. As percentages are out of 100, this can be done by multiplying the decimal by 100 , that is, move the decimal point two places to the right.

In Task 16, pupils are to convert percentages to decimals. This can be done by dividing the percentage by 100, resulting in the decimal point moving two places to the left. Remind pupils that if there is no decimal point shown in a number, then the decimal point will be at the right hand end of the number. Example: 65\% has the decimal point after the 5, that is, $65.0 \%$.
In Task 17, pupils are to test their skills at converting between fractions, decimals and percentages, as they match examples of fractions, decimals and percentages.

## Task 13

$\begin{array}{llllllllllllll}1.0 .2 & \text { 2. } 0.125 & 3.0 .3 & 4 . & 0.6 & 5.0 .875 & 6.0 .5714 & \text { 7. } 0.06 & 8.0 .83 & 9.0 .5 & 10 . & 0.6 & 11 . & 0.583\end{array}$ $\begin{array}{lllllllllllll}12 . & 0.75 & 13 . & 0.3 & 14.0 .9 & 15.0 .5 & 16.0 .25 & 17.0 .625 & 18.0 .4 & 19.0 .75 & 20.0 .46 & \text { 21. } 0.3\end{array}$ 22. $0.25 \quad$ 23. $0.25 \quad 24.0 .6 \quad$ 25. $0.2 \quad$ 26. $0.0 \cdot 9 \cdot, 0.1 \cdot 8 \cdot 0.2 \cdot 7 \cdot 0.3 \cdot 6 \cdot 0.4 \cdot 5 \cdot 0.5 \cdot 4 \cdot, 0.6 \cdot 3 \cdot 0.7 \cdot 2 \cdot, 0.8 \cdot 1 \cdot 0.9 \cdot 0$ 27. $0.1 \cdot 0.2 \cdot 0.3 \cdot 0.4 \cdot 0.5 \cdot 0.6 \cdot 0.7 \cdot 0.8 \quad 28.0 .1 \cdot 42851,0.2 \cdot 85714 \cdot 2,0.4 \cdot 28571 \cdot 4,0.5 \cdot 71428 \cdot 5,0.7 \cdot 14285 \cdot 7$, $0.8 \cdot 57142 \cdot 8$

## Task 14





29. ${ }^{48} / 1000,{ }^{12} / 250 \quad 309 / 1000$

## Task 15

1. $26 \%$
2. $8 \% \quad$ 3. $1.2 \%$ 4. $27 \% \quad$ 5. $2.9 \%$
3. $74 \%$ 7. $40 \%$
4. $75 \%$
5. $52 \% \quad 10.87 \%$
6. $26.7 \%$
$12.37 \% \quad 13.8 .5 \% \quad 14.90 \% \quad 15.70 \% \quad 16.65 \% \quad 17.12 .5 \% \quad 18.60 \% \quad 19.40 .3 \% \quad 20.2 \% \quad 21.3 .6 \%$
7. $210 \% \quad 23.345 \% \quad$ 24. $4.1 \% \quad 25.8 .3 \% \quad 26.30 \% \quad 27.0 .5 \% \quad 28.6 .3 \% \quad 29.186 \% \quad 30.69 \%$

## Task 16

1. 0.65
2. 0.5
3. 0.09
4. 0.15
5. 0.45
6. 0.87
7. 0.55
8. 1 9. 0.17
9. 0.05
10. 0.52
11. 0.4
12. 0.93
13. 0.8
14. 0.23
15. 0.75 17. 0.66 18. 0.3
16. 0.375
17. 0.805
18. 0.018
19. 1.4
20. 0.006
21. 1.37
22. 3.06 26. 0.009 27. 0.0395 28. 0.96 29. 0.548
23. 0.849

## Task 17

| Fraction | Decimal | Percentage |
| :---: | :---: | :---: |
| $1 / 4$ | 0.25 | $25 \%$ |
| $1 / 3$ | 0.3 | $33.3 \%$ |
| $2 / 5$ | 0.4 | $40 \%$ |
| $1 / 2$ | 0.5 | $50 \%$ |
| $2 / 3$ | 0.6 | $66.6 \%$ |
| $3 / 4$ | 0.75 | $75 \%$ |

Finding a percentage of a quantity:
Worksheets 12 \& 13

## Multiplying and dividing decimals:

In Task 18, pupils are to find percentages of a quantity. This can be done using either of the two ways illustrated on the worksheet. Word problems are included and pupils are to create and exchange word problems among themselves.
In Task 19, pupils are to multiply and divide decimals, utilising skills they have learnt over the past few years. Setting out is important and the correct setting out will help to avoid errors.

## Task 18



## Task 19



## Understanding negative numbers:

Understanding and using number lines:
More negative numbers:
Bank overdrafts:
In Task 20, pupils are introduced to negative numbers, by way of everyday events that can be represented as negative numbers. Calculations involving temperature changes is a particularly good way to introduce negative numbers as weather forecasts include the liklihood of frosts, thus highlighting the use of negative numbers.
In Task 21 , pupils are introduced to number lines that include negative numbers. Pupils should be familiar with number lines as they form part of $x-y$ graphs. Using the number line, including negative numbers, pupils are to add positive and negative number together. Adding a negative number results in a movement to the left along the number line. The starting point on the number line is the first number that is in the question.

In Task 22, small groups of pupils are to play a number game with a die (dice). The odd numbers on the die are negative and the even numbers are positive. Pupils are to keep a running total as they roll the die 5 times. The pupil with the lowest score wins.
In Task 23, pupils are to further develop their understanding of negative numbers as they add larger positive and negative numbers.
In Task 24, pupils are to calculate a running total of a bank balance that goes in and out of overdraft. This task is a good example of negative numbers in daily use. On a bank statement, a debit balance is negative and a credit balance is positive.

## Task 20

| 1. $-3,-2,-1, G, 1,2,3,4$, | , $5,6,7,8,9,10$ | 2. ${ }^{-2}$ floor | 3. 4 th floor | 4. 20 m | 5. $4 \mathrm{~m} \quad 6$ | 6. $6,12,16,18$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7. $-4,-8,-10,-16,-20$ | 8. -14 9. -3 | 10. $5.5{ }^{\circ} \mathrm{C}$ ap | ox $11.4{ }^{\circ} \mathrm{C}$ | 12. $8^{\circ} \mathrm{C}$ | 13. $-3^{\circ} \mathrm{C}$ | 14. $7^{\circ} \mathrm{C} \quad 15.4^{\circ} \mathrm{C}$ |
| 16. $-7^{\circ} \mathrm{C}$ 17. ${ }^{-8}{ }^{\circ} \mathrm{C} \quad 1$ | 18. $4^{\circ} \mathrm{C} \quad 19.5^{\circ} \mathrm{C}$ | 20. ${ }^{-9}{ }^{\circ} \mathrm{C}$ | 21. $-3.5{ }^{\circ} \mathrm{C}$ | 22. $4.4{ }^{\circ} \mathrm{C}$ | 23. $-1.3^{\circ} \mathrm{C}$ | C $24.2 .1{ }^{\circ} \mathrm{C}$ |

## Task 21

 $\begin{array}{llllllllllllllll}15 . & 16 & 16 .-4 & 17.9 & 18 . & -7 & 19.7 & 20 . & -6 & 21.3 & 22 . & -9 & 23 . & -11 & 24 . & -11 \\ 25 & -8 & 26.8\end{array}$ 27. $10 \quad 28 .-6 \quad 29.8 \quad 30 .-1 \quad 31 .-1 \quad 32.10 \quad 33 .-5 \quad 34.12 \quad 35 .-4 \quad 36 .-6$ 39. $-11 \quad 40 .-19 \quad 41 .-22 \quad 42 .-14 \quad 43.5 \quad 44.11 \quad 45 .-4 \quad 46 .-6$

## Task 23



## Task 24

Balance $=\$ 112.50,-\$ 72.50,-\$ 17.90,-\$ 87.55,-\$ 1.75, \$ 48.25, \$ 22.50, \$ 92.70,-\$ 107.25$

## Expressing a quantity as a fraction or as a percentage of a whole: Increasing and decreasing by a given percentage:

In Task 25, pupils are to express a quantity as a fraction of a whole and then convert the fraction to a percentage, or vica versa.
In Task 26, pupils are to calculate a percentage of a number and then increase or decrease the number by this amount. The idea of GST, discounts or mark-up, wholesale and retail prices all illustrates practical uses of using percentages. Word problems are included.

## Task 25

1. $2 / 8=1 / 4=25 \%$
2. $6 / 8=3 / 4=75 \%$
3. $4 / 10=2 / 5=40 \%$
4. $4 / 12=1 / 3=33^{1} / 3 \%$
5. $65 / 100=13 / 20=65 \%$
6. $35 / 100=7 / 20=35 \%$
7. $19 / 50=38 \%$
8. ${ }^{17} / 20=85 \%$
9. $9 / 25=36 \%$
10. $3 / 5=60 \% \quad 11 .{ }^{18} / 40=9 / 20=45 \%$
11. $\$ 17.55$
12. $3 / 5=60 \%$
13. $40 \%=2 / 5$
14. 16 min 40 sec
15. $150 / 240=5 / 8=62.5 \%$
16. $\$ 108$
17. 27500
18. $21000 / 27500=42 / 55=76.36 \% \quad 20.6500 / 27500=13 / 55=23.63 \%$
19. $92 \%$

## Task 26



## Writing and simplifying ratios: <br> Writing ratios as fractions:

Sharing quantities by a given ratio:
Creating equivalent fractions and simplifying fractions: Improper fractions and mixed numbers:
Adding and subtracting fractions:
In Task 27, pupils are to write information within a statement as a ratio. The order of the numbers in the ratio will depend on the order in the statement. Example: In Room 7 there are 13 boys and 15 girls. What is the ratio of girls to boys in Room 7? Answer: 15:13
In Task 28, pupils are to rewrite ratios as fractions, then simplify if possible.
In Task 29, pupils are to share quantities by a given ratio, using the steps as outlined in Worksheet 20.
Word problems involving ratios have been included.
In Task 30, pupils are to explore equivalent fractions. A fraction of a group of diagrams has been shaded and pupils express the shaded diagrams as a fraction of the group. A series of progressive exercises guide pupils through the process of working out and creating equivalent fractions. Some large fraction can be simplied to create smaller equivalent fractions. This can be done by dividing the numerator and denominator by the same number.
In Task 31 , pupils are to convert between improper and mixed numbers, using the steps outlined in Worksheet 22.

In Task 32, pupils are to add and subtract fractions. Fractions can only be added or subtracted if the denominators are the same. This is done by creating equivalent fractions. Word problems have been included.

## Task 27

$\begin{array}{llllll}\text { 1. } 5: 7 & \text { 2. } 5: 20=1: 4 & \text { 3. } 40: 60=2: 3 & 4.3: 27=1: 9 & \text { 5. } 78: 14=39: 7 & \text { 6. } 45: 90=1: 2\end{array}$
7. $15: 18=5: 6 \quad 8.6: 30=1: 5 \quad 9.85: 600=17: 120 \quad 10.32: 4=8: 1 \quad 11.1: 5 \quad 12.2: 1 \quad 13.3: 5$
14. $9: 20 \quad 15.9: 11 \quad 16.4: 1 \quad 17.7: 5 \quad 18.4: 7 \quad 19.9: 5$
$\begin{array}{lllllll}24.8: 3 & 25.7: 12 & 26.1: 3: 2 & 27.7: 3: 9 & 28.2: 4: 1 & \text { 29. } 12: 5: 2 & 30.3: 4: 8\end{array}$

## Task 28

1. $14 / 28=1 / 2$ 2. $15 / 30=1 / 2 \quad 3 \cdot{ }^{24} / 36=2 / 3$
2. $15 / 40=3 / 8$
3. $33 / 77=3 / 7$
4. $12 / 32=3 / 8 \quad 7 . \quad{ }^{21} / 42=1 / 2$
5. $27 / 63=3 / 7$
6. $45 / 60=3 / 4 \quad 10 . \quad 30 / 120=1 / 4$
7. $50 / 72=25 / 36$
8. ${ }^{84} / 72=7 / 6$
9. $56 / 88=7 / 11$
10. $108 / 81=4 / 3$
11. $49 / 84=7 / 12$
12. $120 / 65=24 / 13$
13. $150 / 25=6 / 1$
14. ${ }^{26} / 39$
15. $72 / 160=9 / 20$
16. $96 / 108=8 / 9$

## Task 29

$\begin{array}{lllllllllllllll}1.9 & 2.7 & 3.7 & 4.11 & 5.19 & 6.8 & 7.14 & 8.15 & 9.21 & 10.23 & 11.15 & 12.19 & 13.20 & 14 . & 20\end{array}$ | 15． 21 | $16 . ~$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | $10: \$ 40 \quad 17.9 \mathrm{~mm}: 18 \mathrm{~mm} \quad$ 18．$\$ 8: \$ 40 \quad 19.27 \mathrm{~kg}: 36 \mathrm{~kg} \quad$ 20．$\$ 24: \$ 60 \quad 21.84 \mathrm{~kg}: 24 \mathrm{~kg}$ $\begin{array}{llllll}\text { 22．} \$ 52: \$ 65 & 23.8 \mathrm{mg}: 88 \mathrm{mg} & \text { 24．} \$ 33: \$ 55 & \text { 25．} 40 \mathrm{~kL}: 24 \mathrm{~kL} & \text { 26．} \$ 16: \$ 56 \quad 27.49 \mathrm{~L}: 7 \mathrm{~L}\end{array}$

28．$\$ 121: \$ 22 \quad 29.120 \mathrm{~cm}: 80 \mathrm{~cm} \quad$ 30．$\$ 90: \$ 180 \quad$ 31． 40 children $\quad$ 32．$\$ 6000 \quad$ 33．$\$ 4687.50: \$ 7812.50$ 34． 2556 supporters $\quad 35.20: 100=1: 5 \quad 36 . \$ 100 \quad 37 . \$ 1000 \quad 38.27$ weeks $\quad 39.0 .6: 1.8: 1.2$ 40．900L ：600L：1200L

## Task 30

1．$\because \bigcirc$
2．丑 册
曲
3.

4.

5．囲囲囲
囲囲口

6． $3 / 5 \quad$ 7． $4 / 8=1 / 2 \quad 8.3 / 7 \quad 9.6 / 9=2 / 3 \quad 10.2 / 8=1 / 4$ 11． 7 12． 25 13． 5 14． 15 15． 8 16． 12 $\begin{array}{llllllllllll}17 . & 18 & 18.30 & 19.24 & \text { 20．} 24 & 21.48 & 22.10 & 23.55 & 24.56 & 25.36 & 26.24 & 27.24\end{array} 28.27$

 51． $120 / 200=3 / 5 \quad 52 .{ }^{70} / 146={ }^{35} / 73 \quad 53 .{ }^{8} / 14=4 / 7 \quad 54 .{ }^{134} / 152=67 / 76 \quad 55 .{ }^{24} / 144=1 / 6 \quad 56 .{ }^{14} / 20=7 / 10$
57．${ }^{122} / 156=61 / 78 \quad 58 . \quad 28 / 32=7 / 8$
59． $220 / 540=11 / 27 \quad 60.4 / 100=1 / 25$
61． $44 / 50=22 / 25$
62．${ }^{23 / 80}$
63．${ }^{84} / 124=21 / 31 \quad 64 .{ }^{18} / 120=3 / 20$

## Task 31

1． $3 / 5$
2． $6 \frac{3 / 4}{} \quad 3.6 \frac{3}{5}$
4． $9 \frac{1}{2}$
5． $9 \frac{6}{7}$
6． $8^{7 / 8}$
7． 10 \％／9
8． $45 / 6$
9． $8^{2 / 3}$
10． $145 / 7$
11． $7^{4 / 11}$
12． $123 / 10$
13． $23 / 5$
14．${ }^{17} / 2$
15．${ }^{31 / 4} \quad 16 .{ }^{29 / 3}$
17． $59 / 6$
18． $42 / 5$
$\begin{array}{lll}\text { 19．} & 43 / 6 & \text { 20．}\end{array}{ }^{49} / 5 \quad$ 21．${ }^{93} / 8$
22． $94 / 9$
23．${ }^{115 / 9}$ 24． $65 / 12$

## Task 32

1． $1 \frac{1}{2} / 2$
2． 1 3． 1
4． $1^{6 / 11}$
5． $1^{2 / 7}$
6． $3 / 5 \quad 7.1 / 2$
8． $1 / 3$
9． $5 / 12 \quad 10 .{ }^{4} / 11$
11． $1^{5 / 12}$
12．${ }^{13} /{ }_{15}$
13． $1^{7 / 20}$
14． $15 / 12$
15． $8^{4 / 15}$
16． $2 / 5$
17． $9 / 40$
18． $9 / 56$
19． $1 \frac{3 / 5}{5}$
20． $3^{8 / 15}$
21． $5 / 8$
22． $1 \frac{1}{8}$ pizzas
23． $9 / 20$
24． $2 \frac{1}{2}$ minutes
25． $7^{11 / 15}$ metres

## Table of Contents for the Homework / Assessment Worksheet Masters for Number, Level 5

| Worksheet Number | Topic | $\begin{gathered} \text { Number } \\ \text { Objective(s) } \end{gathered}$ |
| :---: | :---: | :---: |
| 1 | Working with whole numbers / Word problems | Revision |
| 2 | Number facts / multiples / Factors / Prime numbers / Order of operations / Word problems | Revision |
| 3 | Squares and square roots / Approximations \& Estimations / Rounding off / Decimal places / Significant figures | N1 / N2 / N3 |
| 4 | Decimals / Fractions / Percentages | N5 |
| 5 | Decimal Operations / Estimations | N4 / N5 |
| 6 | Introductions to integers / Multiplication \& division squares | N6 |
| 7 | Calculating percentages / Writing percentages / Using percentages | N7 / N8 |
| 8 | Writing ratios / Simplifying ratios / Sharing in a given ratio | N9 |
| 9 | Equivalent fractions / Writing fractions / Simplifying / Mixed numbers \& Improper fractions | N9 |
| 10 | Adding \& subtracting fractions / Word problems | N9 |
|  | Answers |  |

To be completed by:

A: 10 Quick Questions

1. $963+857=$
2. How many days in $6 \frac{1}{2}$ weeks? $\qquad$
3. $3000-1285=$
4. How many months in five years?
5. $578 \times 9=$ $\qquad$
6. How many seconds in 9 minutes? $\qquad$

## Down

7. $\quad \$ 6.89 \times 7=$
8. $169 \div 13=$ $\qquad$
9. How many weeks in 4 years?
10. $306 \div 9=$ $\qquad$

## E: Magic Square

| Find the missing |  | 16 |
| :---: | :---: | :---: |
|  |  | 11 |
| this magic square. | 10 | 12 |

## Across

## B: Number Cross

| 1. | $456 \div 8$ | 2. | $276+485$ |
| :--- | :--- | :--- | :--- |
| 6. | $774 \div 9$ | 7. | $7837-4853$ |
| 9. | $13 \times 7$ | 10. | $651 \div 7$ |
| 11. | $551-467$ | 12. | $199 \times 5$ |
| 13. | $411+293-637$ |  |  |



| 1. | $1141-589$ | 3. | $4 \times 17$ | 4. | $678+963$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 5. | $588 \div 6$ | 8. | $1071 \times 9$ | 9. | $1344-398$ |
| 10. | $495 \div 5$ |  |  |  |  |

C: Find the missing numbers
Replace each shape with a number.

|  | $378+\varphi=738$ |  |
| :---: | :---: | :---: |
|  | $53 \times 9=477$ |  |
| 5. | $\checkmark+346=915$ |  |
|  | - $\times 63=504$ |  |
|  | $214-4=68$ |  |
|  | $49 \times 4=343$ | $\stackrel{+}{*}$ |
| 13. | . $\downarrow+187=643$ |  |
|  | - $\times 59=649$ |  |

1. Rangi went to the shop and bought 43 apples, 18 oranges and 29 kiwi fruit. How many pieces of fruit did he buy?
2. Rebecca and Steven have been collecting telephone cards, and together they have 257. If Steven has 184, how many does Rebecca have?
3. Alisi bought 14 boxes of matches. If each box contains 49 matches, how many matches does he have altogether?
4. Mrs Jones has $\$ 128$ to share between her 4 grandchildren. How much would each grandchild receive?
5. Items in a garge sale sell for $\$ 21, \$ 7, \$ 18, \$ 9$ and $\$ 13$. If Sam and Alex are to share this money equally, how much does each person get?
This table shows the number and colour of jelly beans in four boxes which Kiri bought.

| $\\|\\|\\|\\|d\\|\\|$ | Box A | Box B | Box C | Box D |
| :---: | :---: | :---: | :---: | :---: |
| Red | 27 | 26 | 32 | 29 |
| Blue | 17 | 29 | 26 | 27 |
| Green | 25 | 19 | 17 | 24 |
| White | 24 | 19 | 23 | 18 |

6. How many white jelly beans in box $D$ ?
7. How many red jelly beans in box A?
8. How many blue jelly beans in all boxes?
9. Which box had the most white jelly beans?
10. How many jelly beans in box $C$ ?
11. Which box had the least green jelly beans?
12. How many jelly beans altogether?

Please sign:

A: 10 Quick Questions

1. $415 \times 23=$ $\qquad$
2. $1780 \div 5=$
3. Find the missing number $108 \div 9=9$
4. $\$ 6.32 \times 7=$
5. How many sides does a square have?
6. Name this shape

7. $34344 \div 6=$
8. $156+278=$ $\qquad$
9. Find the missing number $\nabla+862=1273$
10. How many centimetres in 2.5 m ?

## B: Numbers Facts

1. Write down the even numbers between 50 and 63
2. Write down the odd numbers between 68 and 77
3. Write down the first 4 multiples of 11
4. Write down the multiples of 7 between 40 and 58
5. How many multiples of 6 are less than 37 ?
6. Write down the prime numbers less than 20
7. Write down the prime numbers between 15 and 35 .
8. What are the factors of 12 ?
9. What are the factors of 28?
10. What are the factors of 36 ?

## D: Word Problems

1. Angela walks to and from school each day, a total of 5 km . How far does she walk in two school weeks?
2. Frank bought a piece of wood 360 cm long. He cuts 8 pieces, each 40 cm long from this piece of wood. How much is left after he has cut the 8 pieces off?

This table shows the price of tickets sold, and the number of each type sold.
3. How many $\$ 15$ tickets were sold?
4. How many tickets were sold altogether?

| Price of <br> ticket | $\$ 15$ | $\$ 20$ | $\$ 25$ |
| :---: | :---: | :---: | :---: |
| Total <br> sold | 45 | 30 | 25 |

5. What would it cost to buy 9 tickets at $\$ 15$ each?
6. What would it cost to buy 13 tickets at $\$ 20$ each?
7. What would it cost to buy 8 tickets at $\$ 25$ each? $\qquad$
8. If Steven buys four $\$ 15$ tickets and six $\$ 20$ tickets, how much would this cost him?
9. If Graham buys seven $\$ 15$ tickets and five $\$ 20$ tickets, how much would this cost him?
10. If Janine has $\$ 95$ how many $\$ 15$ tickets can she buy?
11. If Ken has $\$ 165$ how many $\$ 25$ tickets can he buy?
12. If Andrew has $\$ 110$ and buys $4 \$ 25$ tickets, how much change does he have left after buying the tickets?
13. If Jackie has $\$ 160$ and buys $9 \$ 15$ tickets, how much change does he have left after buying the tickets?

## Order of Operations

1. $17+9-12=$
2. $21-7+10=$
3. $36 \div 9+15=$
4. $9 \times 7+6=$
5. $23+4 \times 6=$
$6 \quad 60 \times 4-47=$
6. $80-9 \times 8=$
7. $39+6 \times 9=$
8. $39-36 \div 3=$
9. $42 \div 7+13=$
10. $(18+27) \times 3=$
11. $5(49-19)=$
12. $7(49-28)=$
13. $6(34+46)=$
14. $8(63+27)=$
15. $11+3(7+13)=$
16. $51-4(37-29)=$
17. $4(6+4 \times 3)=$
18. $6(24 \div 3+7)=$
19. $8+2(21+9)=$
20. $5(9+4 \times 5)=$
21. $19-2(18-11)=$
22. $9+3(24-5 \times 3)=$
23. $29-5(7 \times 2-9)=$
24. $7(4+6 \times 4)-40=$
25. $9(3 \times 9-18)-17=$

# Homework / Assessment Worksheet 

To be completed by:


A: 10 Quick Questions

1. $39+4 \times 8=$
2. $\$ 3.46 \times 13=$
3. How many days in 16 weeks?
4. How many metres in 4.5 kms ?
5. Write $3.2 \times 10^{5}$ as an ordinary number
6. Name this shape (III)
7. Find the missing number a $15+\boldsymbol{*}-47=36$
s.........
8. List the factors of 32
9. Round 72 to the nearest ten
10. Round off 8.35 to one decimal place $\qquad$

## B: Finding Percentages

 Calculate1. $10 \%$ of $\$ 70$ $\qquad$
2. $25 \%$ of 160 kg $\qquad$
3. $75 \%$ of $\$ 48$ $\qquad$
4. $50 \%$ of $\$ 4.50$ $\qquad$
5. $20 \%$ of 320 cm $\qquad$
6. $60 \%$ of 70 kg $\qquad$
7. $33 \frac{1}{3} \%$ of $\$ 45$ $\qquad$
8. $45 \%$ of $\$ 600$ $\qquad$
9. $15 \%$ of 60 m $\qquad$
10. $120 \%$ of $\$ 80$

## G: Decimals / Fractions / Percentages

| Complete the table by converting between commonly used decimals, fractions and percentages. | Decimals $\rightarrow$ | $\leftarrow$ Fractions $\rightarrow$ | $\leftarrow$ Percentages |
| :---: | :---: | :---: | :---: |
|  | 1. | 2. | 10\% |
|  | 0.25 | 3 | 4. |
|  | 5. | $\frac{1}{3}$ | 6. |
|  | 7. | 8. | 50\% |
|  | 9. | $\frac{2}{3}$ | 10. |
|  | 0.75 | 11. | 12. |

## D: Word Problems

1. If $48 \%$ of a club were girls, what percentage were boys?
2. Amanda is in a class of 28 pupils. If $50 \%$ were boys, how many were girls?
3. $10 \%$ of a garden of $160 \mathrm{~m}^{2}$ was planted in roses. What was the area planted in roses?
4. A body contains $70 \%$ water. If Jeremy weighs 60 kg , how much of his weight is water?
5. A class survey on pets, showed that $80 \%$ were cats. If there were 50 pets, how many were cats?
6. Rangi counted 180 cars going past the school gate. If $60 \%$ were going too fast, how many cars was this?
7 In a class of $28,25 \%$ wanted to take netball as a sport. How many students was this?
7. Linwood High School played 20 soccer games during the season, losing only $15 \%$. How many games did they lose?
8. In a school of 670 students, $10 \%$ were absent on Monday. How many were absent?
9. Calculate $30 \%$ of $\$ 26.75$, round off to nearest cent.

## E: Percentages

Find the percentage shaded in each diagram.
1.

2.

3.

4.

5.

6.

7.

8.

9.

10.


[^1]To be completed by:

| A: | 10 Quick Questions |
| :---: | :---: |
| 1. | 42-9×4 |
| 2. | What would 7 items at $\$ 9.30$ each cost? |
| 3. | How many minutes in 16 hours? |
| 4. | How many metres in 3.75 kms ? |
| 5. | Find 10\% of \$84 |
| 6. | Name this shape $\square$ $\qquad$ |
| 7. | Find the missing number $42+9-69=51$ |
| 8. | List the factors of 40 |
| 9. 10. | Round off 8.34 to one decimal place <br> Find $\sqrt{81}$ |

## B: Estimations

Have a guess? Without
calculating the exact answer.
Estimate answer

1. $20.5+4.3=$ eq 24
2. $149.9+51.4=$ $\qquad$
3. $8.6 \times 10.3=$
.............
4. $98 \div 5.2=$
5. $\frac{242}{83}$
6. $\quad 6.3 \times 18.5=$
7. $24.2-11.9=$ $\qquad$
8. $797.5-347.2=$
9. $9.3+2.9 \times 5.1=$ $\qquad$
10. $3.1 \times 5.9+11.9=$ $\qquad$
11. $897.5-637.2=$ $\qquad$

## C: Decimals Operations

Calculate the following ...
1.

| 69.25 |
| ---: |
| +8.78 |

2. 

3.605
3.

| 96.57 |
| ---: |
| -43.25 |

4. $\begin{array}{r}9.250 \\ -4.127 \\ \hline\end{array}$
5. $31.86+0.798=$ $\qquad$ 6. $354.89+65.235=$
6. $96.87-74.73=$
7. $200-96.313=$
8. $52+8.4+0.417=$
9. $28.7-9.15+6.3=$
10. 

2.86
12.
5.94
13.
3.197
14.
4. $\quad 60.4$ $\times 1.2$
15. $72.4 \times 0.4=$ $\qquad$ 16. $4.27 \times 0.03=$
17. $6.340 \div 0.5=$
18. $45.27 \div 0.9=$
19. $0.84 \div 1.2=$
20. $0.648 \div 0.04=$
21. $0.74 \div 0.002=$
$\times 0.4$
$\times 0.02$

$=$.
$5=$
$=\ldots$
0
$=$
D: How much will it Cost?
A school is going to set up a computer in the school office so they can produce newsletters to send home. What will it cost if they buy ...
Computers
$\$ 1750$ each


1. 3 computers
2. 30 computer disks
3. 2000 envelopes
4. 5000 sheets of paper
5. What is the total cost of setting up the school office?
6. What does one computer disk cost?
7. What would 45 computer disks cost?
8. What would 120 computer disks cost?
9. What would it cost to buy 10000 sheets of paper?
10. What would it cost to buy 15000 sheets of paper?
11. The school is going to buy 25 computers to set up in a new classroom. What would this cost?
12. If a school has $\$ 14000$ to spend on computers, how many computers could they buy and how much money would they have leftover? computers \$.
13. If the newsletters are to be posted home each week, at a cost of 40 cents each, how much would this cost each week, if there are 562 pupils at this school?
14. $7.9 \times 9.8=$
15. $26.8 \div 3.7=$ $\qquad$
16. $9.3+4.3 \times 5.1=$
17. $\quad 6.23^{2}=$
18. $\quad 9.87^{2}=$
19. $\quad 11.89^{2}=$


Paper $\$ 4.95$ for 500 sheets


Comments:

## Homework / Assessment Worksheet

To be completed by:

## A: 10 Quick Questions

1. $(7+33) \times 7=$
2. What would 9 books at $\$ 7.65$ each cost? $\qquad$
3. How many days in 9.5 weeks?
4. How many metres in 8.7 km ?
5. Find $20 \%$ of 160 kg $\qquad$
6. Name this shape

7. Find the missing number \& $35 \times$ \& $=175$ $\qquad$
8. $\quad 5.62+0.087=$ .....................
9. $5.32 \times 0.06=$
10. Calculate $13^{2}=$

## D: Integers

Add and Subtract the following

1. $5+9=$
2. $-5+11=$
3. $11+-6=$
4. $-8+9=$
5. $12+-14=$
6. $0+10=$
7. $0+-14=$
8. $6+-6=$
9. $-7+12=$
10. $7+-13=$
11. $-6+11=$
12. $-4+-6=$
13. $-8-6=$
14. $-15-8=$
15. $8--11=$
16. $8--9=$
17. $7--8=$
18. $-9--9=$
19. $-10-7=$
20. $-12--9=$
21. $-15-7=$
22. $-5--9=$
23. $-9-15=$
24. $-9--5=$
25. $0-7=$
26. $-9--5=$

Comments:
$\qquad$

## $B$ : What is the new Temperature?

Calculate the new temperature.

1. $16^{\circ} \mathrm{C}$, then drops $7^{\circ} \mathrm{C}$ $\qquad$
2. $9^{\circ} \mathrm{C}$, then drops $11^{\circ} \mathrm{C}$
3. $8^{\circ} \mathrm{C}$, then rises $5^{\circ} \mathrm{C}$ $\qquad$
4. $-8^{\circ} \mathrm{C}$, then rises $9^{\circ} \mathrm{C}$ $\qquad$
5. $-4^{\circ} \mathrm{C}$, then drops $8^{\circ} \mathrm{C}$
6. $-6^{\circ} \mathrm{C}$, then drops $7^{\circ} \mathrm{C}$
$\qquad$
7. $0^{\circ} \mathrm{C}$, then rises $12^{\circ} \mathrm{C}$ $\qquad$
8. $0^{\circ} \mathrm{C}$, then drops $11^{\circ} \mathrm{C}$ $\qquad$
9. $-6^{\circ} \mathrm{C}$, then drops $5^{\circ} \mathrm{C}$ $\qquad$
10. $4^{\circ} \mathrm{C}$, then drops $11^{\circ} \mathrm{C}$

## E: Problem Solving

Use the numbers $1,2,3,4,5,6$, 7,8 , and 9 , to make a 3 by 3

## Magic Square.

Each number is to be used only once.


C: Am I Sick or Well? In our bodies there are good bugs - $^{-}$, and there are bad bugs © One good bug eats one bad bug.

1. If ()$\cdot()$ means +3 what does $O: O)$ mean? Study these bugs.

2. How many $(-)$ bugs? ...........
3. How many $\odot$ bugs? ............
4. Am I sick or well? ................

Use + , - , and = signs when answering the following:
5. Write a maths sentence to show how you could get your answer for question 4 above. (eg. ${ }^{+6+7=-1 \text { ) }) ~}$

F: Multiplication \& Division Squares
Complete these Multiplication and Division squares.


| $\times$ | +3 | +7 | -2 |  |
| :--- | :---: | :---: | :---: | :---: |
| +4 |  |  |  |  |
| -3 |  |  |  |  |
| +5 |  |  |  |  |
|  | $\div$ | -2 | +3 | -4 |
|  | +12 | +6 |  |  |
| -18 |  |  |  |  |
| +24 |  |  |  |  |



| $x$ | -4 | -9 | +8 |
| :---: | :---: | :---: | :---: |
| +7 |  |  |  |
| -5 |  |  |  |
| -6 |  |  |  |
| $\div$ | +4 | -6 | +12 |
| -12 |  |  |  |
| +36 |  |  |  |
| -60 |  |  |  |

Please sign:
Parent / Caregiver

A: 10 Quick Questions

1. $1.64 \times 1.2=$
2. $38.46 \div 0.2=$
3. How many metres in 565 centimetres?
4. $11^{2}+\sqrt{16}=$
5. Write 83000 in standard form
6. Name this shape

7. Find the next 2 numbers in the pattern $2,5,10,17$,
8. What type of triangle is this?
9. How many sides does a decagon have?
10. How many minutes in 6.25 hours?

## B: Writing Percentages?

Write the following as percentages.


1. 30 out of 60
2. 20 out of 80
3. 5 out of 15
4. 6 out of 18
5. 14 out of 21
6. 30 out of 50
7. 40 out of 50
8. 10 out of 50
9. 8 out of 200
10. 30 out of 40
11. 48 out of 60
12. 30 out of 30

C: What Percentage is it?
Calculate the following.

1. Cheryl got 38 out of 50 in a recent maths test. What percentage did she get? $\qquad$
2. James spent 8 hours asleep last night. What percentage is that of the whole day?
3. The school netball team won 18 games out of 20. What percentage did they lose?
4. What percentage of people watched a rugby test on T.V. if 4 out of 5 watched it on television?
5. Out of 50 pupils at school, 23 walk to school. What percentage is this?

## D: Using Percentages

Calculate the following.

1. Ranui bought birthday presents that were going to cost him \$75.00, but was given a $10 \%$ discount for cash. What did he pay for his presents? $\qquad$

2. A house in the street sold for $\$ 205000$. They had hoped to get $10 \%$ more for the house. What would it have sold for then?
3. A popular take-away bar recently increased its prices by $5 \%$. If a meal had cos $\dagger \$ 7.00$, what would the new price be?

4. A company offered a group discount of $20 \%$. If the normal price for swimming with the dolphins was $\$ 55.00$, what would be the discounted price?
5. In a book sale, all $\$ 18.00$ and $\$ 21.00$ books have been reduced in price by 40\%. What are the sale prices for these books?

6. GST is $12.5 \%$. What would the price be when GST is added to the cost of a new car worth $\$ 21,000$ ?

E: How do you spend your day?
Fill out the table of what you do during any school day. Round off the times to the nearest half hour. Calculate the percentage time you spend on each activity as listed.
(Does not have to add up to 24 hrs )

| $\\|\\|d\\|\\| d \\| d$ | Sleeping | Eating | School | TV | Sport |
| :---: | :--- | :--- | :--- | :--- | :---: |
| Hours <br> spent |  |  |  |  |  |
| $\%$ |  |  |  |  |  |


| A： | 10 Quick Questions |
| :---: | :---: |
| 1. | Find $25 \%$ of \＄60＝．．．．． |
| 2. | $0.36 \times 1.2=$ |
| 3. | How many minutes in 6.5 hours？ |
| 4. | How many kilometres in 5200 metres？ $\qquad$ |
| 5. | Write 0.6 as a percentage |
| 6. | How many sides does a pentagon have？ $\qquad$ |

7．Find the next number 2，7，12，17，
8．List the first 4 multiples of 14
9．Round off 0.594 to two decimal places
10．Calculate $2.5^{2}$

## C：Simplifying Ratios

Simplify these ratios by finding the missing numbers．


## B：Writing Ratios

Write the following as ratios（do not simplify）
1．There were 12 cats to every 15 dogs．
2．There was 1 teacher to every 23 pupils．
3．There were 17 patients to every nurse．
This table shows two Year 9 classes at a school．

| Class 9St |  | Class 9Wt |  |
| :---: | :---: | :---: | :---: |
| Boys | Girls | Boys | Girls |
| 17 | 14 | 15 | 16 |$\quad$| What is the ratio of |
| :--- |
| boys to girls in class |
| 3St？．．．．．．．．．．．．．．．．．．．．．．．．．．．．．．． |

5．What is the ratio of girls to boys in class $3 \mathrm{~W}+$ ？

## $D:$ Sharing in a given Ratio

1．Share $\$ 24$ in a ratio of $1: 2$

2．Share $\$ 54$ in a ratio of $1: 5$

3．Share 63 grams in a ratio of 4：5
4．Share 400 mls in a ratio of 5：3
5．Share $\$ 72$ in a ratio of 3：5：1

6．Share $\$ 80$ in a ratio of 2：3：5

## E：Word Problems

1．The ratio of teachers to pupils on a school trip should be 1 to 8 ． If there are 24 pupils going on the trip，how many teachers should go？
2．Jenny and Steven decided to share 64 lollies between themselves in a ratio of their ages．If
 Jenny is 9 and Steven is 7 ，how many lollies does each child get？
3． 120 tickets were sold for a concert．If the ratio of tickets sold to children and to adults was 9 to 1 ，how many children are going to the concert？ $\qquad$


4．In a class of 28 ，Miri was voted most popular by a $4: 3$ majority．How many votes did she get？

5．Jan has $\$ 180$ ．She buys some clothes，some books and some food in a ratio of $5: 2: 3$ ． How much did she spend on each item？ clothes $\qquad$ books $\qquad$ food

To be completed by:

A: 10 Quick Questions

1. $1.9+18+0.096=$
2. $24.9 \div 0.3=$
3. How many weeks in 59.5 days?
4. How many millimetres in 82 centimetres?
5. $7+2(29-3 \times 8)=$
6. How many years in two decades?
7. Find $20 \%$ of $\$ 43.50$
8. What would 7 items a $\dagger$ $\$ 7.65$ each cost?
9. How many minutes between 1:45 p.m. and $4: 25$ p.m., on the same day?
10. Calculate $0.9^{2}$

## D: Writing Fractions

What fraction in each design is shaded?

1.

2.


| B: Equivalent Fractions |  |
| :---: | :---: |
| Find the missing numbers to complete these equivalent fractions. |  |
|  |  |
| $1 / 2=4 / 12$ |  |
| 2. $2 / 3=\boldsymbol{/} / 18$ |  |
| 3. $3 / 4=1 / 60$ |  |
| 4. $3 / 11$ |  |
| 5. $3 / 7=9 / 35$ |  |
| 6. $3 / 5=\boldsymbol{V} / 5$ |  |
| 7. $4 /$ |  |
| 8. $3 / 8=4 / 48$ |  |
| 9. $6 / 7=\$ / 4$ |  |
| 10. $5 / 9=\Phi / 72$ |  |

Find the simplest equivalent fraction for these fractions.

1. $10 / 15$
2. $12 / 22$
3. $14 / 20$
4. $100 / 400$
5. $40 / 90$
6. $55 / 77$
7. $15 / 90$
8. $18 / 72$
9. $16 / 24$
10. $\quad 18 / 45$
11. $21 / 63$
12. $20 / 45$
13. 48/60


F: Converting Fractions
Convert these improper fractions to mixed numbers.


Change to improper fractions.

| 9. | [3/5 | = ...... |
| :---: | :---: | :---: |
| 10. | $71 / 2$ | = ...................... |
| 11. | $65 / 7$ | = ... |
| 12. | $8^{2 / 3}$ | = ... |
| 13. | 71/6 |  |
| 14. | $9^{3 / 5}$ | = ................... |
| 15. | 75/8 | = .................... |
| 16. | 65/12 | = .................... |

## Homework／Assessment Worksheet

A： 10 Quick Questions
1． $7.2-4.7+0.092=$
2． $43.2 \times 0.8=$
3．Shade $3 / 4$ of this design
4．How many millilitres in 6.7 litres？

5．Write 75 in Roman
Numerals $\qquad$
6． $7+-16=$
7．Find $75 \%$ of $\$ 48$
8．Divide $\$ 35$ in a ratio of 5：2
9．How many minutes between 7：35 am and 2：15 pm ，on the same day？ $\qquad$
10．How many sides does a nonagon have？

## C：What Fraction？

What fraction of each coloured square is in this grid？


2．曲
3.


A pile of 20 cubes is stacked in the corner of a room．There are 2 grey layers， 1 clear layer and 1 black layer of cubes．
4．What fraction of the pile is $\square$ ？
5．What fraction of the pile is［⿴囗
6．What fraction of the pile is

（Remember to count the ones you cannot see）


## B：Adding and Subtracting Fractions

Add or subtract these fractions，simplifying if possible．
1． $1 / 4+3 / 4=$ $\qquad$ 11． $1 / 4+2 / 3=$
2． $2 / 3+2 / 3$ $\qquad$ 12． $1 / 3+3 / 4$ $\qquad$
3． $2 / 4+3 / 4$ $\qquad$ 13． $3 / 4+4 / 5$ $\qquad$
$\qquad$
4． $7 / 11+8 / 11=$ $\qquad$ 14． $4 / 5+2 / 3=$ $\qquad$
5． $6 / 7+5 / 7=$ $\qquad$ 15． $54 / 5+2 \frac{1}{4}=$
16． $3 / 5-1 / 3=$ $\qquad$
6． $3 / 5-1 / 5=$ $\qquad$
－ $1 / 5-1 / 3$
17． $5 / 6-2 / 7=$ $\qquad$
18． $5 / 8-2 / 5=$ $\qquad$
19． $7^{2} / 5-4^{4} / 5=$ $\qquad$
20． $8^{1 / 4}-4^{2} / 3=$ $\qquad$
10． $7 / 11-5 / 11=\ldots \ldots \ldots \ldots \ldots \ldots$

## D：Word Problems

Give answers as fractions in their simplest form．
1．Amelia and Joseph share an apple．If Amelia eats $4 / 7$ how much does Joseph eat？ At a party for 20 school friends， 12 were girls and the rest were boys．What fraction were boys？
3．During the May holidays Mr．Chapman painted ${ }^{3} / 7$ of his house．In the August holidays he painted another $2 / 7$ of the house．How much of the house has been painted so far？
4．The＇All Blacks＇won 14 out of their last 20 games． What fraction of the games did they win？
5．In Year 10， 40 out of 200 students will receive a certificate for great results in their exams． What fraction of the year group is this？


6．Paul cuts two lengths of plastic pipe．If one length is $4 \frac{1}{2}$ metres and the other is $5 \frac{3}{4}$ metres，what is the total length of pipe he cut？
7．Mrs Jones has $6 \frac{1}{2}$ metres of material．If she makes a dress using $3 \frac{3}{4}$ metres，what length of material does she have left？


8．Three TV ads ran for $\frac{2}{3}$ of a minute，$\frac{3}{4}$ of a minute and $\frac{1}{2} a$ minute．Write the total ad time as a mixed number，then convert your answer to seconds． $\qquad$ seconds

## Homework / Assessment Worksheet Answers

## Worksheet 1

A:

1. 1820 2. 45.5 days
2. 1715
3. 60 months
4. 5202
5. 540 seconds
6. $\$ 48.23$
7. 13
8. 208 weeks 10. 34

B:
$C:$


1. 360
2. 326
3. 9
4. 25 5. 569
5. 551
6. 8
7. 702
8. 146
9. 237 11. 7
10. 23
11. 456 14. 1287
12. 11
13. 450
D:
14. 90 pieces of fruit 2. 73 cards 3. 686 matches 4. $\$ 32$ 5. $\$ 34$
15. 18 white jelly beans 7. 27 red jelly beans 8.99 blue jelly beans
16. Box A 10. 98 jelly beans 11. Box C 12. 382 jelly beans

## Worksheet 2

A:

1. 9545
2. 356
3. 12
4. $\$ 44.24$
5. 4 sides
6. ellipse or oval
7. 5724
8. 434
9. 411
10. 250 cm

## B:

1. $52,54,56,58,60,62$
2. $69,71,73,75 \quad$ 3. $11,22,33,44$
3. 42,49
, 56 5. 6 multiples
4. $2,3,5,7,11,13,17,19$
5. $17,19,23,29,31$
6. $1,2,3,4,6,12$
7. $1,2,4,7,14,28 \quad 10.1,2,3,4,6$, 9, 12, 18, 36

## G:

1. 14
2. 24
3. 19
4. 69
5. 47
6. 193
7. 8
8. 93
9. 27
10. 19
11. 135
12. 150
13. 147 14. 480 15. 720
14. 71
15. 19
16. 72
17. 90
18. 

19
21.
145
23. 36
24. 4 25. 156
26. 64
D:

1. 50 km
2. 40 cm
3. 45 tickets
4. 100 tickets
5. $\$ 135$
6. $\$ 260$
7. $\$ 200$
8. $\$ 180$
9. $\$ 205$
10. 6 tickets
11. 6 tickets
12. $\$ 10$ change 13. $\$ 25$ change

## Worksheet 3

A:

1. 11
2. 27 3. 10
3. 4 sides
4. $\$ 19.75$
5. 8500 m
6. hexagon
7. 210 minutes
8. $13,26,39$,

52 10. 1, 2, 7, 14
B:

1. 64
2. 169
3. 225
4. 484
5. 3600
6. 8100
7. 10000
8. 6
9. 7
10. 12
11. 14
12. 20
13. 25
14. 30

C:

1. $9.6 \times 10^{3}$
2. $3.7 \times 10^{4}$
3. $3.14 \times 10^{2}$
4. $7 \times 10^{-4}$
5. $5.7 \times 10^{-2}$
6. 48000
7. 138000000
8. 0.00636
9. 0.000042

D:
no answer supplied
E:

1. 30 2. 50 3. 120
2. 410
3. 90 6. 140
4. 3540
5. 200
6. 300
7. 900
8. 500
9. 1000
10. 3600
11. 6400
12. 6100

F:

1. 16.3
2. 17.9
3. 31.7
4. 192.3
5. 425.5
6. 193.0
7. 936.4
8. 420.0
9. 2.64
10. 9.12
11. 17.91
12. 183.88 13. 163.12
13. 427.35
14. 500.08
15. 638.00
G:
16. 40
17. 70
18. 40
19. 100
20. 60 6. 70
21. 600
22. 540
23. 480
24. 17
25. 380
$\begin{array}{llll}\text { 12. } 5400 & 13 . & 1900 & \text { 14. } 6400 \\ \text { 15. } 13000\end{array}$

## Worksheet 4

A:

1. 71
2. $\$ 44.98$
3. 112 days
4. 4500 m
5. 320000
6. pentagon
7. 68
8. $1,2,4,8,16,32$
9. 70
10. 8.4

B:

1. $\$ 7.00$
2. 40 kg
3. $\$ 36$
4. $\$ 2.25$
5. 64 cm
6. 42 kg
7. $\$ 15.00$
8. $\$ 270$
9. 9 m
10. \$96
G:
11. 1 2. $\frac{1}{10}$
12. $\frac{1}{4}$
13. $25 \%$
14. 0.3
15. $33 \frac{1}{3} \%$
16. . 5
17. $\frac{1}{2}$
18. . 6 .
19. $66 \frac{2}{3} \%$
20. $\frac{3}{4}$
21. $75 \%$

## D:

1. $52 \%$
2. 14 girls
3. $16 \mathrm{~m}^{2}$
4. 42 kg
5. 40 cats
6. 108 cars
7. 7 pupils
8. 3 games
9. 67 pupils 10. $\$ 8.03$

E:

1. $25 \%$
2. $80 \%$
3. $33 \frac{1}{3} \%$
4. $50 \%$
5. $75 \%$
6. $60 \%$
7. $20 \%$
8. $100 \%$
9. $40 \%$
10. $66 \frac{2}{3} \%$

## Worksheet 5

A:

1. 6
2. $\$ 65.10$
3. 960 mm
4. 3750 m
5. $\$ 8.40$
6. (isosceles) trapezium
7. 78
8. $1,2,4,5,8,10$,
20, 40
9. 8.3
10. 9

B:

1. 24
2. 200
3. 90
4. $20 \quad$ 5. $30 \quad$ 6. 120
5. 12
6. 500
7. 24
8. 30
9. 300
10. 80
11. 9 14. 29
12. 36
13. 100 17. 144 18. 400
14. $7 \quad 20.8 \quad 21.86$

C:

1. 78.03
2. 7.976
3. 53.32
4. 5.123 5. 32.658
5. 420.125 7. 22.14
6. 103.687

| 9. | 60.817 | $10 . ~$ | 25.85 | 11.22 .88 | 12.2 .376 | 13. | 0.06394 | 14. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | 2.48 15. $28.96 \quad 16.0 .1281$

17. 12.68
18. 50.3
19. 0
20. 0.7
21. 16
$\begin{array}{rrr}2.376 & 13 . & 0.06394 \\ 21 . & 370 & 22.9\end{array}$
D:
22. $\$ 5250$
23. $\$ 49.50$
24. $\$ 140$
25. $\$ 49.50$
26. $\$ 5489$
27. $\$ 1.65$
28. $\$ 74.25$
29. $\$ 198$
30. $\$ 99$ 10. $\$ 148.50$
31. $\$ 43750$ 12. 8 computers, $\$ 0.00$
32. $\$ 224.80$

## Worksheet 6

## A:

1. 280
2. $\$ 68.85$
3. 66.5 days
4. 8700 m
5. 32 kg
6. parallelogram
7. 5
8. 5.707
9. 0.3192
10. 169
B:
11. $9^{\circ} \mathrm{C}$
12. $2^{\circ} \mathrm{C}$
13. $13^{\circ} \mathrm{C}$
14. $1^{\circ} \mathrm{C}$
15. ${ }^{-12}{ }^{\circ} \mathrm{C}$
16. ${ }^{-13}{ }^{\circ} \mathrm{C}$
17. $12^{\circ} \mathrm{C}$
18. ${ }^{-11}{ }^{\circ} \mathrm{C}$
19. ${ }^{-11}{ }^{\circ} \mathrm{C}$
20. $7^{\circ} \mathrm{C}$
C:
21. 4
22. ${ }^{+15}$
23. -13
24. Well
25. ${ }^{+} 15+-13={ }^{+} 2$
D:
$\begin{array}{lllllllllllllllllll}\text { 1. } 14 & \text { 2. } 6 & 3.5 & 4.1 & 5 . & -2 & 6.10 & 7 . & -14 & 8 . & 0 & 9 . & 5 & 10 . & -6 & 11 . & 5 & 12 . & -10\end{array}$ $\begin{array}{lllll}\text { 13. }-14 & 14 . & -23 & \text { 15. } 19 & 16.17\end{array}$ 17. 15 18. 0 8. $\begin{array}{ccccccc}19 . & 20 . & -3 & 21 . & -8 & 22.4\end{array}$
26. $6 \quad 24.4 \quad 25.7 \quad 26.3$

E:

## F:

| 6 | 7 | 2 |
| :--- | :--- | :--- |
| 1 | 5 | 9 |
| 8 | 3 | 4 |

1. 

| $\times$ | +3 | ${ }^{+} 7$ | 2 |
| :---: | :---: | :---: | :---: |
| ${ }^{+} 4$ | ${ }^{+} 12$ | ${ }^{+} 28$ | 8 |
| 3 | 9 | -21 | ${ }^{+} 6$ |
| +5 | ${ }^{+} 15$ | +35 | 10 |
| $\div$ | 2 | ${ }^{+} 3$ | 4 |
| ${ }^{+12}$ | 6 | +4 | 3 |
| 18 | +9 | -6 | ${ }^{+} 4.5$ |
| ${ }^{+} 24$ | 12 | ${ }^{+} 8$ | 6 |

2. 

| $\times$ | 4 | 9 | ${ }^{+} 8$ |
| :---: | :---: | :---: | :---: |
| +7 | -28 | -63 | +56 |
| -5 | ${ }^{+} 20$ | ${ }^{+} 45$ | -40 |
| -6 | ${ }^{+} 24$ | +54 | 48 |
| $\div$ | ${ }^{+} 4$ | 6 | ${ }^{+} 12$ |
| -12 | -3 | ${ }^{+} 2$ | 1 |
| ${ }^{+} 36$ | ${ }^{+} 9$ | 6 | +3 |
| -60 | -15 | +10 | 5 |

## A：

1． 1.968
2． 192.3
3． 5.65 m
4． 125
5． $8.3 \times 10^{4}$
6．cube
7． 26,37
8．Right angled，scalene
9． 10 sides 10.375 minutes
B：
1． $50 \%$
2． $25 \%$
3． $33 \frac{1}{3} \%$ 4． $33 \frac{1}{3} \%$
5． $66 \frac{2}{3} \%$
6． $60 \%$
7． $80 \%$
8． $20 \%$
9． $4 \%$
10． $75 \%$
11． $80 \%$
12．100\％
C：
1． $76 \%$
2． $33 \frac{1}{3} \%$
3． $10 \%$
4． $80 \%$
5． $46 \%$
D：
1．$\$ 67.50$
2．$\$ 225,500$
3．$\$ 7.35$
4．$\$ 44.00$
5．$\$ 10.80$ \＆$\$ 12.60$
6．$\$ 23,625$

## Worksheet 8

## A：

1．$\$ 15$ 2． 0.432
3． 390 minutes
4． 5.2 km
5． $60 \%$
6． 5 sides
7． 22
8． $14,28,42,56$
9． 0.59 10． 6.25

B：
1． $12: 15$
2． $1: 23$
3． $17: 1$
4． $17: 14$
5． $16: 15$

C：
1． $9 \quad$ 2． 12 3． 3 4． $8 \quad 5.5$
6． 5 7． 1
8． 5 9． 15 10． 2
11． $3: 5$
12． $8: 3$
$\begin{array}{lllllllll}\text { 13．} 7: 10 & 14.3: 5 & \text { 15．} 9: 5 & \text { 16．} 12: 5 & \text { 17．} 3: 1 & 18.3: 5 & 19.3: 7: 10 & 20.2: 5: 8\end{array}$
21．5：2：8 22．5：3：1

## D：

1．$\$ 8, \$ 16$
2．$\$ 9, \$ 45$
3． $28 \mathrm{~g}, 35 \mathrm{~g}$
4． $250 \mathrm{~mL}, 150 \mathrm{~mL}$
5．$\$ 24, \$ 40, \$ 8$
6．$\$ 16, \$ 24, \$ 40$

E：
1． 3 teachers
2．Jenny 36，Steven 28
3． 108 children
4． 16 votes
5．$\$ 90, \$ 36, \$ 54$

F：
7：13

## Worksheet 9

## A：

1． 19.996
2． 83
3． $8 \frac{1}{2}$ weeks
4． 820 mm
5． 17
6． 20 years
7．$\$ 8.70$
8．$\$ 53.55$
9． 160 minutes 10． 0.81

B：
1． 6
2． 12
3． 45
4． 12
5． 15
6． 30
7． 48
8． 18
9． 36
10． 40

## C：

1. 
2. 
3. 
4. 
5. 



3． $1 / 3$ or $3 / 9$
4．${ }^{1} / 2$ or ${ }^{5} / 10$
5． $3 / 5$
6．${ }^{4} / 11$

## E：

1．${ }^{2} / 3$
2．${ }^{6} / 11$
3．${ }^{7} / 10$
4． $1 / 4$
5． $4 / 9$
6． $5 / 7$
7． $1 / 6$
8．${ }^{1 / 4}$
9．${ }^{2} / 3$
10． $2 / 5$

11． $1 / 3$
12． $4 / 9 \quad$ 13． $4 / 5$
F：
1． $3^{2} / 5$
2． $4 \frac{3}{4}$
3． $5^{3} / 5$
4． $10^{1} / 6$
5． $10{ }^{5} / 7$
6． $6 \frac{5}{8}$
7． $95 / 9$
8． $5 / 12$
9．${ }^{28} / 5$ 10．${ }^{15} / 2$
11．${ }^{47} / 7$
12．${ }^{26} / 3$
13．${ }^{43} / 6$
14． $48 / 5$
15．${ }^{61} / 8$
16．${ }^{77} / 12$

## Worksheet 10

A:

1. 2.592
2. 34.56

3. 6700 mL
4. LXXV
5. 9
6. $\$ 36$
7. $\$ 25: \$ 10$
8. 400 minutes 10.9 sides

B:

1. 1
2. $1^{1 / 3}$
3. $1^{1 / 4}$
4. $1^{4} / 11$
5. $1^{4 / 7}$
6. ${ }^{2 / 5} \quad$ 7. $1 / 4$
7. $1 / 3$
8. $2 / 3$
9. $2 / 11$
10. $11 / 12$
11. $1^{1 / 12}$
12. $1^{11 / 20}$
13. $1^{7 / 15}$
14. $8^{1 / 20}$
15. $4 / 15 \quad 17 .{ }^{23 / 42}$
16. $9 / 40$
17. $2^{3 / 5}$
18. $3^{7} / 12$
G:
19. $12 / 25$
20. $8 / 25$
21. $5 / 25$ or $1 / 5$
22. $6 / 20$ or $3 / 10$
23. $13 / 20$
24. $1 / 20$

## $D:$

1. $3 / 7$
2. $8 / 20$ or $2 / 5$
3. $5 / 7$
4. ${ }^{14} / 20$ or $7 / 10$
5. $40 / 200$ or $1 / 5$
6. $10^{1} / 4 \mathrm{~m}$
7. $2^{3} / 4 \mathrm{~m}$
8. $2^{1 / 12}=$ 125 seconds

Tracking Sheet: 'In-class' Activity Sheets


Tracking Sheet: Homework / Assessment Worksheets



[^0]:    Note:
    The codes MP1, MP2, etc. have been created by numbering the Mathematical Processes Achievement Objectives in order as listed in the MATHEMATICS in the New Zealand Curriculum document. The numbering gaps occur as not all objectives are covered at Level 5. [REFER

[^1]:    Comments:

