A Complete Guide to ...



Utilising the objectives as written in

MATHEMATICS in the New Zealand CURRICULUM

for

Level 4

This resource contains:

- ☑ Table of contents
- ☑ Teaching notes
- ☑ In class activity sheets involving
 - worked examples
 - basic skills
 - word problems
 - problem solving
 - group work

☑ Homework / Assessment activity sheets

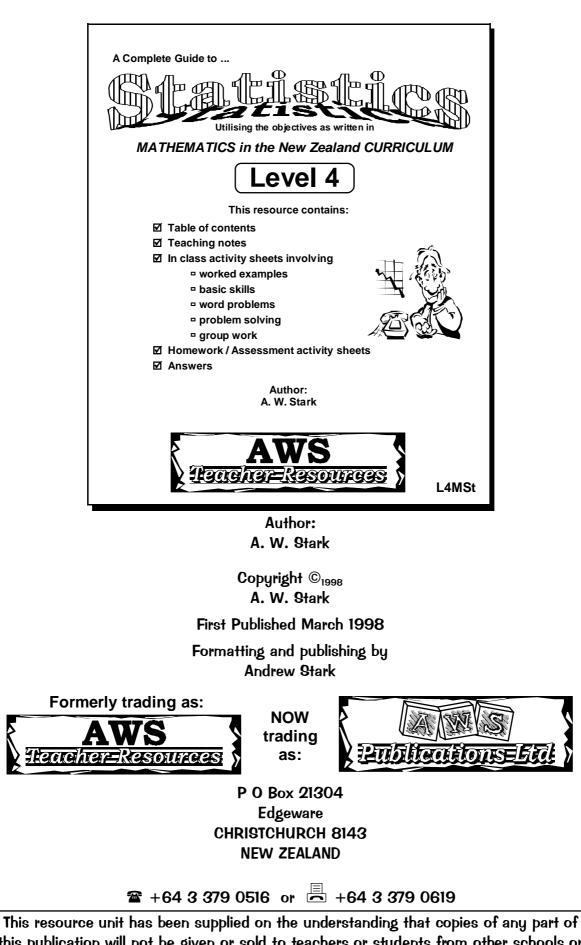


These resources are supplied as PHOTOCOPY MASTERS

Author: A. W. Stark



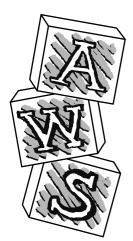




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Note from the author:



This resource ...

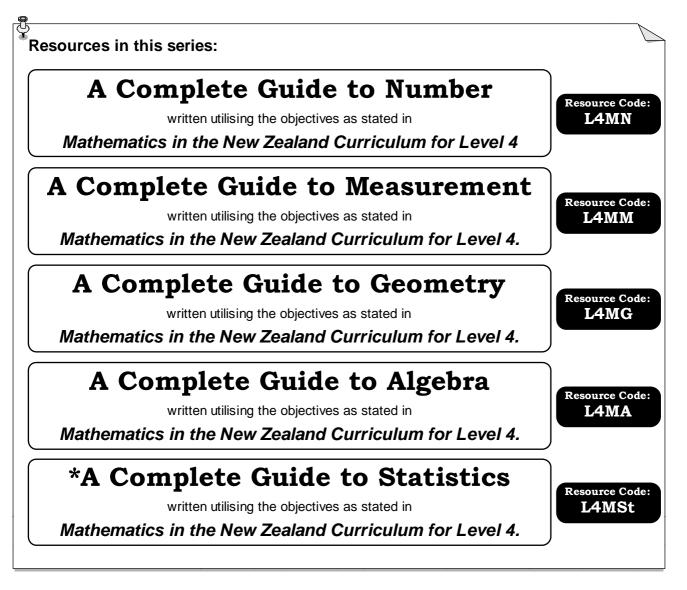
***A Complete Guide to Statistics**

is one of a series of FIVE resources written utilising the objectives as stated in

Mathematics in the New Zealand Curriculum for Level 4.

With my experiences as a specialist mathematics teacher, I enjoyed mathematics as a subject, but I am aware that not all teachers feel the same way about mathematics. It can be a difficult subject to teach, especially if you are unsure of the content or curriculum and if resources are limited.

This series of resources has been written with you in mind. I am sure you will find this resource easy to use and of benefit to you and your class.



For more information about these and other resources, please contact ...



Acknowledgement:

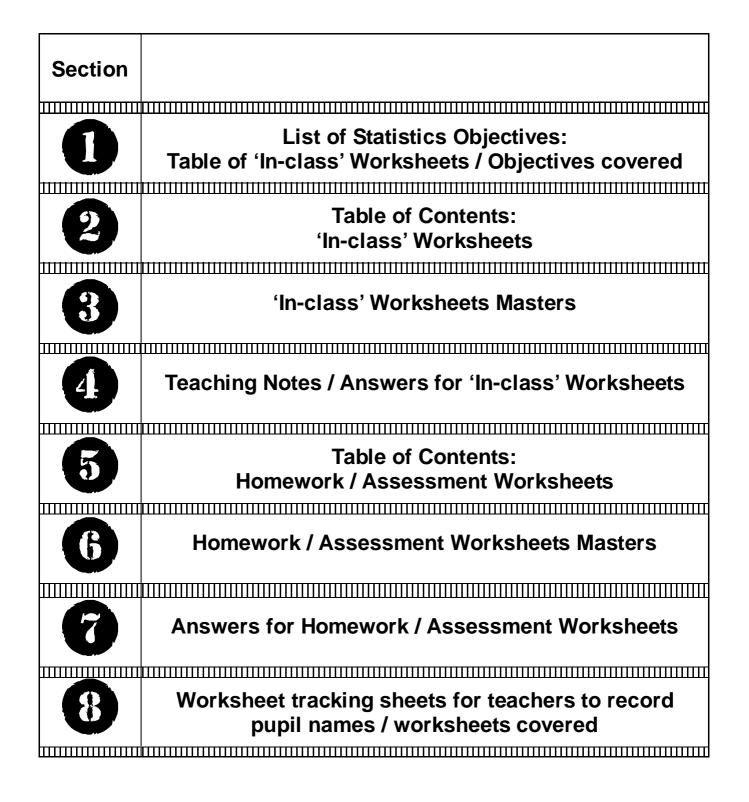
I would like to thank the staff and pupils of **Mairehau Primary School, Christchurch** for their assistance in making these resources possible.

This resource has been divided into EIGHT sections as listed below.

Although there are no page numbers, the sections follow in sequential order as listed.

Note: 'In-class' Worksheets Masters are lesson by lesson reuseable worksheets that can be photocopied or copied on to an OHP.

Homework / **Assessment Worksheets Masters** can be used as homework to reinforce work covered in class or they can be used for pupil assessment.





Statistics

The following are the objectives for Statistics, Level 4, as written in the

MATHEMATICS in the New Zealand Curriculum document, first published 1992. [REFER PAGE 142] Statistical investigations

Within a range of meaningful contexts, students should be able to:

- S1 plan a statistical investigation arising from the consideration of an issue or an experiment of interest;
- **S2** collect appropriate data;
- **S3** choose and construct quality data displays (frequency tables, bar charts and histograms) to communicate significant features in measurement data;
- **S4** collect and display time-series data.

Interpreting statistical reports

Within a range of meaningful contexts, students should be able to:

- **S5** report the distinctive features (outiers, cluster and shape of data distribution) of data displays;
- **S6** evaluate others' interpretations of data displays;
- **S7** make statements about implications and possible actions consistent with the results of a statistical investigation.

Exploring probability

Within a range of meaningful contexts, students should be able to:

- **S8** estimate the relative frequencies of events and mark them on a scale;
- **S9** find all possible outcomes for a sequence of events, using tree diagrams.

At the top of each '**In-class' worksheet** and **Homework / Assessment worksheet**, the Statistics objective(s) being covered has been indicated. *ExAMPLE:* **S1** means objective 1, **S2** means objective 2, etc.



The Mathematical Processes Skills:

Problem Solving, Developing Logic & Reasoning, Communicating Mathematical Ideas,

are learned and assessed within the context of the more specific knowledge and skills of number, measurement, geometry, algebra and statistics. The following are the **Mathematical Processes Objectives** for **Level 4**.

Problem Solving Achievement Objectives [Refer page 24]

- MP1 pose questions for mathematical exploration;
- MP2 effectively plan mathematical exploration;
- MP3 devise and use problem-solving strategies to explore situations mathematically;
- MP4 find, and use with justification, a mathematical model as a problem-solving strategy;
- **MP6** use equipment appropriately when exploring mathematical ideas.

Developing Logic and Reasoning Achievement Objectives [Refer page 26]

- MP8 classify objects, numbers and ideas;
- MP9 interpret information and results in context;
- MP10 make conjectures in a mathematical context;
- MP15 use words and symbols to describe and generalise patterns.

Communicating Mathematical Ideas Achievement Objectives [Refer page 28]

- MP16 use their own language and mathematical language and diagrams to explain mathematical ideas;
- MP17 devise and follow a set of instructions to carry out a mathematical activity;
- **MP20** record information in ways that are helpful for drawing conclusions and making generalisations;
- MP21 report the results of mathematical explorations concisely and coherently.

Note:

The codes MP1, MP2, etc. have been created by numbering the Mathematical Processes Achievement Objectives in order as listed in the MATHEMATICS in the NewZealand Curriculum document. The numbering gaps occur as not all objectives are covered at Level 4. [REFER TO PAGES 23 - 29 OF THE CURRICULUM DOCUMENT]

'In-class' Statistics Worksheets Table of Worksheet Number / Objectives Covered

See the opposite page for details of each objective.

		Sta	atis	tic	s O	bje	cti	ves			M	ath	ema	tica	al P	roce	esse	es O	bjec	ctiv	es	
Worksheet Number	S	S	S	S	S	S	S	S	S	MP			MP									
1	1 ★	2	3	4	5	6	7	8	9	1 ★	2 ★	3 ★	4	6	8	9 ★	10 ★	15	16	17	20	21
2	*									*	*	*				*						
3	•••	*								*	•••	•••				*			*		*	
4		*								*	*					*			*		*	
5		*	*							••	*					*	*		*		*	
6		*	*								*					*	•••		*		*	
7		*	*								*			*		*			*	*	*	
8		•••	*							*	*					*			*		*	
9			*							*	*					*			*		*	
10			*							*	*					*			*		*	
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12			*							*	*					*			*		*	
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18					×					*		*				*				*		
19						×				*		×				×	×			*		×
20							×			×	×	×				×	×		×	×	×	×
21								×				×				×						
22								×		×		×				×			×		×	
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24									×	×		×				×	×				×	
25									×	×	*	*				*	*		×		*	

Table of Contents for the 'In-class' Worksheet Masters for Statistics, Level 4

Worksheet Number	Торіс	Statistics Objective(s)
1	Introduction to statistical investigations	S1
2	Designing a questionnaire	S1
3	Collecting and organising discrete data using a frequency table	S2
4	Organising grouped discrete data	S2
5	Displaying ungrouped discrete data as a column graph	S2 / S3
6	Displaying grouped discrete data as a histogram	S2 / S3
7	Collecting and organising continuous data using a frequency table	S2 / S3
8	Creating stem and leaf graphs	S3
9	Creating pictograms	S3
10	Creating dot plot graphs	S3
11	Creating strip graphs / percentage bar graphs	S3
12	Understanding pie graphs	S3
13	Creating pie graphs using a protractor	S3
14	Creating time-series data	S4
15	Calculating the mean (average score)	S5
16	Calculating the median (middle score)	S5
17	Finding the mode (most common score)	S5
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24	Finding outcomes using tree diagrams	S9
25	Using probability to predict outcomes	S9
	Teaching Notes / Answers	



Introduction to statistical investigations:

If a crime is committed, the police will do an investigation, by asking questions of the people involved, to find out what happened. In a **statistical investigation** questions will also be asked and i**nformation** or **data** collected.

Example: "50% of the pupils at Carrington School bike to school", stated Kate.

Discuss how Kate could have collected this information, to be able to make this statement. What questions would she have asked? Who would she have asked?

Task 1

Before conducting a statistical investigation, there are some **important statistical words** that need to be understood. **Copy** and **complete** sentences 1 to 7 by adding a **statistical word** from the list below.

rar	idom popul	ation bio	used sample	questionnaire	representative sample	survey		
1.			•	•	hool is called a			
2.	. Ais part of the population we are interested in.							
3.								
4.	For the result	ts of a survey	y to apply to that	population, the sam	nple must be a			
5.	A sample that	is not a repi	resentative sampl	e is called a	sample.			
6.	Α	sample	means that every	y person, or item, h	as an equal chance of being	chosen.		
7.								
8.	List 5 examples of populations , remembering that a population does not have to be people. <i>Example:</i> The trees in the school playground.							
9.	•	•	tion 8, name a sa 2 metres tall.	mple of each populo	ation that could be surveyed	d.		
10.	Why is it some	etimes easie	r to survey a sam	ple of a population,	rather than the whole pop	ulation?		
	-		•	girls. Only 10% of ite televison progra				
11.	• •		any girls should b I tive sample of th	e surveyed so that his population?	those pupils			
	•	•		rrington School, th is going to be char	iere are 8 teachers, 1 princ iged.	ipal, 2		
40	T (. .							

- 12. If only the teachers were asked about the uniform changes, why is this a biased sample?
- 13. Who should be asked about possible uniform changes, so that the opinions are not biased?
- 14. List 3 ways a random sample of the 180 Carrington School pupils could be selected.

Task 2

Working in a small group, decide on 5 important issues that you could investigate.

Points to consider when carrying out an investigation:

- A: Decide on the purpose of your investigation.
- **B:** Decide what data needs to be collected and how it is going to be collected.
- C: Collect and organise the data.
- D: Interpret the data and draw conclusions from it.
- E: Write a report based on your investigation.

Discuss how you are going to complete the first 3 points above. Compare your methods with other groups.



Was that 5 or 7



Designing a questionnaire:

A questionnaire is used when we are asking opinions about an issue.

The **design** of a questionnaire, that is, the way the questions are worded, the way the answers are to be given and the overall look or layout of the questionnaire is most important.

Some points to consider about designing a good questionnaire would be ...

- ☑ What questions relating to the 'issue/s' are you going to ask?
- ☑ Do not ask questions that are not important to the issue.
- Make the questions clear and concise and not too many of them.
- ☑ How are these questions going to be answered? Example: multi-choice, single words, short answers or long answers.
- ☑ Have you allowed for every possible answer?
- Do you need to give instructions as to how the questionnaire has to be filled out?
- I How are you going to organise and display the data you have collected?

Discuss other points that might be important when designing a questionnaire.

Task 3

A new teacher in Room 10 wanted to know more about the pupils in his class.

He asked pupils to answer the questions below, which require only 'Yes' or 'No' answers. **Record** your answers to these questions.

- 1. Were you born in New Zealand? 2. Have you lived in New Zealand all your life? 3.
 - Can you speak more than one language? 4. Do you enjoy mathematics?

5. Make up 5 more 'Yes' or 'No' questions that the teacher might ask.

He then asked some more questions that required answers other than 'Yes' or 'No'. Record your answers to these questions.

- 6. How old are you? 7. In which month is your birthday?
- What is your favourite T.V. programme? 9. 8. What is your favourite sport?

For some questions, being given a choice of answers is a good idea. Record your answers to these questions.

How do you travel to school? 10.

walk	bike	bus	car	other

How far do you travel to school? 11.

less than	1 km to	2 km to	more than
1 km	2 km	3 km	3 km

Make up 5 more questions that cannot be answered by 'Yes' or 'No' answers. 12. Supply a choice of answers for your questions.

Task 4

Working in a small group, choose one of the issues you discussed in Task 2, Worksheet 1.

Who are you going to survey to gain opinions or ideas about the issue you are investigating?

Design a questionnaire for your sample population to fill out. How are you going to get them to fill it out?

Include questions in your questionnaire that require a 'Yes' / 'No' answer, some word answers and / or answers where the choices are given.

Discuss how the data collected could be organised and presented.





Collecting and organising discrete data using a frequency table:

There are **two types** of data that can be collected, **discrete** data and **continuous** data. A **frequency table** (tally chart) is a good way to organise both types of data as the data is being collected.

Discrete data is data that is obtained by counting.

Example: John records the number of people in cars as the cars go past the school gate.

Example: This frequency table shows the results of John's

	Number of people	Tally	Frequency
S	1		10
	2	₩ T III	8
	3		4
			22

How many cars had only one person?

Answer: 10 cars.

survey.

What other information is contained within this frequency table?

Continuous (measurement) data is obtained by measuring and will be looked at in Task 11, Worksheet 7. Example: Amanda measured the height of her younger sister every week.

> 2, 1

Task 5

The following data shows the number of spelling mistakes that pupils in Room 10 made in a spelling test of 20 words.

- 1. Copy and complete the frequency table.
- 2. What was the most common number of mistakes made?
- 3. How many pupils sat the spelling test?

Number of spelling mistakes	Tally	Frequency
0		
1		
2		
3		
4		

The total of the **frequency**

Answer: There were 22 cars

in John's survey.

What does this tell us?

column is 22.

Pupils in Room 9 were surveyed to find out how they travelled to school and how far away from school they lived (measured to the nearest km). Below are the results of the survey.

walk 1km, bike 2km, car 5km, walk 2km, bike 3km, bus 7km, bus 5km, walk 1km, bike 2km, car 6km, walk, 2km, bike 3km, walk 1km, bus 4km, walk 2km, bike 2km, walk 1km, walk 1km, bike 3km, walk 2km, bus 6km, car 4 km, walk 2km, bike 3km, walk 1km, bike 5km, walk 2km, bus 6km, car 5km, bike 2km, walk 1km, bike 3km, walk 1km

Organise the results of this survey into two frequency tables.

How many pupils in Room 9?

Study the results in both frequency tables, then write a statement about the 'average' Room 9 pupil - how he/she travels to school and how far she/he has to travel.

7. **Conduct** a similar survey of the pupils of your class and organise and display your results in two frequency tables.



Task 6

Look at the questions in the questionnaire you created in Task 4, Worksheet 2.

For some of your questions, using a **frequency table** may be a good way to collect and organise the data. **Create frequency tables** for those questions, then **collect** the **data** using your frequency tables.



Organising grouped discrete data:

To avoid having too many rows in a frequency table, the data can be grouped into categories or class intervals. Usually 6 to 7 class intervals is the maximum number to have in any one frequency table.

Each category or class interval should be the same width.

Example: The number of toys sold each hour at a local toy shop has been recorded in this frequency table.

Which numbers would be recorded in the class interval 6 - 10?

How many times were less than 11 toys sold in an hour?

Answers: The numbers 6, 7, 8, 9 and 10 would go in the 6 - 10 class interval.

On 16 occasions, less than 11 toys were sold in an hour.

What other information is contained within this frequency table?

Task 7

The following data shows the number of Lego blocks used to create some models made by pupils in Room 7.

12,	26,	31,	28,	25,	19,	14,	
11,	21,	29,	30,	24,	16,	18,	
23,	14,	13,	31,	22,	29,	20,	
23,	17,	12,	23,	29,	21,	34	
							_

- 1. Copy and complete the frequency table, recording the numbers in the appropriate class interval.
- 2. What was the most common class interval?
- 3. How many pupils used less than 21 blocks in their models?
- 4. How many pupils used more than 25 blocks?
- How many pupils in Room 7? 5.

This data shows the points scored by the pupils in Room 8 in a school speech competition, entitled 'A famous person I admire'.



-				,
15,	21,	18,	22, `	6.
29,	30,	18,	16,	
23,	29,	24,	11,	
19,	17,	22,	17,	7
11,	27,	26,	21,	7.
23,	19,	18,	14	8.
\square				9.

Organise this data in a frequency table using the class intervals 11 - 15, 16 - 20, 21 - 25 and 26 - 30.

What was the top mark in the speech competition?

- How many pupils scored more than 20?
- How many pupils entered the competition?

This data shows the number of trees planted in the gardens of houses along one street.

12.



5, 12,	8, 18,	9,
	9, 12,	
	3, 11, 3 4, 12, 3	
	12, 17,	
8, 15,	, 9, 17,	, 9

10.	Organise this data in a frequency table
	using 4 class intervals.
11.	What was the most common class interv

- What was the most common class interval?
- How many gardens had less than 11 trees?
- How many gardens had more than 10 trees? 13.
- 14. How many houses were surveyed?

Ĵ	
	S P

Number of toys sold each hour				
Class Interval	Tally	Frequency		
1 - 5	HH II	7		
6 - 10	##* IIII	9		
11 - 15	₩¥ III	8		
16 - 20	₩	5		
21 - 25	I	1		
		30		

Number of Lego blocks used			
Tally	Frequency		





Displaying ungrouped discrete data as a column graph:

Number of

1.

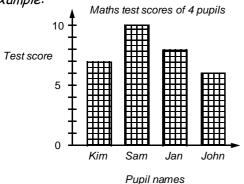
2.

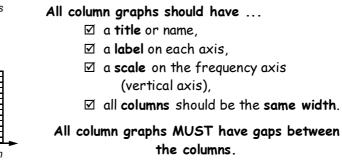
3.

4.

5.

Ungrouped discrete data, organised using a frequency table, can be displayed as a column graph. Example:







What other information is contained within this column graph?

Task 8

This frequency table shows the goals scor

by 5 players in Western Soccer Club during one season.

red	Name	goals scored
	Simon	7
	Mark	3
	Steven	9
	Rangi	5
	David	8

Plaver's

- Create a column graph to display these results.
- Who scored the most number of goals?
- How many goals did Rangi score?
- Who scored 3 goals?

How many goals did these 5 Western Soccer Club players score in this season?

Michelle asked pupils in her class three questions:



How many brothers and / or sisters do you have? In which month of the year is your birthday? If you had to make a choice between having a cat or a dog as a pet, which pet would you choose?



Below are the results of her survey, in the order the questions were asked.

How could Michelle improve the way she recorded this data? 6.

2, September, cat	3, March, dog	1, January, cat	2, September, cat	0, May, dog	4, September, cat
3, June, cat	2, September, cat	1, August, dog	3, July, cat	4, March, cat	2, March, dog
2, December, dog	1, June, cat	0, March, cat	2, October, cat	0, May, cat	1, April, cat
2, August, dog	3, February, cat	2, November, cat	3, January, dog	2, July, cat	3, September, dog
2, October, dog	1, April, cat	2, August, dog	4, December, dog	2, May, cat	0, April, dog

- 7. Reorganise Michelle's survey results into 3 frequency tables.
- 8. Draw 3 column graphs to display these results.
- 9. Write several statements about the pupils in Michelle's class, based on the data Michelle collected.



Task 9

Create column graphs from the frequency tables created in Task 5, guestions 1 and 4, Worksheet 3.

Look back at the frequency tables you used to collect and organise data from your questionnaire. Create column graphs from the frequency tables you created in Task 6, Worksheet 3 (if appropriate).





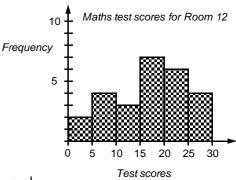
Displaying grouped discrete data as a histogram:

Grouped discrete data, organised using a frequency table with class intervals, can be displayed as a **histogram**. A histogram is like a column graph without the gaps.

Continuous (measurement) **data** can also be displayed as a **histogram** (See **Task 11**, **Worksheet 7**). *Example:* The results of a class test are shown in this **frequency table** and drawn as a **histogram**.

Test scores	Frequency	
0 - 4	2	ł
5 - 9	4	ł
10 - 14	3	1
15 - 19	7	
20 - 24	6	ć
25 - 30	4	
	26	

How many pupils scored between 10 and 14 marks in the test? How many pupils got exactly 23 in the test?



Answers: 3 pupils scored. It is impossible to tell if any pupils scored exactly 23. We can only say that 6 pupils scored between 20 - 24.

All histograms should have ...

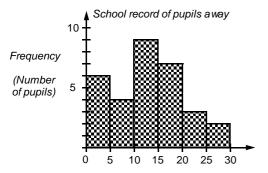
- \square a title or name, \square a label on each axis,
- \square class intervals that have the same interval,
- \square a **scale** on each axis,
- \square all columns should be the same width.

A histogram DOES NOT have gaps between the columns.

Task 10

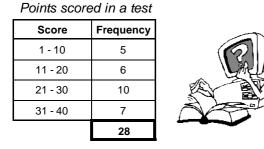
Every school has to keep a record of pupils who are absent from school.

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Number of days away from school

5. Draw a histogram from the grouped data contained in this frequency table.



This **histogram** shows the number of days pupils were away from school in one year, for a small country school.

- 1. How many pupils were away for less than 5 days?
- How many pupils were away for more than 9 days but less than 15?
- 3. Which class interval shows that 9 pupils were away?
 - How many pupils were away for more than 20 days?
 - 6. **Organise** this data into a frequency table using 4 class intervals of 10.

Points scored by Room 8 pupils in a speech competition

21, 35, 20, 40, 19, 41, 32, 28, 33, 24,	
27, 17, 49, 23, 24, 47, 36, 24, 22, 37,	
11, 24, 29, 45, 37, 20, 36, 17, 45, 29	

- 7. **Draw** a histogram to display these results.
- 8. What were the top and bottom scores?
- 9. Which class interval was the most common?
- 10. Collect some grouped discrete data of your own and draw histograms to display your data.

4.



Collecting and organising continuous data using a frequency table:

The second type of data that can be collected is called continuous data.

Continuous data is obtained by measuring. Because continuous data can take on any value, it is recorded in frequency tables that have **class intervals**, similar to frequency tables for grouped discrete data.

Example: The height of pupils in Room 8 are shown in this frequency table.

What range of heights would appear in the class interval 1.40m - 2

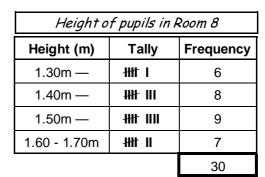
Answer: Any heights ranging from 1.40m to 1.499m, that is, just below 1.50m.

Although we know that 8 pupils were in the class interval 1.40m —, we do not know their exact heights.

Task 11

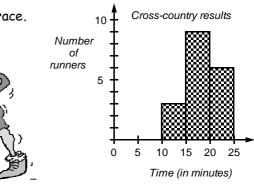
This **histogram** shows the results of a school cross-country race.

- 1. How many runners ran the course in under 15 minutes?
- 2. How many runners took longer than 20 minutes to run the race?
- 3. How many runners ran the race?





What other information is contained within this frequency table?



Each year there is a salmon fishing competition at the Rakaia river. The data below shows the weight of each fish caught during the competition.



 Fish weights for the Rakaia Salmon Competition (kg)

 2.5, 1.8, 3.1, 2.7, 2.4, 1.6, 5.1, 4.6, 2.9,

 3.7, 4.1, 3.0, 2.9, 1.7, 3.6, 2.1, 4.9, 5.3,

 3.7, 4.2, 5.7, 1.9, 5.8, 4.7, 3.4, 2.1, 3.9,

 3.8, 4.6, 1.7, 2.6, 3.2, 1.9, 4.3, 3.7, 1.2

- 6. What was the heaviest fish in the competition? 7.
- 8. How many fish were caught in this competition? 9.
- 4. Organise this data into a frequency table with class intervals 1.0kg -, 2.0kg -, 3.0kg -, 4.0kg and 5.0kg 6.0kg.
- 5. **Draw** a **histogram** to display this information.

How many fish were lighter than 4.0kg? How many fish were heavier than 5.0kg?

Task 12

Collect some **continuous** (measurement) data of your own, recording the data in a frequency table. **Decide** on no more than 7 appropriate **class intervals** for each set of data you collect.

Example: The height of pupils in your class.

The weight of various sizes of apples, fruit or vegetables. The volume of water various containers will hold ... etc.

Try to obtain at least 20 measurements for each set of data.

Draw histograms to display your results.





Creating stem and leaf graphs:

Just as tally charts and frequency tables can be used to record data as it is being collected, so too can a **stem and leaf graph** be used this way.

Example: Pupils in Martin's class were asked the day of the month that their birthdays were on. As they called out the dates, Martin recorded the dates using a stem and leaf graph.

Birthday dates for pupils in Martin's class

The numbers 0, 1, 2 and 3 written between the parallel lines, form the **stem** part of the graph. 0 8, 9, 4, 3, 1, 7 1 9, 8, 2, 0, 6, 7, 6 2 8, 4, 3, 1, 6, 7, 2, 0 3 0, 1, 0, 1

The numbers outside the parallel lines form the **leaf** part of the graph. **Leaf numbers** are usually written as single digits.



1.

The first row of numbers shown by this graph are 8, 9, 4, 3, 1 and 7. The fourth row of numbers are 30, 31, 30 and 31.

List the numbers that are in the 20's. Answer: 28, 24, 23, 21, 26, 27, 22 and 20.

A **back-to-back** stem and leaf graph has '**leaf**' numbers on both sides of the '**stem**' numbers. This type of graph can be used when comparing two sets of scores.

Task 13

List the numbers that are represented in these stem & leaf graphs, then answer the questions below.

 Test results for Room 9 pupils

 4
 4, 1, 5, 9, 5, 0

 5
 0, 2, 8, 7, 2, 9, 1

 6
 2, 5, 1, 8, 7, 1, 6, 1

 7
 8, 2, 3, 7

4. 5.

6.

 Cost of buying lunch (\$)
 3.

 0
 8, 9, 7, 6

 1
 5, 3, 9, 1, 3, 8, 0, 8

 2
 9, 0, 3, 4, 5, 7, 3

 3
 1, 0, 4, 5

	e taken to run a race (seconds)
10	4, 8, 9
11	1, 5, 7, 8, 9
12	1, 2, 2, 6, 7, 8, 9
13	3, 4, 5, 7, 9, 9
13	4, 8, 9 1, 5, 7, 8, 9 1, 2, 2, 6, 7, 8, 9 3, 4, 5, 7, 9, 9



How many pupils sat the test in Room 9?

2.

What were the most expensive and the least expensive lunches bought?

Convert the fastest and slowest times for this race into minutes / seconds.



Pupils in Room 10 had their heights measured in metres. The results are shown in Box A.



 Box A
 7.

 1.35, 1.27, 1.41, 1.19, 1.23,
 1.34, 1.37, 1.27, 1.26, 1.29,

 1.46, 1.15, 1.37, 1.42, 1.37,
 8.

 1.32, 1.29, 1.43, 1.21, 1.19
 9.

- **Create** a stem & leaf graph, using the numbers 1.1, 1.2, 1.3 and 1.4 as the stem numbers, to display these results. What were the tallest and shortest heights?
- How many pupils were measured?

Pupils in Room 7 sat an English test and a Mathematics test. Both tests were marked out of 50. The results are shown below.

10. Organise this data as a back-to-back stem & leaf graph.

English test results

Í	45, 32, 9, 13, 26, 45, 37, 15, 50, 38, 31, 27, 8, 14, 49, 41, 30, 29, 19, 17, 22, 9, 27, 25, 44, 28	Ì	35, 17, 50, 44, 25, 47, 38, 39, 21, 50, 0, 22, 40, 20, 24, 8, 20
I	30, 31, 27, 0, 14, 49, 41, 30, 29,		ZI, 50, 9, ZZ, 49, 50, Z4, 6, Z0,
Į	19, 17, 22, 9, 27, 25, 44, 28		23, 45, 49, 31, 32, 47, 35, 43, 50

Mathematics test results



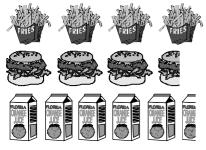
- 11. Look at the stem & leaf graph you have created and comment about the results of the two tests.
- 12. Collect your own data and present your data as stem & leaf graphs.



Creating pictograms:

Discrete data that has been collected using frequency tables can be represented as pictograms. Example: This pictogram shows the number of each food item sold during one lunchtime at a local shop.

Food items sold





Pictograms represent data with pictures.

All pictograms should have ...

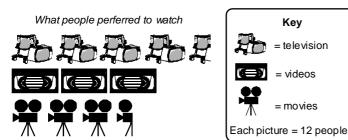
- a title or name,
- a key.
- a scale stating the value of each picture.

From this pictogram we can work out that 40 cartons of fries were sold. Were there 25, 35 or 45 hamburgers sold? Answer: 35 hamburgers

What other information is contained in this pictogram?

Task 14

A survey was conducted to find out if people preferred to watch TV, watch a video or go to the movies. This pictogram displays the results.



- 1. How many people does each picture represent?
- How many people preferred to watch a 2 video?
- 3. How many people preferred to go to the movies?
- How many people were surveyed? 4.

A second survey 6 months later was conducted, with the following results. 72 people preferred watching TV, 42 people preferred watching videos and 66 people preferred to go to the movies.

6.

5. **Draw** a **pictogram** to display these results.

Draw pictograms for the data contained in these frequency tables. Comment about each graph.



Shoe size	F
6	18
7	24
8	12
9	9

Weather conditions recorded for 50 days	5
---	---

Weather	F
sunny	16
cloudy	20
raining	12
snowing	2

9. 1	Гу
	á

Number of each type of book sold							
	Type of book	F					
	adventure	80					
	nature	120					
	fiction	140					
	travel	60					

10. Collect your own data and present your data as pictograms.

8.

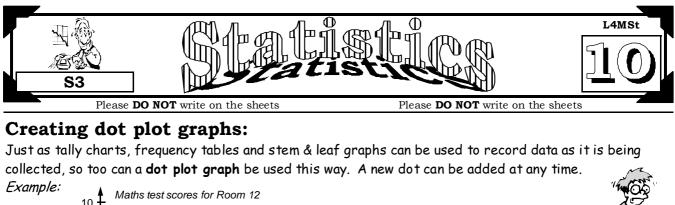
Task 15

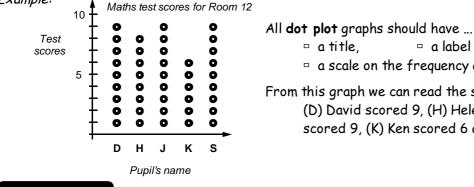
Create pictograms from the frequency tables created in Task 5, questions 1 and 4, Worksheet 3.

Look back at the frequency tables you created to collect and organise data from your questionnaire. Create pictograms from the frequency tables you created in Task 6, Worksheet 3 (if appropriate).

7.

How many people were surveyed this time?





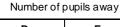
a label on each axis, • a scale on the frequency axis. From this graph we can read the scores as follows ... (D) David scored 9, (H) Helen scored 8, (J) John scored 9, (K) Ken scored 6 and (S) Sam scored 9.

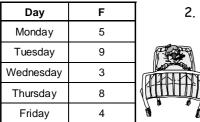


6.

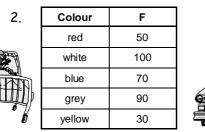
1.

Draw dot plot graphs for the data contained in these frequency tables. Comment about each graph. Remember to choose an appropriate scale on the frequency (vertical) axis.





Number of cars of each colour sold





upiis	scores in	i a iviatris	lesi
		-	

Name	Score
David	10
Jason	8
Karen	6
Jackie	9
Andrew	7

At a local restaurant orders were being taken for dinner using the menu below.

<u> </u>		The orders are	e shown in this	table below.		
ў (S) Soup ў (G) Garlíc Bread	\$4.50 \$2.95	S, G, P, I	G, C, A, I	S, G, F, I	S, P, A, I	G, F, A, I
ች ቼ (C) Chícken	\$ \$ 11.95	S, G, F, I	S, C, I	S, G, C, A	S, F, A, I	S, F, I
暮(P) Pork 暮(F) Fish	\$12.95 \$10.95	G, C, A	G, P, A, I	S, G, P, A	S, C, A	G, F, A, I
聋 是(A) Apple Pie	\$6.50	S, G, C, I	S, G, F, A	S, P, A, I	G, C, A, I	S, G, C, I
\$ (I) ice-cream	\$3.95 Å	G, P, I	S, G, C, A	S, G, F, I	S, G, P, I	G, C, A, I

ŘRARARARAREEEEEŘ

4. Organise this data into a dot plot graph. 5.

How many people ordered chicken? How many people ordered pork?

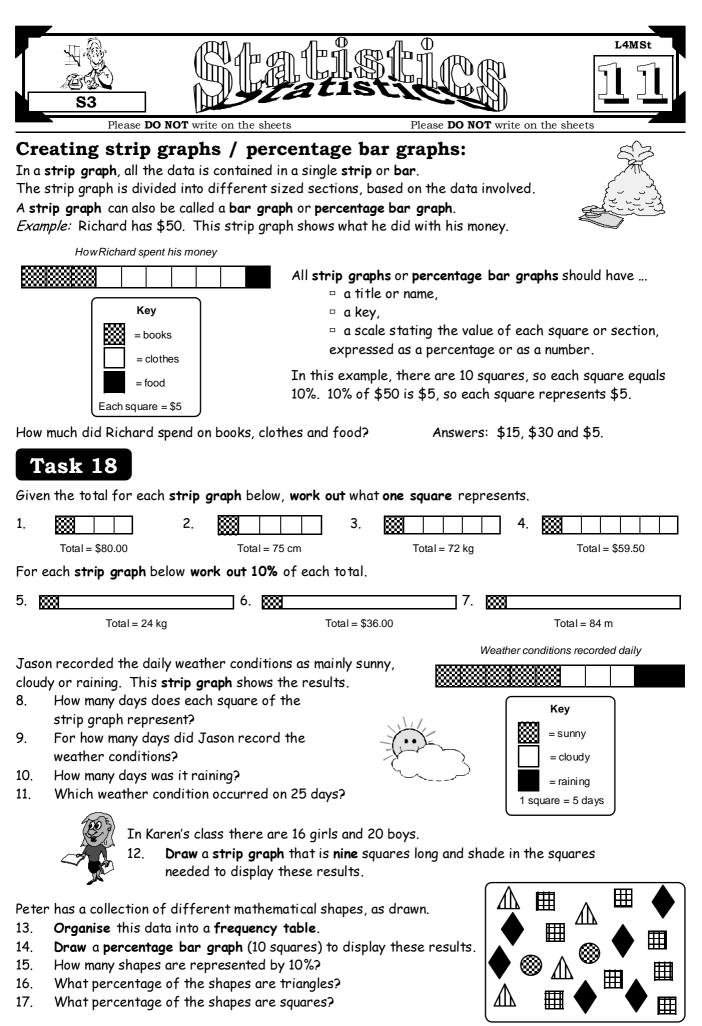
- What was the most popular food item ordered?7. Jan has \$40.00 If she ordered S, G, C, A and I what would it cost her and how much money would 8. she have left?
- 9. List what you would order and how much it would cost.
- 10. Collect your own data and present your data as dot plot graphs.

Task 17

Create dot plot graphs from the frequency tables created in Task 5, questions 1 and 4, Worksheet 3.

Look back at the frequency tables you created to collect and organise data from your questionnaire. Create dot plot graphs from the frequency tables you created in Task 6, Worksheet 3 (if appropriate).





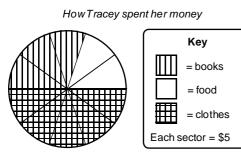
18. Collect your own data and present your data as a strip graph or a percentage bar graph.



Understanding pie graphs:

A **pie graph** is a circle that has been divided into sectors, like cutting up a round pie. Each sector represents a fraction or percentage of the total.

Example: Tracey has \$50.00. This pie graph shows how she spent her money.



- All pie graphs should have ...
 - 🛛 a title or name,
 - □ a key,
 - a scale stating the value of each sector, expressed as a fraction, a percentage or as a number.

In this example, there are 10 sectors, so each sector equals $1/_{10}$ or 10% or \$5.00, (\$50.00 ÷ 10 = \$5.00).

What fraction of her money did Tracey spend on books? What percentage of her money did she spend on clothes? How much did Tracey spend on food? Answer: $3/_{10}$ Answer: 50% Answer: \$10.00



Task 19

Julie recorded the daily weather conditions as mainly sunny, cloudy,

raining or stormy. This **pie graph** shows the results.

- 1. How many sectors in this pie graph?
- What fraction does each sector represent?
- 3. How many days does each sector represent?
- 4. On how many days was it stormy?
- 5. For what fraction of the days was it sunny?
- 6. On how many days was it sunny?
- 7. For what fraction of the days was it raining?
- 8. On how many days was it raining?
- 9. What weather condition occurred $3/_{10}$ of the time?
- 10. What time of the year do you think Julie collected this data? Explain your answer.



- In Siona's class there are 12 girls and 20 boys.
- 11. **Draw** a **pie graph** that has **eight** sectors.
 - How many pupils are represented by each sector?
 - Shade in the sectors to display this data.

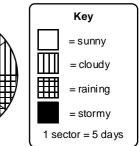
Linda spent \$40 on some new clothes, banked \$60 and spent \$20 on a birthday present.

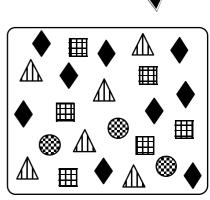
- 14. Draw a pie graph that has 12 sectors and state how much each sector is worth.
- 15. Shade in the sectors to display this data.

Robin has a collection of different mathematical shapes, as drawn.

- 16. Organise this data into a frequency table.
- 17. How many shapes are there altogether?
- 18. How many shapes are represented by one sector?
- 19. Draw a pie graph with 8 sectors to display these results.
- 20. What fraction of the shapes are diamonds?
- 21. What fraction of the shapes are squares?
- 22. Which shape makes up $\frac{3}{24}$ or $\frac{1}{8}$ of the total number?
- 23. Collect your own data and present your data as a pie graph.

Weather conditions recorded daily







Creating pie graphs using a protractor:

By using a **protractor**, a pie graph can be divided into sectors to represent the data. To draw a pie graph we must first calculate the angles needed to be able to divide the pie graph into sectors.

Example: This table shows the eye colours of pupils in Room 4.

Follow these steps to calculate the pie graph sector angles.

_		
Ste	F	Eye colour
Ste	9	blue
	12	hazel
	9	brown
Ste	6	green
	36	

ep 1: Add up the frequency column. Example: 36
ep 2: Divide the number of degrees in a circle (360°) by the frequency total. Example: 360° ÷ 36 = 10°. This means that each person is represented by a 10° angle sector in the pie graph.
ep 3: Multiply each group of data by your answer in Step 2.

Example: blue eyes is $9 \times 10^\circ$ = 90° , hazel eyes colour is $12 \times 10^\circ$ = 120° , brown eyes is $9 \times 10^\circ$ = 90° , green eyes is $6 \times 10^\circ$ = 60°

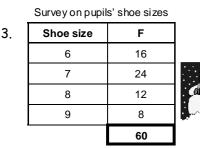
5.

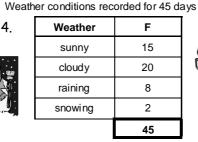
Step 4: Draw a circle with a compass, draw in one radius, then draw the sectors using your angle answers from Step 3, using a protractor.

Task 20

- 1. **Draw** a pie graph with sector angles of 80°, 160° and 120°.
- 2. Draw a pie graph with sector angles of 45°, 125°, 60° and 130°.

Calculate the **sector angles** required to draw pie graphs for the data in these frequency tables, following the steps outlined above.





Number of each type of book sold

Eye colour

brown eye 90⁰

hazel eyes 120⁰

(33.3%)

(25%)

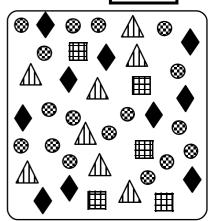
blue eyes 90°

(25%)

green eyes 60⁰

16.7%)

Type of book	F
adventure	70
nature	110
fiction	130
travel	50
	360



Andrew has a collection of different mathematical shapes, as drawn.

- 6. Organise this data into a frequency table.
- 7. How many shapes are there altogether?
- 8. What percentage of the shapes are triangles?
- 9. What fraction of the shapes are circles?
- 10. Which shape makes up $\frac{5}{40}$ or $\frac{1}{8}$ of the total number?
- 11. Which shape makes up 25% of the total number?
- 12. Calculate a sector angle for each mathematical shape.
- 13. To display this data, **draw** a **pie graph** using a compass, protractor and the sector angles calculated in question 12.
- 14. Collect your own data and present your data as a pie graph.

Task 21

Create pie graphs from the frequency tables created in Task 5, questions 1 and 4, Worksheet 3.

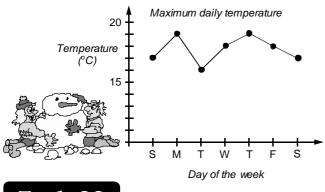
Look back at the frequency tables you used to collect and organise data from your questionnaire. **Create pie graphs** from the frequency tables you created in **Task 6**, **Worksheet 3** (if appropriate).



Creating time-series data:

Data that changes with time can be graphed as a time-series graph. Time-series graphs will always have time on the horizontal axis. This may be in years, months, weeks, days, minutes or seconds.

Example: Jeremy recorded the maximum daily temperatures for one week.



All time-series graphs should have

- a title or name,
- time on the horizontal axis,
- $\hfill\square$ a label and scale on each axis,
- • or X to mark each point, joined by lines.

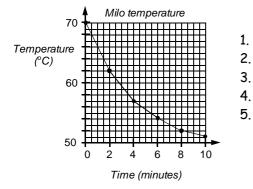
In this example, the maximum temperature on Sunday was 17°C. List the maximum temperatures for the other days of the week, in order.

Answers: $19^{\circ}C$, $16^{\circ}C$, $18^{\circ}C$, $19^{\circ}C$, $18^{\circ}C$ and $17^{\circ}C$

Task 22

Martin made himself a cup of milo, but it was too hot to drink. The time-series graph below shows the temperature of the milo as it cooled.





- What was the temperature after 2 minutes?
- After how many minutes was the temperature 54°C?
- What was the temperature of the milo at the start?
- How much did the temperature drop in the first 6 minutes?
- Use the graph to estimate what the temperature of the milo was after 7 minutes.

Mr Jones has been training each day for a running race.

He runs the same distance each day and this table shows

how long it takes him, with time recorded in minutes.

- 6. Draw a time-series graph to display this data.
- 7. On which day did he run the fastest time?
- 8. On which day was he feeling really tired?
- 9. What is the difference between his fastest and slowest training times?
- 10. For how many minutes has Mr Jones been training so far?



Rainfall is collected in a rain gauge and is measured in millimetres.

This table shows the volume of rainfall that fell, collected in Sam's rain gauge.

Week	1	2	3	4	5	6	7	8	9	10
Rainfall (mm)	8	14	З	20	15	9	17	6	12	10

- 12. Draw a time-series graph to display this data. 13.
- 14. In which week was there the least rain?
- 16. In which week did 14mm of rain fall?
- In which week did it rain the most?
- 15. How much rain fell in the 8th week?
- 17. How much rain fell altogether?

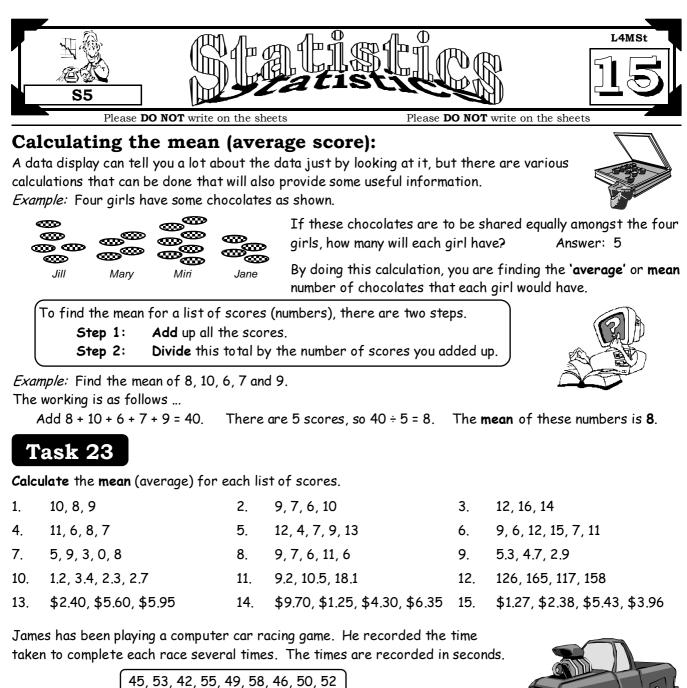
11.

18. Collect your own time-series data and present your data as a time-series graph.

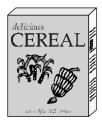
How often is the rainfall measured?

т w т F S Day М S 23 21 27 20 17 22 19 Time (m)





- 16. How many times did James play this car racing game?
- 17. Find the **mean** time taken for these races.
- 18. What was the difference between the fastest and slowest times?



As cereal boxes are filled, they are weighed in grams by a machine.

```
705, 698, 701, 695, 692, 714, 703, 699, 704, 709
```

- 19. How many boxes of cereal have been filled so far?
- 20. Calculate the **mean** weight for these cereal boxes.
- 21. What was the difference between the lightest and the heaviest cereal box?

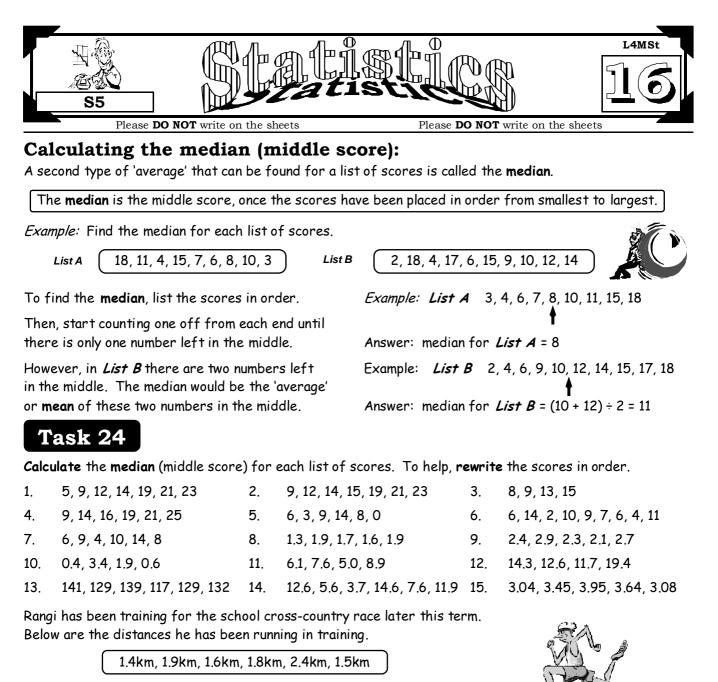
Jeremy listed the price of cars in a local car sales yard.

\$8500, \$9300, \$10200, \$7500, \$8900, \$11200, \$14500, \$19900

- 22. How many cars are in this car sales yard?
- 23. Calculate the **mean** cost for these cars.
- 24. What is the difference between the cheapest and the most expensive car?
- 25. Create your own list of scores or numbers, then calculate the mean value for each list.



AWS



- 16. How many times has Rangi been out training?
- 17. Find the **median** distance of his training runs.
- 18. What was the difference between the shortest and the longest run?

delicious CEREAL

As cereal boxes are filled, they are weighed in grams by a machine.

995, 1009, 995, 1012, 1008, 999, 1014, 996, 1009, 1006

- 19. How many boxes of cereal have been filled so far?
- 20. Calculate the **median** weight for these cereal boxes.
- 21. What was the difference between the lightest and the heaviest cereal box?

Jeremy likes playing golf and below are his scores for each hole for his latest round of golf.

4, 5, 8, 7, 4, 5, 5, 3, 8, 7, 6, 6, 5, 4, 3, 5, 6, 7

- 22. How many holes of golf did he play?
- 23. Calculate the **median** number of shots taken during this round.
- 24. What is the difference between the best and the worst hole score?
- 25. What was Jeremy's total score for this round of golf?

25. Create your own list of scores or numbers, then calculate the median value for each list.

AWS



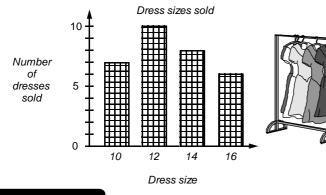
Finding the mode (most common score):

A third type of 'average' that can be found for a list of scores is known as the **mode**. The mode can often be worked out by looking at a data display.

The most common score is known as the mode. There may be more than one mode or no mode, if all scores are different.



Example: What is the most popular dress size sold during one day.



Looking at this graph, we can see that a size 12 dress was the most common dress size sold.

Find the mode for these scores.

5, 9, 12, 9, 6, 5, 3, 7 Answer: Both 5 and 9 are modes.

2, 3, 9, 6, 7, 4, 5, 0 Answer: There is no mode.

Task 25

Find the mode (most common number) for each list of scores.

1.	5, 6, 9, 8, 4, 5, 9, 7	2.	6, 8, 6, 7, 2, 10	3.	3, 1, 6, 8, 3, 4, 2, 1, 3, 6, 2
4.	9, 10, 5, 6, 8, 7, 0, 2	5.	23, 14, 15, 23, 17, 15	6.	9, 14, 23, 14, 9, 5, 7, 9, 2, 9
7.	10, 9, 6, 8, 10, 9, 8, 5	8.	14, 23, 27, 31, 29, 20, 16	9.	45, 12, 35, 64, 25, 14, 35
10.	1.3, 1.6, 1.3, 1.4, 1.3, 1.9	11.	2.3, 5.6, 4.2, 1.2, 2.3, 4.2	12.	126, 165, 117, 158, 156, 161
13.	12.01, 12.10, 12.01, 12.00	14.	1, 2, 1, 2, 1, 4, 1, 2, 1, 3, 2	15.	3, 6, 2, 1, 3, 2, 1, 4, 2, 3, 1, 2

At a local supermarket, juice cartons come in three sizes, 250mL, 600mL and 1000mL. The number of each size container sold is recorded below.

250, 600, 250, 1000, 1000, 600, 250, 600, 250, 1000, 600, 250, 250, 250, 600, 1000 250, 600, 600, 1000, 1000, 600, 250, 250, 600, 250, 600, 1000, 1000, 600, 250, 250

FLORDA ORANGE

16. Organise this data into a frequency table.

- 17. From your frequency table, state the mode or most common size sold.
- 18. How many juice cartons were sold altogether?

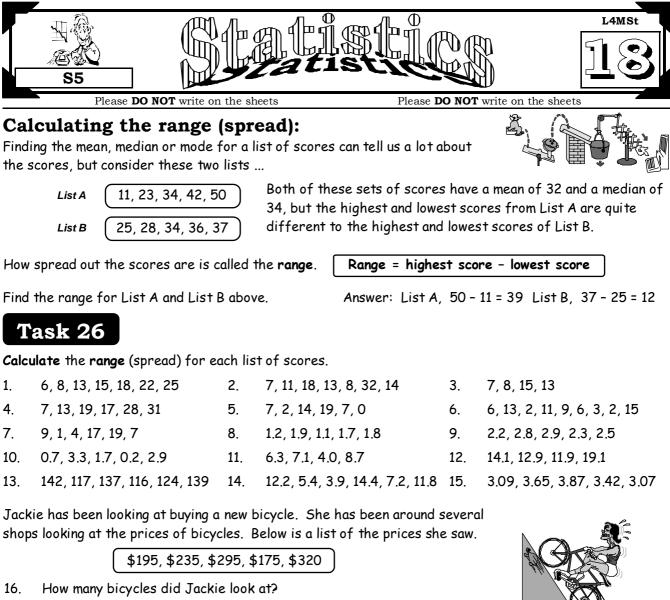
In the evenings and weekend, telephone calls cost only \$5.00 and you can talk for as long as you like. The length of some telephone calls is shown below, recorded in minutes.



15, 18, 19, 16, 20, 15, 16, 18, 19, 12, 15, 14, 15, 14, 12, 19, 19, 15, 16, 17, 20, 20, 18, 15, 14, 13, 19, 12, 16, 15, 20, 17, 12, 19, 17, 15

- 19. Organise this data into a frequency table.
- 20. From your frequency table, state the mode or most common length of telephone call.
- How many telephone calls were made altogether? 21.
- 22. Create your own list of scores or numbers, then state the mode value for each list.





- 17. Calculate the **range** of prices for these bicycles.
- 18. Calculate the **mean** price of these bicycles.



As cans of baked beans are filled, they are weighed in grams by a machine.

333g, 338g, 330g, 338g, 335g, 339g, 334g, 332g, 337g, 334g

- 19. How many cans of baked beans have been filled so far?
- 20. Calculate the **range** of weights for these baked bean cans.
- 21. Find the median weight of these baked bean cans.

Jeremy likes playing golf and below are his scores for each hole, for his latest round of golf.

5, 6, 7, 8, 5, 4, 4, 7, 3, 4, 7, 5, 6, 5, 4, 4, 7, 5

- 22. How many holes of golf did he play?
- 23. Calculate the **range** for the number of shots taken per hole during this round.
- 24. What was the mode or most common score that Jeremy got?
- 25. What was Jeremy's total for this round of golf?
- 26. If the highest score is 123 and the range is 39, calcluate the lowest score.
- 27. If the lowest score is 58 and the range is 47, calculate the highest score.
- 28. If the range is 26 and the score 34 is exactly in the middle, calculate the lowest and highest scores.
- 25. Create your own list of scores or numbers, then calculate the range value for each list.

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Interpreting data display:

The purpose of drawing various graphs and working out means, medians, modes and ranges is to be able to answer questions that have been raised by an investigation. The ability to interpret a data display is an important skill.

Example: Billy scored 45%, 45%, 87%, 75% and 69% in her exams, but said, "I didn't do very well because my most common mark was only 45%!" Was she right?

Answer: While the mode was 45%, her other three scores were all good, so she did quite well.

Task 27

Look at each data display. Read the comments written beside them. Are the comments correct? Explain your answers.

1.

3.

20

15

10

boys

4

Number

of pupils

Colour	Frequency
white	11
black	9
red	7
blue	8
	35

Car colour

Anna recorded the colour of cars in the school car park. Kevin said, "Most teachers have white coloured cars."

Is his statement correct?



	Test scores for Room 4		Test scores for Room 5
2.	8, 9, 7, 7, 6, 7 0, 6, 7, 6	0 1	8, 9, 7 9, 8, 5, 9, 6, 6, 6 0
	0, 0, 0	2	0

girls

Pupils in Room 3

This is a back-to-back stem and leaf graph showing test scores for two classes. David, who is in Room 4 said, "We are the top class as three pupils scored 20 out of 20."

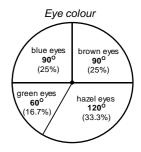
Is his statement correct?

This column graph shows the number of boys and girls in Room 3. Sally said, "Because the column for girls is twice as tall as the column for boys, there must be twice as many girls as boys in this class."

Is her statement correct?

This pie graph shows the colour of Room 7 pupil's eyes. Tony said, "Most pupils have hazel coloured eyes."

Is his statement correct?



5. Look back at the data displays you and your classmates created as a result of your investigations. **Compare** your displays with classmates and **comment** about the features of your displays.

Task 28

Collect some frequency tables /data displays from the newspaper or some magazine.

Look at each table / data display and talk about the features that make the data displays stand out.



Creating statistical reports:

Working in small groups of 2 or 3, your task is to create a statistical report.

Organise the data into various tables and displays, perform calculations such as finding the **mean**, **median**, **mode** and **range**, as you try to prove or disprove the statement written beside the data.

Remember to finish your report with a conclusion.

Task 29

John and Rangi like playing a computer car racing game. They have turns (1, 2, 3, 4 & 5) playing the game and they record the time in seconds taken to drive around each of the three courses (A, B, & C).



John's lap times									
	Α	В	С						
1	66	124	46						
2	59	129	44						
3	69	137	41						
4	71	115	55						
5	63	127	43						

Rangi's lap times

	Α	В	С
1	62	119	50
2	64	126	36
3	60	135	42
4	70	117	48
5	63	130	43



John believes he is the better driver as he has the faster lap times. Is he correct?

Task 30

At a local restaurant, records are kept about people who attend the restaurant.

Key for main

meals C = chicken F = fish B = beef P =pork

Size of group			Time spent at restaurant	
3 people	C, C, F	\$48.00	21⁄2 hrs	
5 people	F, F, P, C, C	\$96.00	4 hrs	
2 people	С, В	\$37.50	1½ hrs	
4 people	B, B, C, F	\$86.50	4 hrs	
2 people	B, C	\$34.50	3½ hrs	
5 people	P, B, C, C, F	\$127.50	3 hrs	
6 people	C, F, P, P, B, B	\$142.00	5 hrs	
3 people	C, F, B	\$73.00	4½ hrs	

The owner of the restaurant believes that ...

- average group size is about 3 people,
- most people like fish best,
- the average price per meal is \$20.00 per person,
- people stay for about 3 hours.

Is the owner correct?

Task 31

By now you know how to

- \blacksquare plan an investigation, write a questionnaire / conduct a survey,
- ☑ collect and display data,
- \square perform calculations on this data
- \blacksquare make predictions and write a conclusion based on the results of the investigation.

Conduct an investigation to demonstrate the above skills.





Understanding probability words:

Probability is a measure of how likely it is that an event will happen.

The likelihood of an event or something happening could be described by using one of the following words ... certain, possible, impossible.

Other words that could be used are ...

certain, likely, unlikely, impossible

or certain, good chance, even chance, poor chance, impossible.

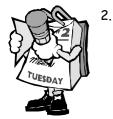
Task 32

1. Use the words ...

certain, likely, unlikely and impossible,

to **write** statements about events that you know of, that could be described by using these words. *Example:* There is a good chance it will rain tomorrow.





- Arrange these events in order of likelihood, starting with the most likely event first.
 - A If you roll a die (dice) the number 4, 5 or 6 will come up.
 - **B** The Prime Minister will visit your school tomorrow.
 - C Someone in New Zealand will win 1st prize in lotto this week.
 - D If today is Monday, tomorrow will be Tuesday.
 - **E** A glass jar will break when dropped.

Decide if these events are certain, likely, unlikely, possible or impossible.

- 3. Today it will be dark at 7:00 p.m.
- 4. I will win the school cross-country race.
- 5. Tomorrow I will go to the doctor.
- 6. 10 pupils in your class will be away sick tomorrow.
- 7. It will snow on Christmas day this year.
- 8. It is your birthday tomorrow.
- 9. The sun will rise tomorrow.
- 10. There will be a February 29th this year.
- 11. You will get a job when you leave school.
- 12. New Year's day is the 1st January.



Use **even chance**, **good chance** or **poor chance** to describe the likelihood of the following events happening.

- 13. A coin is tossed and a tail comes up.
- 14. Two coins are tossed, one is a tail and one is a head.
- 15. Two coins are tossed and two heads come up.
- 16. A die (dice) is rolled and an odd number comes up.
- 17. A die is rolled and a number less than 4 comes up.
- 18. A die is rolled and a six comes up.
- 19. A die is rolled and a 1, 3 or 5 comes up.
- 20. A card is drawn from a deck of cards and it is an ace of spades.
- 21. A card is drawn from a deck of cards and it is a heart.
- 22. A card is drawn from a deck of cards and it is a black card.







Calculating relative frequency / probability scales:

The **relative frequency** of an **event** occurring is the fraction or proportion of times the event occurs. Relative frequency could also be known as **experimental probability**.

Example: In an experiment, two coins are tossed 50 times (50 **trials**).

The event that Kaye recorded is, 'how many times two heads occur!. This occurred 12 times.



Relative frequency =	Number of times the event occurs
Relative frequency -	Total number of trials

In Kaye's experiment the number of trials was 50, and the number of times the event occurred was 12, therefore the relative frequency of this event was $^{12}/_{50}$.

This event could be marked on a probability scale.

↓ 2 heads	certain
	↑ 2 heads

Task 33

8.

Below is a frequency table recording the results of an experiment where two coins were tossed.

1. Copy this frequency table and complete the frequency column.

5.

Event	Tally	F
HH	₩ ₩ III	
HT	1111 1111 1111 III	
ΤH	JH JH JH III	
TT	ш ш	

- 2. How many trials were there in this experiment?
- 3. Calculate the relative frequency for the event head / head.
- 4. Which event had a relative frequency of ${}^{11}/_{60}$?
 - **Calculate** the relative frequency for the event tail / head, in any order.
- 6. **Draw** a probability scale and **mark** on the scale where these three events would be ... HH, TT and HT / TH combined.

Working in small groups, repeat the above experiment of tossing two coins.

- 7. Record your results in a frequency table,
 - Work out the **relative frequency** of all events.
 - 9. Mark the results of your experiment on a probability scale.

Inside a container are the mathematical shapes shown in this diagram.

- 10. Organise the data in a frequency table.
- 11. If a shape is selected at random from the container, work out the relative frequencies that it could be ...

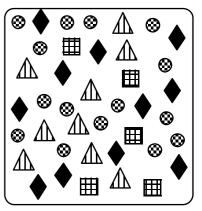
a circle, a square, a triangle or a diamond.

- Draw and mark on a probability scale these events ...
 - Event A: a square is selected from the container.
 - Event B: a diamond is selected from the container.
 - Event C: a mathematical shape is selected from the container.
 - Event D: a hexagon is selected from the container.

Working in small groups, place up to 20 coloured blocks, preferably all the same size, in a container or bag, noting how many of each coloured block you have.

- 13. Select a block from your container and record which one. Replace the block and repeat 50 times.
- 14. Based on your results, work out the **relative frequency** of selecting each different coloured block.
- 15. Mark the results of your experiment on a probability scale.

12.







Finding outcomes using grids:

All possible results of an experiment are called **outcomes**. When James is thirsty he will have a drink. If he can have either a drink of water or a drink of juice, the choice is easy. His two choices of water or juice are called **outcomes**.

Finding all possible outcomes is not always easy.

Example: A coin and a die are thrown at the same time. List all possible outcomes. One way to find the outcomes is to use a grid or box.

		6 sided die					
		1	2	3	4	5	6
	н	H1	H2	H3	H4	H5	H6
coin	т	T1	T2	Т3	T 4	T5	Т6

The outcomes can be obtained from the grid ...

(H,1), (H,2), (H,3), (H,4), (H,5), (H,6),

(T,1), (T,2), (T,3), (T,4), (T,5), (T,6) ...

where (H,1) means heads on the coin and a '1' on the die came up.

Task 34

Pupils in Room 7 can choose (C) cricket, (Sb) softball or (T) tennis as their summer sport. In winter they can choose (R) rugby or (Sc) soccer. Pupils can play only one summer and one winter sport.

- 1. Copy and complete this grid to help work out the combinations of sports that pupils can play.
- 2. List all the possible outcomes or choices that the pupils have.

Alex has two bags containing different coloured beads. Bag A has some (R) red, (B) blue and (G) green beads. **Bag B** has some (P) purple, (Y) yellow and (O) orange beads.

- 3. Alex picks one bead from each bag. Use a **grid** to help work out all possible combinations of coloured beads she could select.
- 4. List all the possible outcomes or combinations of coloured beads.

Alex adds some (W) white and (BI) black beads to Bag A and some (Br) brown beads to Bag B.

- 5. **Draw** a **grid** to help work out the new combinations of coloured beads that Alex could select if she selects one bead from each bag.
- 6. How many possible outcomes are there altogether?

Breakfast Mer	Г. Г. С.		
(B) Bacon & Eggs	\$4.60		
(1) Toest & Jem	\$3.50		
(C) Cereal	\$4.00		
"Drinks'			
(M) Milo	\$1.20		
(F) Fruit juice	\$0.90		
(H) Hot chocolate	\$1.50		

- For breakfast, Miri has a choice of one of the three 'Breakfast Menu' items and one of the 'Drinks'.
- 7. **Draw** a **grid** to help work out all the possible choices Miri has.
- 8. List all possible breakfast combinations.
- 9. If Miri had bacon & eggs and fruit juice, what would it cost her?
- If she paid for breakfast with a \$20.00 note, what change did she receive?
- 11. If her breakfast cost \$4.70, what did she have to eat and drink?

During the holidays, Martin has a choice of going to the (M) movies, hiring a (V) video, going to the (P) park to play or going to a (F) friend's place. He is allowed to do one of the above activities, but only on one day of the week.

- 12. Draw a grid to work out all possible combinations of these activities on the days of the week.
- 13. How many possible outcomes are there altogether?
- 14. If Martin cannot go out on Monday or Wednesday, how does this alter the number of possible outcomes?



С

R

Sc

Sb

Т



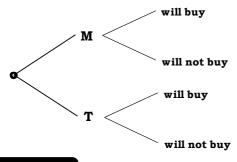






Finding outcomes using tree diagrams:

A **tree diagram**, so named because of its shape, is another way of working out all possible outcomes. *Example:* Jack will go shopping on Monday or Tuesday and might buy a new toy.



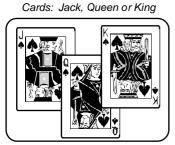
To find all possible outcomes, follow each branch of the tree diagram. There are four branches so there will be four outcomes.



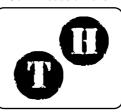
The outcomes would be ... (Monday, will buy), (Monday, will not buy) (Tuesday, will buy), (Tuesday, will not buy).

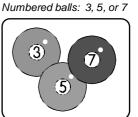
Task 35

Michelle is going to select a picture card, toss a coin and select a numbered ball from a bag.



Coin: Heads or Tails





- 1. **Draw** a tree diagram to help work out all possible combinations, as Michelle selects a card, tosses a coin and selects a numbered ball, in that order.
- 2. Use your tree diagram to list all possible outcomes.
- 3. How many outcomes include the King of spades?
- 4. How many outcomes include a coin showing heads?
- 5. How many outcomes include a ball with the number 7 showing?
- 6. Michelle changes the order to tossing a coin, selecting a ball and then selecting a card. **Draw** a new tree diagram to show this combination.

Brezkfest Menu			
(B) Bacon & Eggs	\$4.60		
(1) Toəst & Jəm	\$3.50		
(C) Cereal	\$4.00		
Frait			
(O) Orange	\$0.50		
(K) Kiwi fruit	\$0.30		
(A) Apple	\$0.40		
"Drinks'			
(M) Milo	\$1.20		
(F) Fruit juice	\$0.90		
(H) Hot chocolate	\$1.50		

For breakfast, John has a choice of one of the three

'Breakfast Menu' items, a piece of 'Fruit' and one of the 'Drinks'.
7. Draw a tree diagram to help work out all the possible combinations that John could have.

- 8. How many outcomes are there altogether?
- 9. If John does not like bacon & eggs, how many combinations does he have to choose from?

10. If John had some toast, an orange and a drink of milo for breakfast, how much did it cost?



11. If John paid for his breakfast with a \$20.00 note, how much change did he receive?

12. If his breakfast cost \$5.90, what did he have to eat and drink?

13. Think of some events in your life. **Create** your own **grid diagrams** or **tree diagrams** as above to work out all possible outcomes for these events.



Using probability to predict outcomes:

Data that has been collected can be used to make predictions.

Example: A coin is tossed 100 times. How many times would you expect 'heads' to come up?

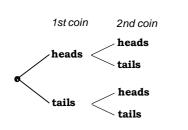


For a coin, the probability or chance of getting heads is '1 out of 2' or $\frac{1}{2}$ or 50%. If a coin is tossed 100 times, you could expect heads to occur 50 times (100 × $\frac{1}{2}$ = 50).

How many times would you expect tails to occur if a coin is tossed 200 times? Answer: $200 \times \frac{1}{2} = 100$ times.

Task 36

This tree diagram shows the possible outcomes when two coins are tossed.



- 1. List all possible outcomes.
- 2. What is the probability or chance that two heads come up? 3. What is the probability or chance that two tails come up? 4. What is the probability that a head and a tail, in any order come up? If the two coins are tossed 100 times, how many times would you 5. expect HH to come up?
- If HT and TH came up 150 times altogether, how many times do you 6. think the two coins were tossed?

A six sided die (dice) is rolled several times.

7. What is the probability that it lands showing the number 6?

- 8. What is the probability that it lands showing a number less than 4?
- What is the probability that it lands showing the number 2 or 4? 9.
- If a die is rolled 60 times, how many times would you expect the number 5 to occur? 10.
- If a die is rolled 200 times, how many times would you expect a number greater than 3 to occur? 11.

A local shop-keeper kept a record of the number of different drinks that he sold to pupils in one day. This table shows the result.

Drink	Number sold	12.
Coca Cola	50	13. 14.
Fanta	30	15.
Flavoured milk	20	16.
Fruit juice	15	17
Ginger beer	5	17.

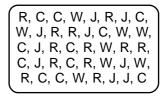
- 12. How many drinks has he sold altogether?
- What is the probability that a pupil had a drink of Coca Cola? 13.
- 14. What is the probability that a pupil had a drink of fruit juice?
- 15. 20 out of 120 pupils chose which drink?
- If 240 pupils ordered drinks, how many Fanta drinks would the 16. shop-keeper expect to sell?
 - If 360 pupils ordered drinks during the week, how many Ginger beer drinks would the shop-keeper expect to sell?

A radio station surveyed 40 people, asking them to name their favourite style of music, given a choice between, rock (R), jazz (J), country & western (W) and classical (C).

18. Organise this data into a frequency table.

- 19. What was the probability that a person liked rock music?
- 20. What was the probability that a person liked classical music?
- Based on these survey results, predict how many people would 21. like each style of music if 400 people were surveyed.

Music survey results





22. Make up some frequency tables as above and use your information to work out the probability of each outcome. Then use your probability values to make predictions for larger populations.

'In-class' Worksheet

Teaching Notes & Answers

How to use this section:

Teaching notes are enclosed in a box with a 'push-pin' at the top left corner. The teaching notes precede the answers for each worksheet / task. The teaching notes have been included to provide assistance and background information about each topic or unit of work.

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Introduction:

The topic of **Statistics** is concerned with the planning of investigations, providing an opportunity to study issues that are important to the pupils at your school. The ability to collect the appropriate data and to display the data in various tables or graphs to communicate the results of the investigation is an important skill. From the displays, distinctive features can be highlighted and further calculations can be performed, to interpret the data to support the investigation. From these interpretations, statements and conclusions can be made that are consistent with the results of the statistical investigation.

Exploring probability is also investigated through the use of relative frequency tables and tree diagrams.

₿ Worksheets 1 & 2 Introduction to statistical investigation: Designing a questionnaire: In **Task 1** pupils are introduced to important statistical words and their meanings. Key statistical words are listed below: A survey is a brief or detailed study, whereby data that is collected can be used to draw Survey: various statistical graphs, interpret the information and make conclusions or predictions based on the evidence of the survey. Questionnaire: A questionnaire is one way of surveying a population when you are asking for an opinion about an issue. A good guestionnaire has guestions that are clear and concise, but not too many questions. Population: In everyday language the word 'population' refers to the number of people in a town, city or country. In statistics, a 'population' can refer to a group of not just people or animals, but a group of anything. *Example:* a population of trees, a population of books, etc. A sample is part of a population you are interested in. A sample of a population is used if Sample: the population is very large or if it is not necessary to survey the whole population. **Representative sample:** When we want to make statements about a population, using a survey to sample the population, the sample should be a **representative sample**. *Example:* 10% of the pupils at a school are to be surveyed. If there are 200 pupils, 10% would be 20 pupils. If there are 90 boys and 110 girls and 10% are to be surveyed, for the sample to be a representative sample, there would be 9 boys and 11 girls surveyed, giving us a total of 20 pupils. Random sample: Choosing at random, means that every person, or item, has an equal chance of being chosen. Biased sample: A sample that is not a representative sample is called a biased sample. Example: In a class of 15 girls and 15 boys, if 10 boys and 5 girls were surveyed about what sport they wanted to play at lunchtime, the pupils surveyed would be a biased sample as more boys were asked than girls. In **Task 2** pupils are to work in small groups and decide on any important issues that they could investigate. The main features of an investigation are listed with the task.

In **Task 3** pupils are to consider what type of questions they would use when designing a questionnaire, given points about what makes a good questionnaire. Questions are to have 'yes' / 'no' answers and pupils are to create similar questions. Other questions are to be answered and created where choices for answers are given.

In **Task 4** pupils are to look back at the issues they considered investigating in Task 2, Worksheet 1 and design a suitable questionnaire. Having designed the questionnaire, pupils are to decide what is the best way the data can be collected and organised.

Task 1

1. population 2. sample 3. survey 4. representative sample 5. biased 6. random 8. - 9. - 10. The population may be too large to survey. It is quicker to do. 7. guestionnaire 11. 10% of 180 pupils is 18. 10% of 100 boys is 10 and 10% of 80 girls is 8, therefore 10 boys surveyed and 8 girls surveyed, gives a total of 18 pupils. 12. Teachers are a small percentage of the whole population and could be a biased sample. 13. All interested parties, pupils, parents / caregivers, teachers and 14. Choose 10% of the pupils in each class, draw 50 family names from the school records at principal random, ask every 5th pupil / parent coming through the school gate in the morning, etc.

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Worksheets 3 & 4

Collecting and organising discrete data using a fequency table: Organising grouped data:

The are two types of data, discrete and continuous data. Discrete data is any data that has been collected by counting. Continuous data is any data that has been collected by measuring.

The use of a **frequency table** (or tally chart) is an effective way to collect data that is randomly being collected, called out or presented as a random list. Encourage pupils to count in 'fives' as this makes it easier when adding up. Marking data in the appropriate row as you go, rather than searching for all the same data at once, will make it less likely that data items are overlooked. By adding up the frequency column, the number of data items collected can be found.

To use a frequency table to collect discrete data that is well spread out, the data can be **grouped**. Grouping data avoids having too many rows in the frequency table and the grouped data is easier to display. Each grouping or category is called a **class interval**. Class intervals should be the same widith or size.

Example: The class interval 1 - 5 includes the numbers 1, 2, 3, 4 & 5 The class interval 6 - 10 includes the numbers 6, 7, 8, 9, 10. Both class intervals are made up of five numbers.

The only disadvantage with grouped data is that you do not know exactly what the number is, once the number has been recorded, only that it falls within a certain class interval.

Example: There are 5 numbers in the class interval 6 - 10, but are the numbers 6's, 7's, 8's, 9's or 10's?

In **Task 5** pupils are to organise discrete data in a frequency table, utilising a tally column, marking off in fives. The number of items collected is found by adding up the frequency column. By studying the frequency tables created, pupils are to write a statement about the data.

In **Task 6** pupils are to create frequency tables for any appropriate questions that were created in Task 4, Worksheet 2. Having created the frequency tables, pupils are to collect the data, recording the responses in the frequency table.

In **Task 7** pupils are given data that is to be recorded in frequency tables that have class intervals already given. In later questions, pupils are decide on the class intervals that will be used. As a general rule, somewhere between 5 and 7 equal class intervals is usually enough.

Task 5

1.

No. of mistakes	Tally	F
0	HH.	5
1	HHT IIII	9
2	1117 HIT	10
3	1111 I	6
4	=	3
		33

4.	Travel	Tally	F
	walk	HHT HHT IIII	14
	bike	HHT HHT	10
	bus	HHT I	6
	car	1111	4
			34
5.3	4 pupils		

10.

Distance	Tally	F
1	HHT III	8
2	HH HH	10
3	1111	5
4	н	2
5	1111	4
6	ш	3
7	н	2
		34

2. 2 mistakes 3. 33 pupils

6. The most common way pupils in Room 9 travel to school is by walking, followed by biking to school. The most common distance that pupils live away from the school is 2km, followed closely by 1km distance.

6.

1.

Number a	of Lego blo	cks used
CI	Tally	F
11 - 15	1111 I	6
16 - 20	1111	5
21 - 25	1111 III	8
26 - 30	1111 I	6
31 - 35		3
		28

Speech o	competition	scores
CI	Tally	F
11 - 15		4
16 - 20	1111 III	8
21 - 25	1111 II	7
26 - 30	łłł	5
		24

	Number a	of trees per	garden
	CI	Tally	F
	1 - 5	III	3
Ī	6 - 10		10
	11 - 15	₩¥ III	8
	16 - 20	HH* 11	7
			28

2. 21 - 25 3. 11 pupils 4. 9 pupils 5. 28 pupils 7. 30 8. 12 pupils 9. 24 pupils 11. 6 - 10 12. 13 gardens 13. 15 gardens 14. 28 houses

Display	ing ungrouped discrete data as a column graph: ing grouped discrete data as a histogram: ng and organising continuous data using a frequency table:
and are	d confusion I would suggest that column graphs are always referred to as column graphs not called bar graphs. A bar graph is a different type of graph and is referred to in more Worksheet 11, Creating strip graphs /Percentage bar graphs.
	 n graph is used to display ungrouped discrete data, that is, data that has been collected ting. All column graphs should have a title or name a label on each axis a scale on the vertical axis, usually starting from zero gaps between columns a all columns should be the same width
separat	is occur between the columns because the data is ungrouped discrete , discrete meaning e. <i>Example:</i> A column graph displaying the number of cars of each colour in the staff car s gaps because each column represents a different colour.
histogr will be v the sam	umn graph is drawn without gaps between the columns it is called a histogram. A am is used to display grouped discrete data or continuous data. Within each column there various scores represented. The 'groupings' are called class intervals. All class intervals o e graph should be the same width, just as they are for frequency tables. The features of ams are the same as for column graphs, except there are no gaps between the columns.

In **Task 8** pupils are to create column graphs, given data presented in a frequency table. Data is also presented in a table, from which frequency graphs can be created, followed by the drawing of a column graphs. Remind pupils to present the graph neatly, with all necessary labels etc.

In **Task 9** pupils are to create column graphs from frequency tables created in Task 5, Worksheet 3 and from data collected in their investigations. Having created the column graphs, pupils are to write statements about the data. Remind pupils that the whole purpose of drawing any form of graph is to 'tell a story about the data', so presentation is important.

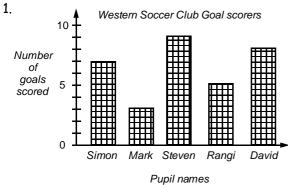
In **Task 10** pupils are to interpret information displayed as a histogram, create histograms from grouped discrete data and from frequency tables created in Task 7, Questions 6 & 7.

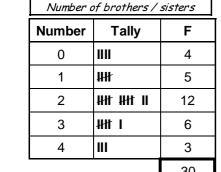
In **Task 11** pupils are to create **histograms** from **continuous data** displayed in frequency tables. Pupils are also to organise data into frequency tables before drawing more histograms.

In **Task 12** pupils collect their own continuous data, utilising frequency tables and then draw histograms to display the data.

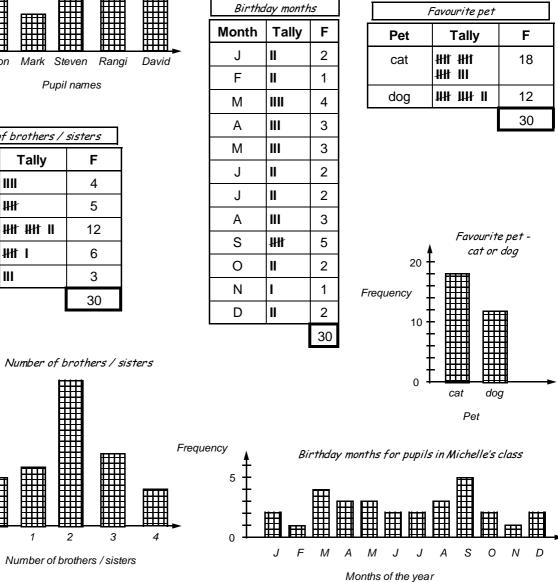
Task 8

J





- 2. Steven 3. 5 goals 4. Mark 5. 32 goals 6. Michelle could have set up a frequency table and
 - recorded the pupil's responses in them directly, rather than in the table she used.



7.

8.

1(

5

0

0

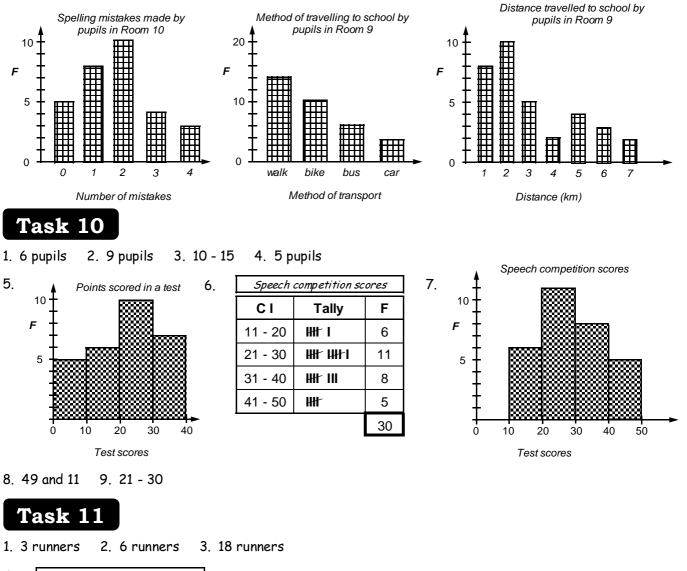
Frequency

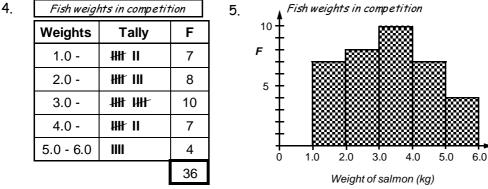
9. Examples of possible statements:

More pupils in Michelle's class have 2 brothers and / or sisters. The most common month for a birthday was September. More pupils prefer cats as pets than dogs as pets.



Column graphs using the data from Task 5, Questions 1 and 4.





6. 5.7kg 7. 25 fish 8. 36 fish 9. 4 fish

Creating stem and leaf graphs:

Worksheet 8

A stem & leaf graph is so called because of its shape. Stem & leaf graphs can be used to collect data in the same way as a frequency table can be used. Visually stem & leaf graphs can be useful when displaying two sets of similar data, when you want to compare results. When drawn this way, it is called a back-to-back stem & leaf graph. Stem & leaf graphs should have a title.

In **Task 13** pupils are to interpret the data displayed as a stem & leaf graph and create graphs given the data. Pupils are to collect and present data as stem & leaf graphs.

Task 13

1. 44, 41, 45, 49, 45, 40, 50, 52, 58, 57, 52, 59, 51, 62, 65, 61, 68, 67, 61, 66, 61, 78, 72, 73, 77 2. 8, 9, 7, 6, 15, 13, 19, 11, 13, 18, 10, 18, 29, 20, 23, 24, 25, 27, 23, 31, 30, 34, 35 3. 104, 108, 109, 111, 115, 117, 118, 119, 121, 122, 122, 126, 127, 128, 129, 133, 134, 135, 137, 139, 139

4. 25 pupils 5. \$35, \$6 6. 1 min 44 sec, 2 min 19 sec

7. Hei	ights of pupils in Room 10	10.	English test results		Mathematics test results
1.3 1.4	9, 5, 9 7, 3, 7, 6, 9, 9, 1 5, 4, 7, 7, 7, 2 1, 6, 2, 3 1.15m 9. 20 pupils		9, 8, 9 7, 8, 4, 5, 3 8, 5, 7, 2, 9, 7, 6 0, 1, 8, 7, 2 4, 1, 9, 5, 5 0	1 2 3	7, 5, 1, 2, 4, 0, 3 5, 8, 9, 0, 1, 2, 5,

11. In both tests the lowest mark was 8 and the highest mark was 50. However, in the Mathematics test there were three pupils who scored 50, whereas only one pupil scored 50 in the English test. Overall there were more scores in the 30's and 40's in the Mathematics test, than in the English test.

Creating pictograms:

Worksheet 9

As the name implies, **pictograms** are created using pictures to represent data. All pictogram should have ...

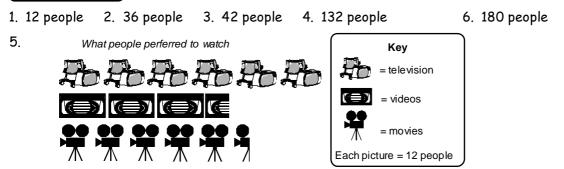
a title or name a key a scale stating how much each picture is worth

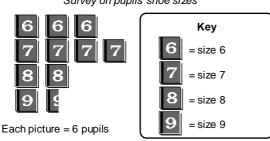
Each picture represents a certain number of data items and part pictures can also be used, therefore the number of pictures drawn for pictogram questions will vary depending on the value of each picture.

In **Task 14** pupils are to interpret the data displayed as a pictogram and create graphs given the data. Pupils are to collect and present data as pictograms.

In **Task 15** pupils are to create pictograms from the frequency tables created in Task 5, Questions 1 & 4, Worksheet 3. Pupils are to look back at the data they collected during their investigation and graph appropriate data as a pictogram.

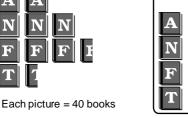
Task 14





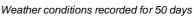
9.

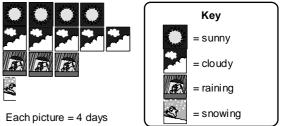
Number of each type of book sold





8.





Task 15

Pictograms using the data from Task 5, Questions 1 and 4.

1. 4. Spelling mistakes made Method of travelling to school by Distance travelled to school by pupils by pupils in Room 10 pupils in Room 9 in Room 9, in kilometres Each picture = 4 pupils Each picture = 2 pupils Key = walk Key 0 = 0 mistakes = bike = 1 mistake = bus = 2 mistakes = car The numbers refer to distance, measured in km. Each number = 2 pupils R = 3 mistakes = 4 mistakes

Worksheet 10

2

Creating dot plot graphs:

A dot plot graph is basically the same as a column graph, where the columns have been replaced by dots. Like the frequency table and stem & leaf graphs, items of data can be added to the graph at any time, in any order, once the axes have been drawn up.

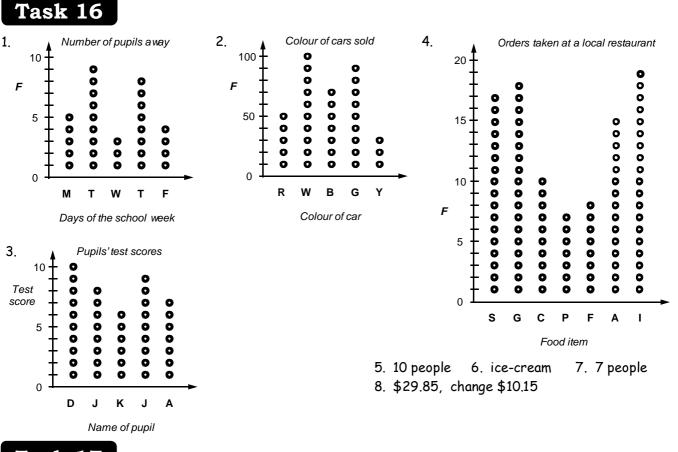
All dot plot graphs should have ...

- □ a name or title
- a scale on the vertical axis
- all dots should be the same size.
- a label oneach axis
- gaps between the dots

In **Task 16** pupils are to organise data and create dot plot graphs, plus answer questions related to the data. Having collected their own data, pupils are to create their own dot plot graphs.

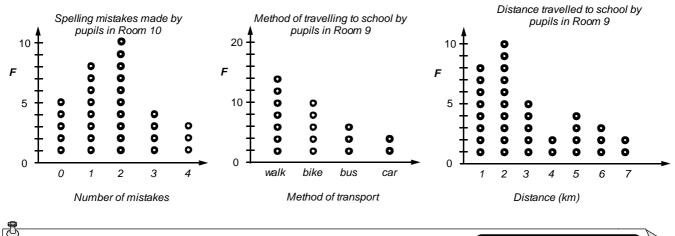
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In **Task 17** pupils are to create dot plot graphs from the frequency tables created in Task 5, Questions 1 & 4, Worksheet 3. Pupils are to look back at the data they collected during their investigation and graph appropriate data as dot plot graphs.



Task 17

Dot plot graphs using the data from Task 5, Questions 1 and 4.



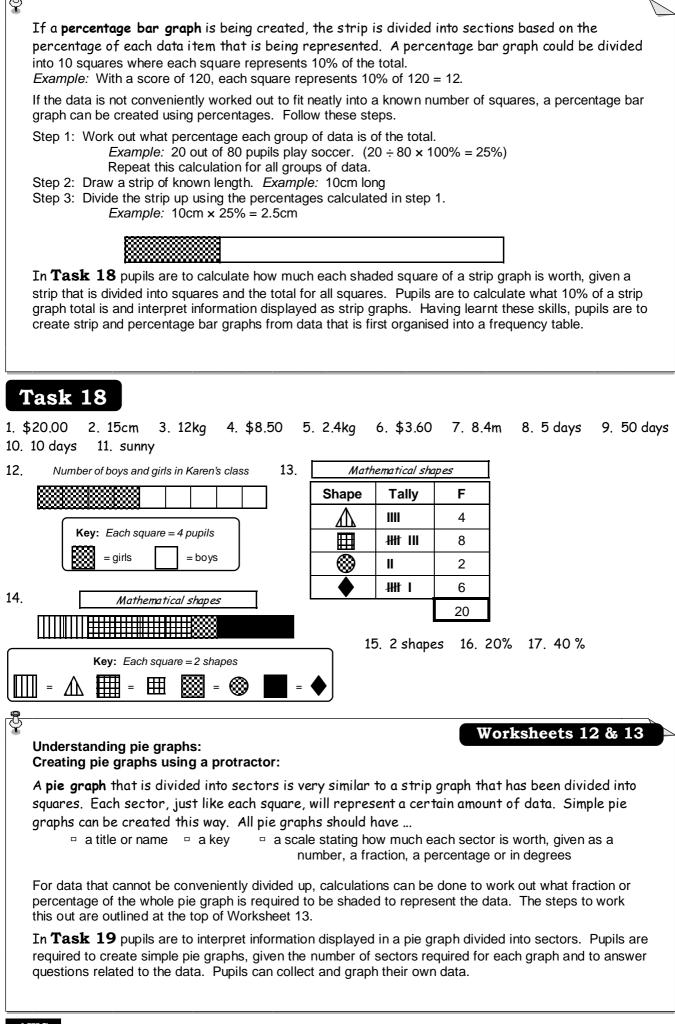
Creating strip graphs / percentage bar graphs:

Worksheet 11

A strip graph is also known as a bar graph or percentage bar graph. The strip graph can be divided into squares, where the squares represent a known number of items. *Example:* A strip graph made of 8 squares, where each square represents 20 items.

All strip graphs or percentage bar graphs should have ...

a title or name
 a key
 a scale stating how much each square is worth (optional)

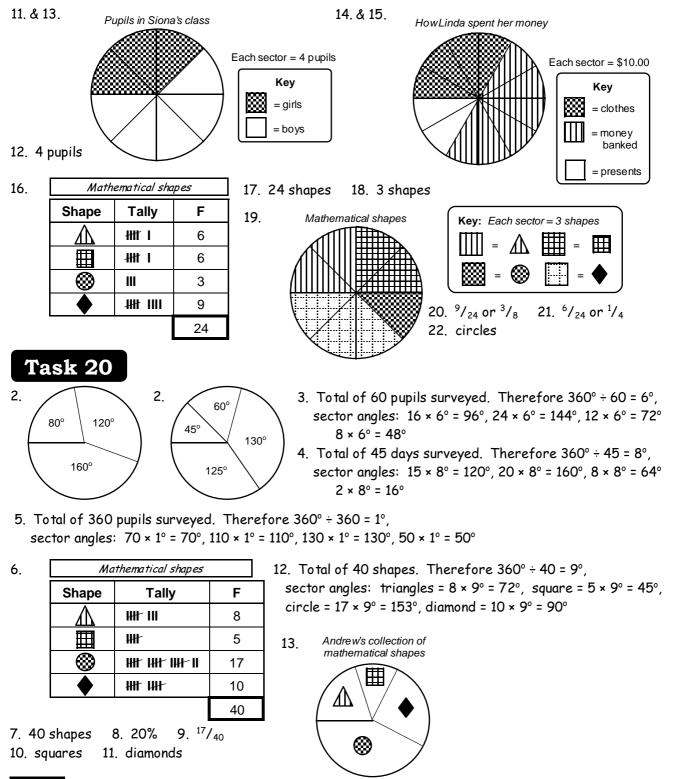


In **Task 20** pupils are to draw accurate pie graphs using protractors to create the sector sizes following the steps outlined at the top of Worksheet 13. Having created the pie graphs, pupils are to answer questions related to the information displayed.

In **Task 21** pupils are to create pie graphs from the frequency tables created in Task 5, Questions 1 & 4, Worksheet 3. Pupils are to look back at the data they collected during their investigation and graph appropriate data as pie graphs.

Task 19

1. 10 sectors 2. $1/_{10}$ 3. 5 days 4. 5 days 5. $2/_{10}$ or $1/_5$ 6. 10 days 7. $4/_{10}$ or $2/_5$ 8. 20 days 9. cloudy 10. winter, because 50% of the time it was raining or stormy



Task 21

Below in the tables are the sector angle calculations, but the pie graphs have not been drawn.

1. F = 30, 360° ÷ 30 = 12°

No.	F	sector angles
0	5	$5 \times 12^{\circ} = 60^{\circ}$
1	8	$8 \times 12^{\circ} = 96^{\circ}$
2	10	$10 \times 12^{\circ} = 120^{\circ}$
3	4	$4 \times 12^{\circ} = 48^{\circ}$
4	3	$3 \times 12^{\circ} = 36^{\circ}$
	30	

4. F = 34, 360° ÷ 34 = 10.6°

F т sector angles walk 14 $14 \times 10.6^{\circ} = 148.4^{\circ}$ bike 10 $10 \times 10.6^{\circ} = 106^{\circ}$ $6 \times 10.6^{\circ} = 63.6^{\circ}$ 6 bus 4 $4 \times 10.6^{\circ} = 42.4^{\circ}$ car 34

D	F	sector angles
1	8	8 × 10.6° = 84.8°
2	10	$10 \times 10.6^{\circ} = 106^{\circ}$
3	5	$5 \times 10.6^{\circ} = 53^{\circ}$
4	2	2 × 10.6° = 21.2°
5	4	$4 \times 10.6^{\circ} = 42.4^{\circ}$
6	3	3 × 10.6° = 31.8°
7	2	2 × 10.6° = 21.2°
	34	

Time-series graphs:

J

Worksheet 14

As the name implies, time-series graphs are used to display data that has been collected over time. Example: temperature, height or weight changes, etc. This type of data is often continuous data as it is obtained by measuring.

All time-series graphs should have ...

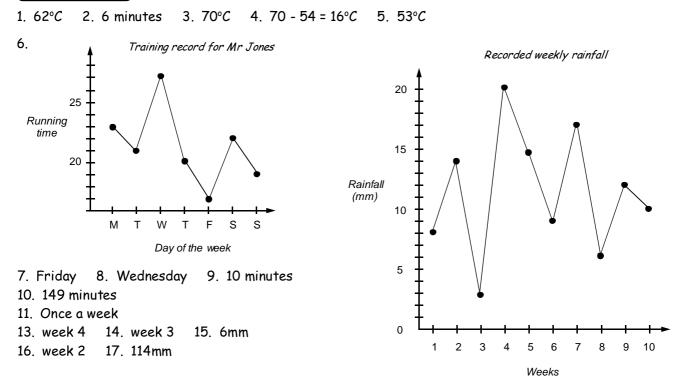
- a title or name

- a label on each axis

- a scale on the vertical frequency axis dots or X to mark points, joined by lines
- time on the horizontal axis

In Task 22 pupils are to interpret a time-series graph, create graphs given the data, and answer questions using the data display. Pupils are to collect and graph their own time-series data.

Task 22



Worksheets 15 to 18

Calculating the mean (average): Calculating the median (middle score): Finding the mode (most common score): Calculating the range (spread):

There are three different 'averages' that can be worked out, depending on the data and what you are trying to find out.

The **mean** is commonly known as the 'average'. To find the mean, add up all the scores and divide by the total number of scores, including any zeros that are among the scores.

The **median** is the middle score or half way between the two scores in the middle, once the scores have been placed in numerical order from smallest to largest.

The mode is the most common score. There can be more than one mode or no mode at all.

The **range** is a measure of how spread out the scores are. It is calculated by finding the difference between the highest and the lowest scores.

In **Task 23** pupils are to calculate the **mean**, given a list of scores, and solve word problems involving finding the mean.

In **Task 24** pupils are to calculate the **median**, given a list of scores, and solve word problems involving finding the median.

In **Task 25** pupils are find the **mode**, given a list of scores, and solve word problems involving finding the mode.

In **Task 26** pupils are to calculate the **range**, given a list of scores, and solve word problems involving finding the range.

Task 23

π,

1. 92. 83. 144. 85. 96. 107. 58. 7.89. 4.310. 2.411. 12.612. 114.513. \$4.6514. \$5.4015. \$3.2616. 9 turns17. 50 seconds18. 16 seconds19. 10 boxes20. 702g21. 22g22. 8 cars23. \$1125024. \$12400

Task 24

1.14 2.15 3.11 4. 17.5 5. (0, 3, 6, 8, 9, 14) 7 6. (2, 4, 6, 6, 7, 9, 10, 11, 14) 7 7. (4, 6, 8, 9, 10, 14) 8.5 8. (1.3, 1.6, 1.7, 1.9, 1.9) 1.7 9. (2.1, 2.3, 2.4, 2.7, 2.9) 2.4 10. (0.4, 0.6, 1.9, 3.4) 1.25 11. (5.0, 6.1, 7.6, 8.9) 6.85 12. (11.7, 12.6, 14.3, 19.4) 13.45 13. (117, 129, 129, 132, 139, 141) 130.5 14. (3.7, 5.6, 7.6, 11.9, 12.6, 14.6) 9.75 15. (3.04, 3.08, 3.45, 3.64, 3.95) 3.45 16. 6 runs 17. (1.4, 1.5, 1.6, 1.8, 1.9, 2.4) 1.7km 18. 1km 19. 10 boxes 20. (995, 995, 996, 999, 1006, 1008, 1009, 1009, 1012, 1014) 1007 21. 19a 22. 18 holes 23. (3, 3, 4, 4, 4, 5, 5, 5, 5, 5, 6, 6, 6, 7, 7, 7, 8, 8) 5 24. 5 stokes 25.98

Task 25

1. 5, 9 2. 6 3. 3 4. no mode 5. 15, 23 6. 9 7. 8, 9, 10 8. no mode 9. 35 10. 1.3 11. 2.3, 4.2 12. no mode 13. 12.01 14. 1 15. 2

19.

16.

Juice cartons sold					
Volume	Tally	F			
250mL	##F #F	13			
600mL	JHH- IHH-1	11			
1000mL	HHT III	8			
		32			

17. 250mL cartons 18	. 32 cartons
----------------------	--------------

Length of telephone toll call (minutes)									
Time	12	13	14	15	16	17	18	19	20
F	4	1	3	8	4	3	3	6	4

20. 15 minutes 21. 36 calls

Task 26

Ψ

1. 19 2.25 3.8 4.24 5.19 6.13 7.18 8.0.8 9. 0.7 10. 3.1 11. 4.7 17. \$145 12. 7.2 13.26 14. 10.5 15. 0.8 16. 5 bicycles 18. \$244 19. 10 cans 20. 9g 21. (330, 332, 333, 334, 334, 335, 337, 338, 338, 339) 334.5q 22. 18 holes 23.5 27, 105 24. 4. 5 25. 96 shots 26. 84 28. 21 and 47

Interpreting data displays: Creating a statistical report: Misleading data displays:

The whole purpose of creating a data display, doing calculations using the data, is to convey a message or prove or disprove a statement. A data display tells a story about the data and being

able to interpret that story is an important skill.

Task 27 is a revision exercise where pupils are to interpret various data displays.

In **Task 28** pupils are to look at and talk about data displays that have been collected from newspapers or magazines, discussing the features that make the displays stand out.

In **Tasks 29 to 31** pupils are presented with some data. Using all the skills they have previously learnt about creating data displays and doing calculations using the data, pupils are to create a statistics report to prove or disprove a statement about the data.

Task 27

- 11 teachers do have white cars and while it was the most common car colour, 24 teachers did not have white cars. It is therefore incorrect for Anna to say that 'most' teachers have white cars as 11 out of 35 only 31.4% of teachers.
- 2. David is correct in that three pupils in his class did score 20, whereas only one from Room 5 scored 20. The range for both classes is also the same (20 - 7 = 13). However, looking at the distribution of scores, Room 5 had more pupils score in the 10's than Room 4 did. The mean for Room 4 marks was 11.2 (1 dp) and the mean for Room 5 was 14.8 (1 dp), further proving that David's statement is incorrect.
- 3. Sally's statement is incorrect. The scale on the vertical axis does not start at zero, but starts at 10. From the graph we can see that there are 15 boys and 20 girls.
- 4. For similar reasons as in question 1 above, most pupils do not have hazel eyes as only 33.3% of all pupils have hazel eyes. That means that 66.6% do not. In Room 7, hazel is the most common eye colour, but that does not mean that 'most' pupils have hazel coloured eyes.

Task 29

For this task various graphs and calculations could be done; below are some examples.

John does have the faster lpas times for all three courses, but does that make him a better driver. Calculating the **range** and **mean** would be useful.

 Range for John's lap times

 Course A: 71 - 59 = 12 sec

 Course B: 137 - 115 = 22 sec

 Course C: 55 - 41 = 14 sec

 Mean for John's lap times

 Course A: 65.6 sec

 Course B: 126.4 sec

 Course C: 45.8 sec

 Range for Rangi's lap times

 Course A:
 70 - 60 = 10 sec

 Course B:
 135 - 117 = 18 sec

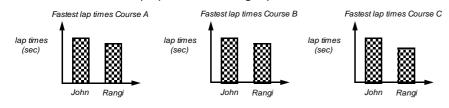
 Course C:
 50 - 36 = 14 sec

Mean for Rangi's lap times Course A: 63.8 sec Course B: 125.4 sec Course C: 43.8 sec Looking at the range values, Rangi's is the more consistent driver as his range values are less than those for John's lap times. Also Rangi's mean lap times for all courses are better than those of Rangi.

Worksheets 19 to 21

Who is the 'better' driver?

This data could be displayed as column graphs (not drawn to scale), such as



Similar column graphs could be drawn to display mean lap times and range values.

Conclusion: While John does have the faster lap times for all courses, Rangi has the more consistent lap times has his range values are narrower and his mean lap times are fastest. Based on these calculations, John's statement is incorrect, therefore Rangi is the better driver.

Task 30

Possible displays and calculations that could be done, as you consider the restaurant owner's statements:

Group size: Organise data into a frequency table and then draw a graph.

Calculate the mean, median and mode for group size.

Mean = 30 ÷ 8 = 3.75 people, Median (2, 2, 3, 3, 4, 5, 5, 6) = 3.5 people, Mode = 2, 3 & 5

Choice of main meal: Organise data into a frequency table and then draw a graph.

Cost per meal per person: Calculate the mean cost of a meal. Total cost of all meals = \$645. Total number of meals = 30 Mean cost = \$645 ÷ 30 = \$21.50

Meal	F
chicken	11
fish	7
beef	8
pork	4

Length of time spent at the restaurant: Draw column or dot plot graph. Calculate the mean, median and mode times.

Mean = 28hrs ÷ 8 = 3.5hrs, Median $(1\frac{1}{2}, 2\frac{1}{2}, 3, 3\frac{1}{2}, 4, 4, 4\frac{1}{2}, 5) = 3\frac{3}{4}$ hrs, Mode = 4hrs

Conclusion: To summarise the results, the average number of people per group is 3.5, the most popular main meal is chicken. The average cost per person is \$21.50 and the groups stay for an mean (average) time of 3.5 hours. Based on these results, the restaurant owner was about right for group size, cost per person per meal and length of stay, but was incorrect in his choice of the most popular main meal.

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                                                                         Worksheets 21 to 25
   Understanding probability words:
   Calculating relative frequency / probability scales:
   Finding outcomes using grids:
   Finding outcomes using tree diagrams:
   Using probability to predict outcomes:
   Probability is a measure of the chance of how likely something will happen. Different words can be
   used to describe the chance of something happening and there are several probability calculations
   that can be performed. Some important probability words include experiment, trial, outcome &
   event.
   The rolling of a die, the drawing of a card are called experiments. When a die is rolled it is called
   a trial. An outcome is the result of an experiment. Finding all possible outcomes can be a
   challenge. An event is one of the possible outcomes.
   In Task 32 pupils are to use probability words to describe the likelihood of events happening.
   In Task 33 pupils are to calculate the relative frequency of something happening. Relative
   frequency can also be known as experimental probability. The relative frequency is worked out on
   actual results of an experiment.
                                              Number of times the event occurs
                     Relative frequency =
                                                    Total number of trials
```

Having calculated the relative frequencies of various events, these results are to be displayed on a probability scale.

In **Tasks 34 & 35** pupils are to work out all possible outcomes for an experiment or situation in a systematic way using a simple grid or tree diagram. Pupils are to use information they have calculated to work out various questions associated with the data.

In **Task 36** pupils are to work out the probability of events happening, based on data contained in tree diagrams, frequency tables or lists. Having worked out the probability values, pupils are to use this information to predict what they would expect to happen, given a larger population.

Task 32

J

2. D, E, A, C, B

For questions 3 to 22, some answers will vary depending on the pupils and the time of the year, therefore no answers have been given. Discuss each question with your class, explaining why different answers are acceptable.

Task 33

2. 60 trials 3. ¹³/₆₀ 4. TT 1. HH = 13, HT = 17, TH = 19, TT = 11 5. $^{36}/_{60}$ or $^{3}/_{5}$ 6. ŀ **†**† impossible certain HT & TH TT HH 10. Mathematical shapes 11. circle = $\frac{15}{40}$, square = $\frac{5}{40}$, triangle = $\frac{9}{40}$, diamond = $\frac{11}{40}$ 12. Shape Tally F HH IIII 9 ۸N impossible certain Ħ łłłł 5 ŧ \odot 15 Α В С D HH HH I 11 40 <u> Task 34</u> 1. 3. 5. С Т R В G Sb R W BI В G RC RSb Ρ PR PB PG Ρ PR PG PW R RT PB PBI YR YB Sc ScC ScRb ScT Υ YG Υ YR YB YG YW YBI OR OB OG 0 0 OR OB OG OW OBI BrR BrB BrG BrW BrBl Br (rugby, cricket), (rugby, softball), (rugby, tennis), (soccer, cricket), (soccer, softball), (soccer, tennis). 4. (purple, red), (purple, blue), (purple, green), (yellow, red), (yellow, blue), (yellow, green), (orange, red), (orange, blue), (orange, green)

(purple, red), (purple, blue), (purple, green), (purple, white), (purple, black), (yellow, red), (yellow, blue), (yellow, green), (yellow, white), (yellow, black), (orange, red), (orange, blue), (orange, green), (orange, white), (orange, black), (brown, red), (brown, blue), (brown, green), (brown, white), (brown, black)

М	BF	BH	
М	TF	ΤН	9.
М	CF	СН	
	M M	M TF	M TF TH

. (bacon & eggs, milo), (bacon & eggs, fruit juice), (bacon & eggs, hot choc), (toast & jam, milo), (toast & jam, fruit juice), (toast & jam, hot choc), (cereal, milo), (cereal, fruit juice), (cereal, hot choc) . \$5.50 10. \$14.50 11. Toast & jam, milo

7.

12.

Μ ۷ Ρ F

М	т	W	
MM	МТ	MW	

ММ	МТ	MW	МТ	MF	MS	MS
VM	VT	VW	VT	VF	VS	VS
РМ	PT	PW	PT	PF	PS	PS
FM	FT	FW	FT	FF	FS	FS

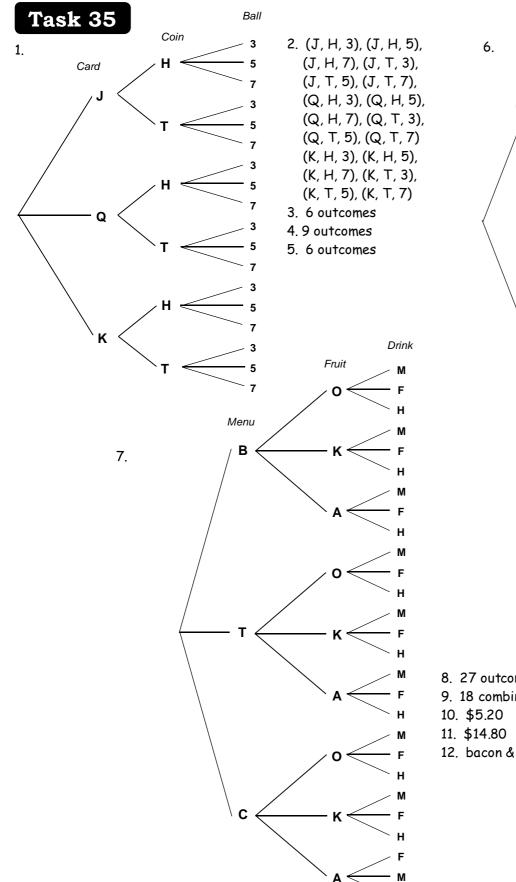
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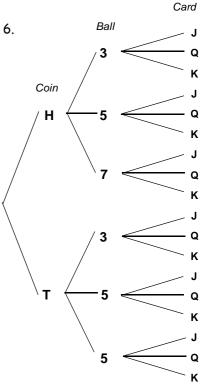
F

S

S

13. 28 outcomes 14. reduces the outcomes by 8, therefore only 20 outcomes





8. 27 outcomes or choices

9. 18 combinations

н

12. bacon & eggs, an apple, fruit juice

Task 36

1. (H,H), (H,T), (T,H), (T,T) 2. 1 out of 4 or $\frac{1}{4}$ 3. 1 out of 4 or $\frac{1}{4}$ 4. 2 out of 4 or $\frac{1}{2}$ 5. $\frac{1}{4}$ of 100 = 25 times 6. 300 times 7. 1 out of 6 or $\frac{1}{6}$ 8. 3 out of 6 or $\frac{1}{2}$ 9. 2 out of 6 or $\frac{1}{3}$ 10. $\frac{1}{6}$ of 60 = 10 times 11. $\frac{1}{2}$ of 200 = 100 12. 120 drinks 13. $\frac{50}{120}$ or $\frac{5}{12}$ 14. $\frac{15}{120}$ or $\frac{1}{8}$ 15. flavoured milk 16. 60 Fanta drinks 17. 15 ginger beer drinks

-	0	
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-	υ.	

Music choices	Tally	F
rock	HHT HHT II	12
jazz	HH HH	9
country & western	HH HH	8
classical	HH HH I	11
		40

 F
 19. ¹²/₄₀ or ³/₁₀
 20. ¹¹/₄₀

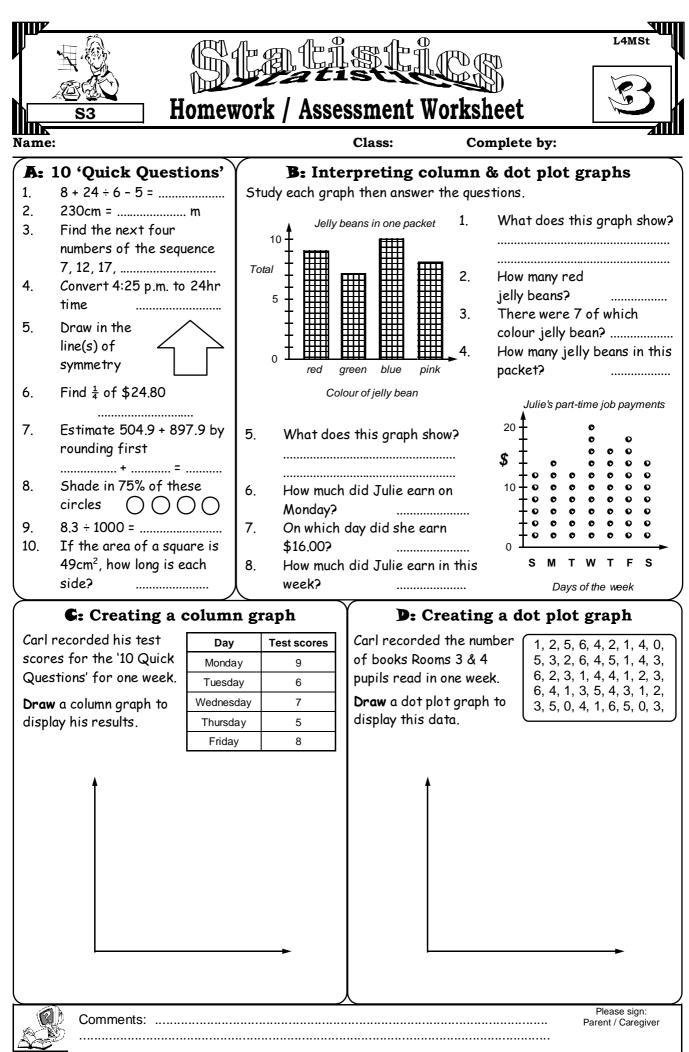
 II
 12
 21. rock = 120, jazz = 90, country & western = 80, classical = 110

Table of Contents for the Homework / Assessment Worksheet Masters for Statistics, Level 4

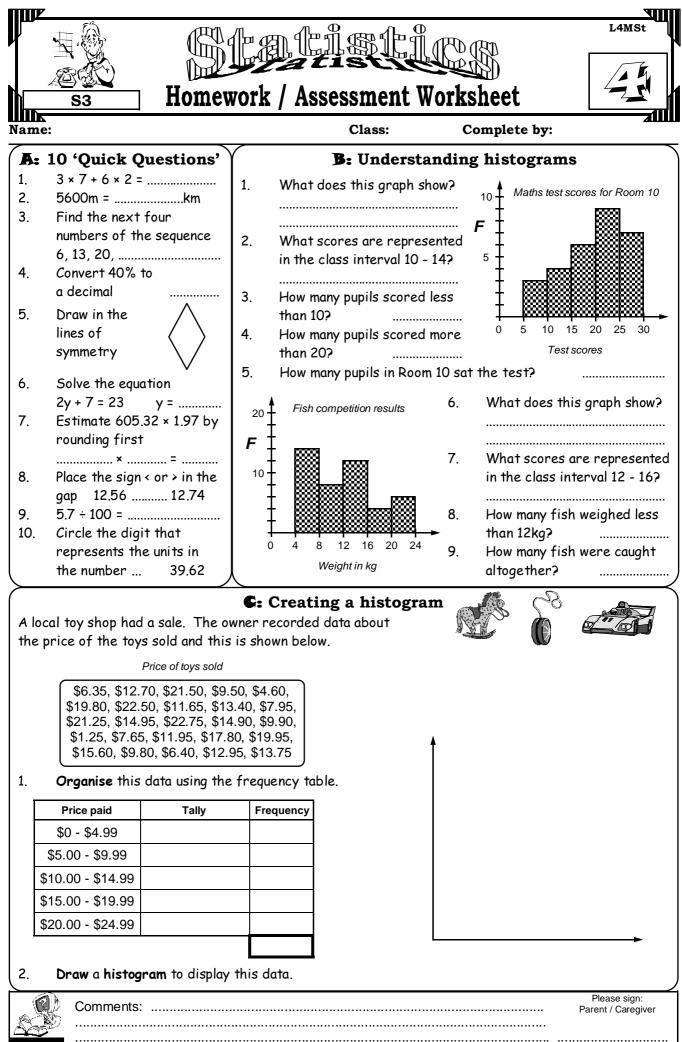
Worksheet Number	Торіс	Statistics Objective(s)
1	Statisitical words / Designing a questionnaire / What would you investigate?	S1
2	Types of data / frequency tables / More frequency tables / Collecting data	S2 / S3
3	Interpreting column & dot plot graphs / Creating a column graph / Creating a dot plot graph	S3
4	Understanding histograms / Creating a histogram	S3
5	Understanding stem & leaf graphs / Creating a stem & leaf graph	S3
6	Understanding pictograms / Understanding pie and strip graphs / Creating a pictogram, a strip graph and a pie graph	S3
7	Creating percentage bar graphs / Pie graph calculations / Creating a pie graph using a protractor	S3
8	Understanding time-series graphs Creating a time-series graph / Collecting data	S4
9	Mean, median, mode & range / Finding the mean / Finding the median / Finding the mode / Finding the range / Word problems	S5
10	Interpreting data displays / Creating a statistical report	S6 / S7
11	Relative frequency / probability scales / Experiment & investigation	S8
12	Listing outcomes / Creating a tree diagram / More outcomes / Creating a grid diagram	S9
13	Using probability to predict outcomes / probability	S9
	Answers	

	L in	T
И		
	si Homev	work / Assessment Worksheet 🛛 🛛 🚣
Name:	:	Class: Complete by:
	10 (Outol: Outors)	B: Statistical words
1.	10 'Quick Questions' 7 + 4 × 9 + 5 =	Complete these sentences, using the words listed in the box.
2.	Calculate 15 ² =	1. In statistics, a group of anything such as the trees in your
3.	Find the next four	garden is called a
	numbers of the sequence	2. Ais part of the population
	3, 9, 15,	we are interested in.
4.	Convert $\frac{3}{4}$ to	3. If we wish to comment about a population, we often
	a percentage	a population or a sample of the population
5.	Find the missing $/x$	4. For the results of a survey to apply to the whole population,
	angle X	the sample must be a
	X =	5. A sample that is not a representative sample is called a
6.	Find 1/4 of \$36.80	
		6. A sample means that every person, or
7.	Estimate 398.86 ÷ 3.95 by	item, has an equal chance of being chosen.
	rounding first	7. Ais one way to obtain
	÷ =	people's opinions. (sample questionnaire population survey)
8.	Shade in 66.6 % of these	
	circles 000	random biased representative sample
9.	9.3 ÷ 1000 =	G: Designing a questionnaire
10.	If the perimeter of a	A questionnaire is used when we are asking opinions about an issue.
	square is 36cm, how long	The design of a questionnaire is important. List 4 points that you
	is each side?	should consider when designing a questionnaire.
	- What would you	1
	• What would you	
	investigate?	
What	investigate?	2.
	t issues in your school,	
comm	t issues in your school, nunity, town, city or country	2.
comm	t issues in your school, nunity, town, city or country rou interested in or worried	3.
comm are ye	t issues in your school, nunity, town, city or country rou interested in or worried	
comm are ye	t issues in your school, nunity, town, city or country rou interested in or worried	3.
comm are ye	t issues in your school, nunity, town, city or country rou interested in or worried	 3. 4. A new teacher wants to find out more about
comm are ye	t issues in your school, nunity, town, city or country rou interested in or worried	 3. 4. A new teacher wants to find out more about the pupils in his /her class.
comm are ya about	t issues in your school, hunity, town, city or country ou interested in or worried	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask,
comm are yo about	t issues in your school, nunity, town, city or country ou interested in or worried	 3. 4. A new teacher wants to find out more about the pupils in his /her class.
comm are yo about	t issues in your school, nunity, town, city or country ou interested in or worried t? Three issues you are erned about in order of	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask, that require a 'yes / 'no' answer. 5.
comm are yo about	t issues in your school, nunity, town, city or country ou interested in or worried	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask, that require a 'yes / 'no' answer. 5. 6.
comm are ya about List conce	t issues in your school, nunity, town, city or country ou interested in or worried t? Three issues you are erned about in order of	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask, that require a 'yes / 'no' answer. 5. 6. 7.
comm are ya about List conce	t issues in your school, nunity, town, city or country ou interested in or worried t? Three issues you are erned about in order of	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask, that require a 'yes / 'no' answer. 5. 6. 7. Write a question that this teacher might ask , that requires a
comm are ya about List conce	t issues in your school, nunity, town, city or country ou interested in or worried t? Three issues you are erned about in order of	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask, that require a 'yes / 'no' answer. 5. 6. 7. Write a question that this teacher might ask , that requires a choice of answers. Include the choice of answers for your question
comm are ya about List conce	t issues in your school, nunity, town, city or country ou interested in or worried t? Three issues you are erned about in order of	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask, that require a 'yes / 'no' answer. 5. 6. 7. Write a question that this teacher might ask , that requires a
comm are ya about List conce	t issues in your school, nunity, town, city or country ou interested in or worried t? Three issues you are erned about in order of	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask, that require a 'yes / 'no' answer. 5. 6. 7. Write a question that this teacher might ask , that requires a choice of answers. Include the choice of answers for your question
comm are ya about List conce	t issues in your school, nunity, town, city or country ou interested in or worried t? Three issues you are erned about in order of	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask, that require a 'yes / 'no' answer. 5. 6. 7. Write a question that this teacher might ask , that requires a choice of answers. Include the choice of answers for your question
comm are ya about List conce	t issues in your school, hunity, town, city or country ou interested in or worried the state of the state of	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask, that require a 'yes / 'no' answer. 5. 6. 7. Write a question that this teacher might ask , that requires a choice of answers. Include the choice of answers for your question
comm are yo about	t issues in your school, nunity, town, city or country ou interested in or worried t? Three issues you are erned about in order of	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask, that require a 'yes / 'no' answer. 5. 6. 7. Write a question that this teacher might ask , that requires a choice of answers. Include the choice of answers for your question 8.
comm are yo about	t issues in your school, hunity, town, city or country ou interested in or worried the state of the state of	 3. 4. A new teacher wants to find out more about the pupils in his /her class. Write three questions that this teacher might ask, that require a 'yes / 'no' answer. 5. 6. 7. Write a question that this teacher might ask , that requires a choice of answers. Include the choice of answers for your question 8. Please sign:

	<u>s2 / s3</u> Homev	ork / Assessment Worksheet
Name	:	Class: Complete by:
A: 1. 2. 3. 4. 5. 6. 7. 8. 9. 10.	10 'Quick Questions' 15 - 3 × 4 + 9 = Convert 435mm to cm . Change 15:45 in 24hr time to a.m or p.m. time Calculate 2 ³ Find the missing angle X 151° X X = Find $\frac{1}{2}$ of \$39.50 Estimate 97.56 × 10.53 by rounding first 	 B: Types of data / frequency tables There are two types of data that can be collected, discrete data and continuous data. Complete these sentences using these words. Data that is obtained by counting is called data. Data that is obtained by measuring is called data. Sally recorded the number of library books each pupil in Rooms 4 and 5 read in one week. Organise this data in the frequency table below. Number of books each pupil reads Number of books each pupil reads 1, 3, 4, 2, 3, 1, 2, 4, 3, 2, 4, 4. Number of books read? How many pupils read at least 3 books? How many pupils in Rooms 4 and 5?
avoid The [.]	G: More freq n there is large range of data l having too many rows in the f following data shows the numb to create some models.	scores, data can be grouped to requency table. If you are at school or at home, collect this data about these
10 39 18, 13, 9,	12, 23, 28, 32, 19, 39, , 21, 34, 8, 29, 37, 21, , 26, 11, 38, 9, 29, 26, 16, 24, 35, 40, 16, 26, 24, 36, 34, 26, 27, 18, 23, 27, 34, 40, 16, 21, 5, 11, 26, 13, 24, 8, 38	cks Taily F 0
1. 2. 3. 4. 5.	Organise the data into the f What numbers occur in the group 11 to 20? How many Lego models had no more than 30 blocks? How many Lego models were	requency table. class interval or t least 21 blocks? What was the most common object you counted?
AWS	<u>ن</u>	Please sign: Parent / Caregiver Copyright © ₁₉₉₇ AWS <i>TEACHER RESOURCES</i>



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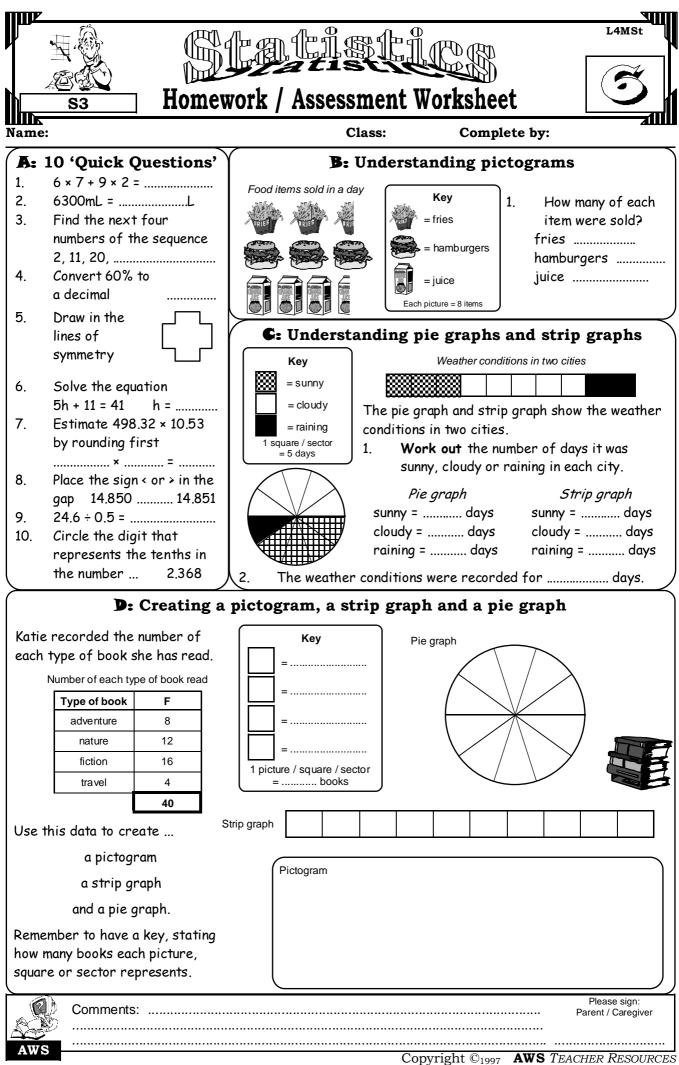


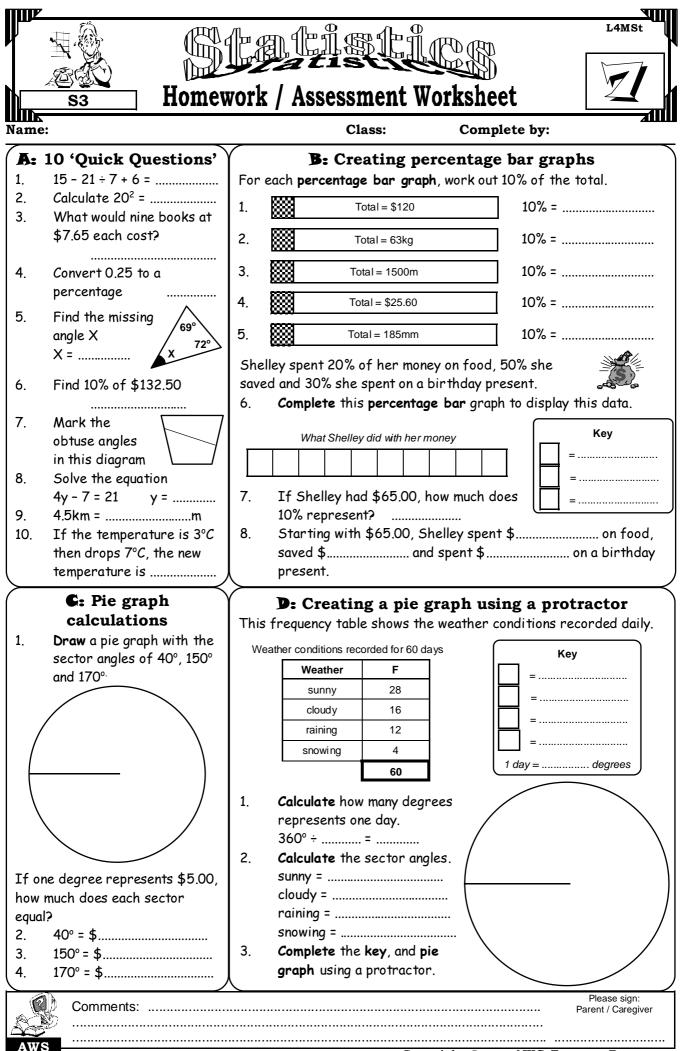
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. 5 . Co . Ro . No . It . So . Fi . Fi . ar	• Quick Questio × 8 - 7 × 4 = alculate $\sqrt{225}$ = ound \$16.76 to the earest dollar f the perimeter of a quare is 12cm, what is ne area?	····· 1. ···	What doe			Complete by: tem & leaf gi	aphs
. 5 . Co . Ro . No . It . So . Fi . Fi . ar	× 8 - 7 × 4 = alculate $\sqrt{225}$ = ound \$16.76 to the earest dollar f the perimeter of a quare is 12cm, what is	····· 1. ···	What doe		•	tem & leaf gi	aphs
2. So 3y to to 9 9 9. 1,1 0. M th	ind the missing ngle X = olve the equation $y - 5 = 13$ $y = hange 09:25 in 24hr to a.m or p.m. time ace the sign < or > in ap 17.07517.0 2 \times 0.9 =leasure the length ofmis line to the nearest$	112° 4. 5. ime the 79 8.	test? List the s this grap ,	s the top scores rep h. y pupils so y pupils in arrace (seco 0, 9, 3 1 9 s the slow the fastes fastest 1	cored above Room 7? onds) 6. 7. vest lap time st and slowe	 1 2, 3, 9, 8 7, 3, 7, 9 3 8, 4, 3, 1 4 0, 0 9 20? What does this What was the formula to th	- <i>pupils in Room 7</i> 3, 3, 1 9, 4, 7, 2 1, 6, 7, 2, 0 <i>graph show?</i> <i>graph show?</i> <i>astest lap time</i> <i>minutes and</i>
The tes Eng 19, 20 48, 30 31, 42	Room 7 had an Englis ts were marked out o glish test scores 5, 38, 41, 50, 50, 5, 24, 18, 18, 29, 2, 46, 35, 24, 29, 28, 24, 31	Mathemati 19, 27, 25 50, 27, 26 12, 38, 50		ntics test nown belou 1. 2. 3.	last week. w. Organise th stem & leaf What are th scores for English: Mathematic Look at the	nis data as a bac graph. he highest and lo	owest , , ph you have

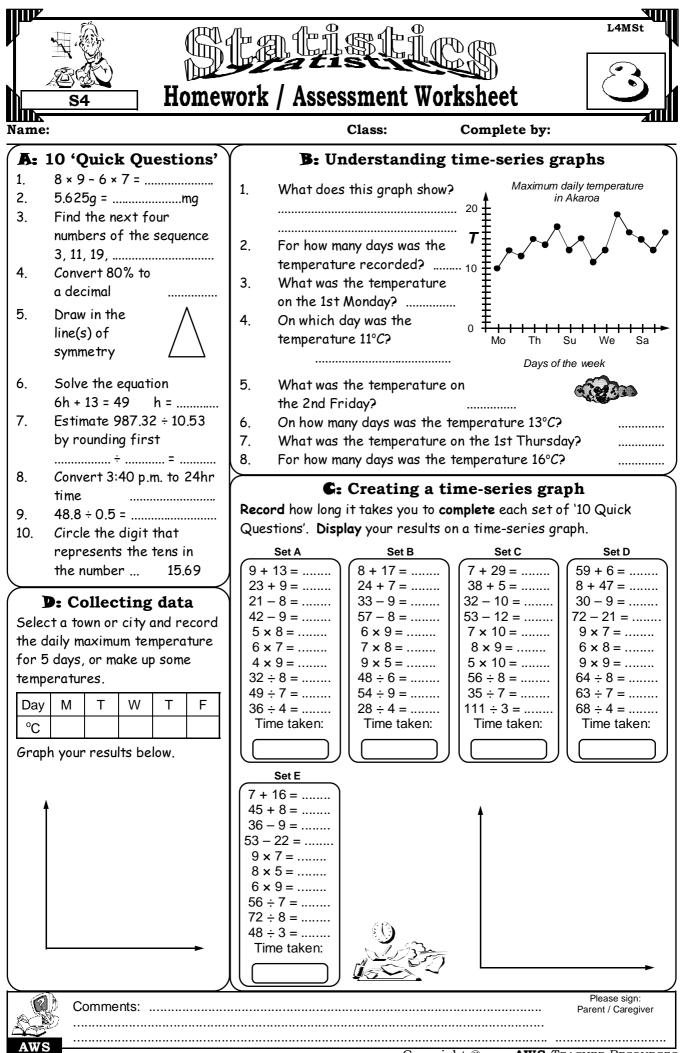
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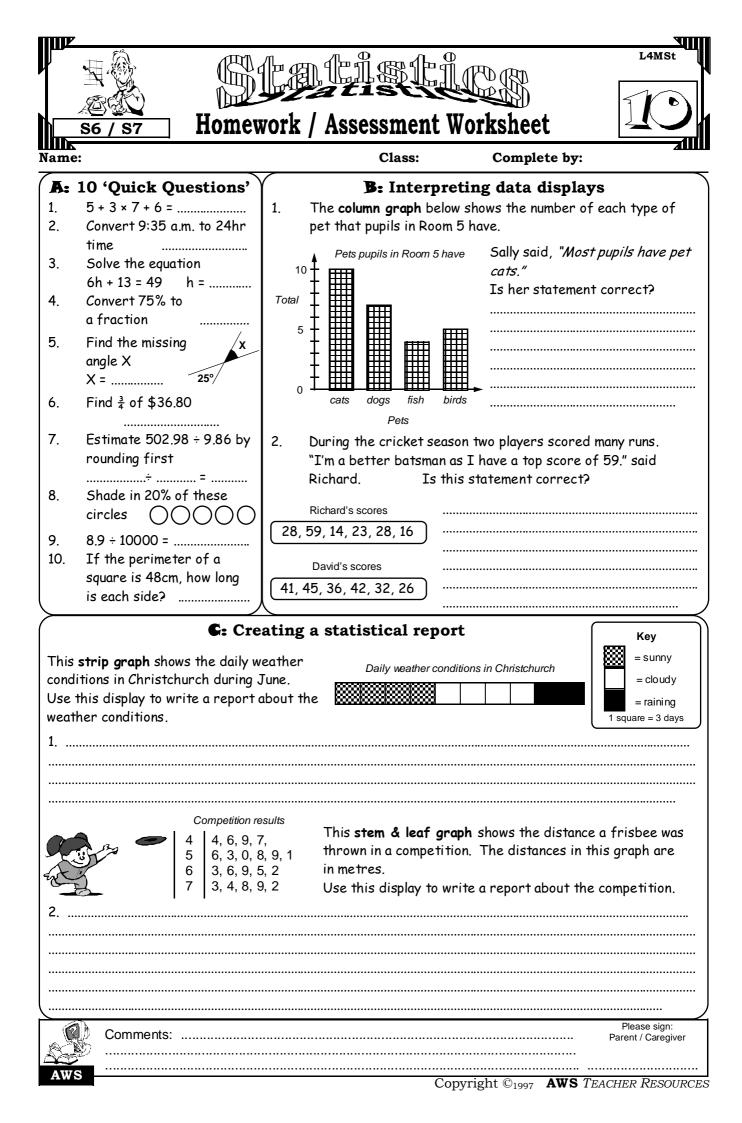
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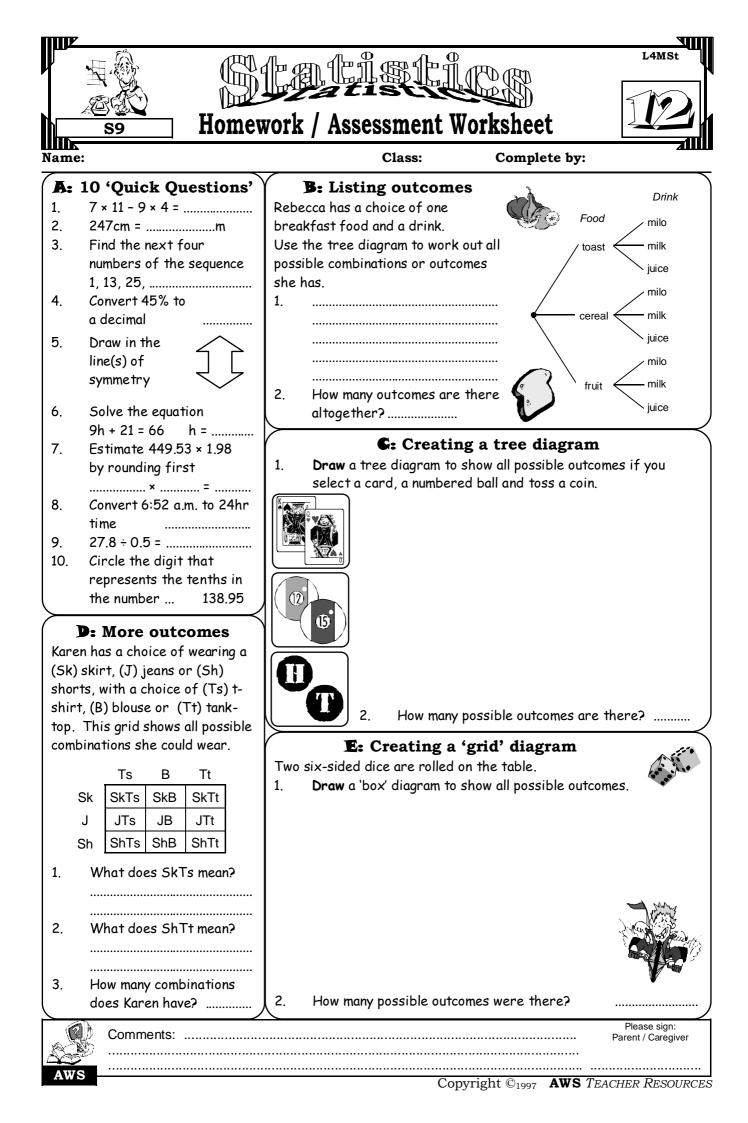
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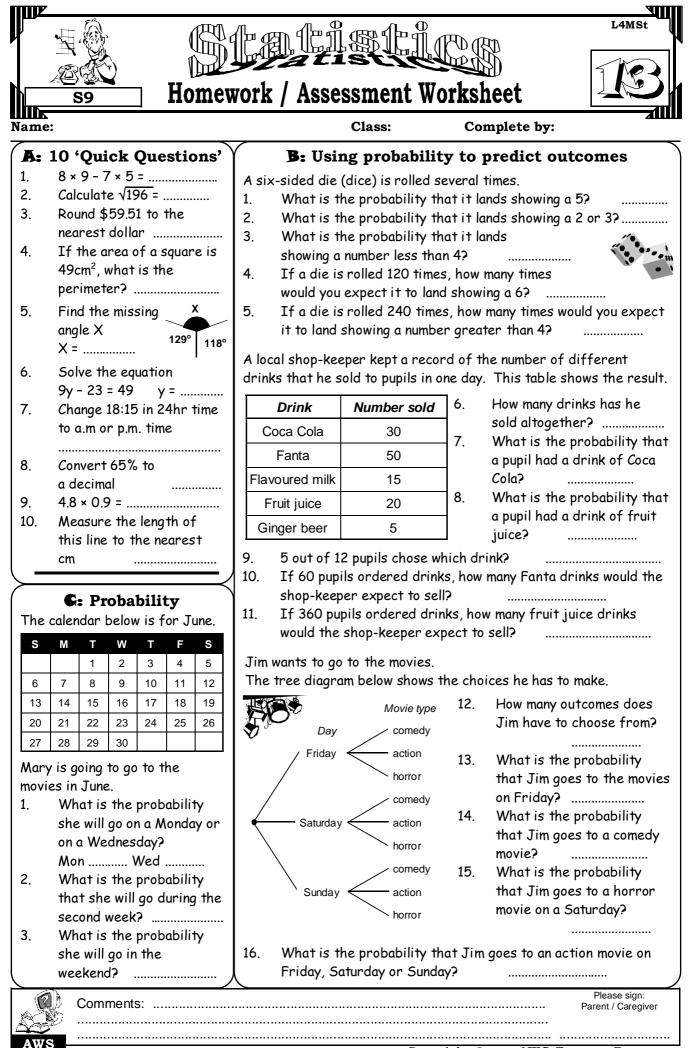
			
			L4MSt
		work / Assassment Worksheet	
	<u>ss</u> nomev	work / Assessment Worksheet	
Name): :	Class: Complete by:	
A :	10 'Quick Questions'	B: Mean, median, mode & range	
1.	21 - 36 ÷ 4 + 9 =	Fill in the missing words from the box, to complete these	sentences.
2.	Calculate 1.2 ² =	1. To find the 'average' or for a lis	tof
3.	What would 12 books at	scores, first add up all the scores, then divide by	the
	\$4.95 each cost?	number of scores you added up.	
		2. The middle score, once the scores are placed in ord	
4.	Convert 0.65 to a	smallest to biggest, is called the	
	percentage	3. The most common score is called the	
5.	Find the missing	There may be more than one or none at all.	
	anale X ⁵ /67°	4. The highest score — lowest score is called the	
	$X = \dots \qquad X \xrightarrow{73^{\circ}}$	range mode median mean	
			\longrightarrow
6.	Find 20% of \$147.50	C: Finding the mean	
-	AA 1. : .1	Find the mean for each list of scores.	
7.	Mark in the	1. 8, 10, 12 2. 7, 7, 10, 12	
	acute angles	3. 4, 9, 5, 6, 8, 4 4. 5, 8, 6, 4, 3, 5,	4
	in this diagram	5. 14, 12, 11, 17 6. 7, 104, 66, 33	
8.	Solve the equation	D: Finding the median	
	9y - 12 = 24 y =	Find the median for each list of scores.	
9.	5265g =kg	Remember the scores must be in order.	T E
10.	If the temperature is 8°C	1. 7, 9, 11, 13, 15 2. 5, 8, 10, 15, 18	•
	then drops 10°C, the new	1. 7, 9, 11, 13, 13 2. 3, 0, 10, 13, 13 3. 9, 12, 16, 17 4. 13, 19, 21, 25	
\square	temperature is	5. $6, 18, 21, 11, 13$,	
F	: Finding the range	6. 7, 3, 11, 5, 9, 12,,,, media	
	the range for these lists of		<u> </u>
scor	-	E: Finding the mode	·
1.	2, 5, 8, 12, 14	Find the mode for each list of scores.	
2.	17, 3, 11, 1, 9	1. 4, 4, 6, 8, 10, 9 2. 8, 7, 5, 8, 6, 7	
3.	8, 0, 12, 21, 4	3. 4, 12, 11, 7, 3 4. 3, 8, 10, 5, 6, 8	, 6
4.	13, 27, 41, 34, 9	5. 5, 5, 7, 8, 9, 11, 7 6. 3, 8, 9, 4, 5, 11	, 9
5.	Five houses were sold for		
	the following prices:	G: Word Problems	" "
	\$152000	In the first nine holes of golf, Greg recorded the	
	\$198500	following scores. (4, 5, 4, 7, 8, 4, 3, 4, 6)	(Star) d
	\$156900	1. Find his mean score.	har for in
	\$147990	2. What was the range of his scores?	
	\$178500	3. What was the mode score?	
	Calculate the range of the	4. List the scores from lowest to highest.	
	house prices	5. What was the median for his golf scores?	•
6.	If the dearest house sold	In the next nine holes, Greg recorded the following scores.	
	for \$205400 and the	(4, 3, 7, 7, 3, 5, 6, 4, 5)	
	range was \$67900, what	6. Combine the two sets of nine scores to find the new m	edian
	would the cheapest house	6. Combine the two sets of nine scores to find the new m	
l	sell for?	New median =	
			lease sign:
	all -	Pare	nt / Caregiver
AW	5		

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		Catistics	L4MSt
		Talis (111
	ss Homew	ork / Assessment Worksheet	
me	:	Class: Complete by:	
5:	10 'Quick Questions'	B: Relative frequency / probabilit	y scales
	9 × 7 - 8 × 6 =	The relative frequency of an event is the proportion	on or fraction of
	Calculate √169 =	times the event occurs.	Number F
	Round \$29.86 to the nearest dollar	A die is rolled 150 times and the results	1 23
	If the perimeter of a	are shown in this table.	2 25
•	square is 20cm, what is	1. Find the relative frequency of	3 28
	the area?	each number occurring. 1 =	4 21
	Find the missing \mathbf{x}	1 =	5 27
	angle X	5 = 5 =	6 26
	X = ^{131°} 118°		
	•	This frequency table was used to record the results as two coins	Tally F
	Solve the equation 6y - 11 = 25 y =	were tossed.	Ht Htt II
	Change 14:35 in 24hr time		HT HHT I
	to a.m or p.m. time		H+ H+ III
		2 Llow many times were the	
	Convert 40% to	coins tossed?	## ###
	a decimal	4. What is the relative frequency of the event '	ΤΤ'?
	3.6 × 0.8 =	5. Which event had a relative frequency of $17/_{70}$	
).	Measure the length of	6. What is the relative frequency of the	
	this line to the nearest	events 'HT' and 'TH' combined?	
	mm	7. Mark on the probability scale below the ever	its 'TT', 'HH' and
		'HT' / 'TH' combined.	
	G: Experiment &	impossible	certain
	investigation		
	ct a card from a pack of	Michalla has a has of Loop blocks containing diffor	ont colourod
	s 30 times, replacing the	Michelle has a bag of Lego blocks containing different blocks. This table shows how many of each coloured	
	each time. Record the	the bag.	
su	Its in the table below.	(R) red (W) white (B) blue (G) green	n (Y) yellow
he	eart 🛛 🖌 🗛	25 40 15 20	100
liar	mond	8. How many Lego blocks does Michelle have?	
00		9. If a block is selected from the bag, calculate	the relative
	pade	frequency of selecting each colour of block.	
cl	ubs 🔤	red = white =	
150	d on your results, what is	blue =green =	
	relative frequency	yellow =	
	electing each suit?	10. If the relative frequency of selecting a ball is	s 10%, which
	-		
	hearts =	11. Mark on the probability scale below the ever	nts of choosing
	diamonds =	each colour of Lego block.	
	spades =	impossible	certain
	clubs =		
(A			Please sign:
<u> </u>	U Comments:		Parent / Caregiver
, e	J/		





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Homework / Assessment Worksheet

Answers

Worksheet 1

A:

5. 31° 6. \$9.20 7. $400 \div 4 = 100$ 1. 48 2. 225 3. 21, 27, 33, 39 4. 75% 8. 9. 0.0093 10. 9cm B: 1. population 2. sample 5. biased 3. survey 4. representative sample 6. random 7. questionnaire C: Possible answers for questions 1 to 4. ☑ What questions relating to the 'issue/s' are you going to ask? ☑ Do not ask questions that are not important to the issue. ☑ Make the questions clear and concise and not too many of them. \square How are these questions going to be answered? Example: multi-choice, single words, short answers or long answers. ☑ Have you allowed for every possible answer? ☑ Do you need to give instructions as to how the questionnaire has to be filled out? I How are you going to organise and display the data you have collected? Worksheet 2 A: 1. 12 2. 43.5cm 3. 3:45 p.m. 4.8 5. 29° 6. \$19.75 7. $100 \times 10 = 1000$ 8. $\bigcirc\bigcirc\bigcirc$ 9. 5700 10. circle the digit '6' C: B: 1. discrete 2. continuous 1. Number 2. 11, 12, 13, 14, of blocks Tally F 15, 16, 17, 18, 3. Number 4. 2 books F Tally 19, 20 1 - 10 |||| | 6 of books 5. 29 pupils 3. 21 models 11 - 20 ₩1 ₩1 II 12 HHT HHT || 6. 63 pupils 1 12 4. 13 21 - 30 ### ### ### III 2 ### ### ### III 22 18 5. 49 models 31 - 40 ₩+ ₩+ III 13 ₩ ₩ ₩ III 19 3 4 ₩ ₩ 10 49 63 Worksheet 3 A: 1.7 2. 2.3m 3. 22, 27, 32, 37 4. 16:25 5. 6. \$6.20 7. 500 + 900 = 1400 8. 🔿 🌑 🜑 9. 0.0083 10. 7cm B: 1. The number of each colour of jelly beans in one jacket. 2. 9 red 3. green 4. 34 jelly beans 5. Money Julie earned from a part-time job. 6. \$14 7. Thursday 8. \$106 C: D: Number of books read by Carl's 10 Quick pupils in Rooms 3 & 4 10 Question scores 10 Test C C scores Frequency C 0 0 C C O C O C C . o 0 0 C O 0 C . 0

0

2 3 4 5

Number of books read

6

0 1

т Days of the week

W TF

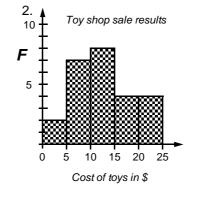
М

A:

- 7. 600 × 2 = 1200 1. 33 2. 5.6km 3. 27, 34, 41, 48 4. 0.40 5. 6. y = 8 8. < 9. 0.057 10. circle the digit 9
- B:

- 2. 10, 11, 12, 13, 14 3. 3 pupils 1. Maths test scores for Room 10 pupils 4. 16 pupils 5. 29 pupils 6. Weights of fish in a fishing competition 7. 12.00kg to 15.99kg 8. 22 fish 9. 44 fish
- C: 1.

Price paid	Tally	Frequency
\$0 - \$4.99	II	2
\$5.00 - \$9.99	HH+ 11	7
\$10.00 - \$14.99	₩¥ III	8
\$15.00 - \$19.99	1111	4
\$20.00 -	1111	4
JIKSHEEL J		25



A:

Ŵ

4. 9 cm² 5. 124⁰ 1. 12 2.15 3. \$17 6. y = 67. 9:25 a.m. 8. < 9. 1.08 10. 43mm B:

1. Test results for pupils in Room 7 2. 40 3. 12, 13, 19, 18, 13, 11, 27, 23, 27, 29, 24, 27, 22, 38, 34, 33, 31,

36, 37, 32, 30, 40, 40 4. 17 pupils 5. 23 pupils

6. Lap times for a car race recorded in seconds 7. 230 seconds 8. 269 seconds

9. fastest time = $3 \min 50 \sec$, slowest time = $4 \min 29 \sec$ 10. 20 cars

C:

1	English test scores		Maths test scores
	English test scores 8, 8, 9 4, 8, 9, 4, 9, 4, 6 1, 5, 1, 6, 8 6, 2, 8, 1 0, 0	1	9, 6
	4, 8, 9, 4, 9, 4, 6	2	7, 5, 7, 6, 6
	1, 5, 1, 6, 8	3	9, 7, 9, 1, 8, 9
	6, 2, 8, 1	4	2, 9, 2, 7, 1
	0, 0	5	0, 0, 0

2. English: 50 & 18, Mathematics: 50 & 16 3. 3 pupils scored 50 out ot 50 for the mathematics test, whereas only one pupil got 50 in the English test. Overall, the Mathematics were better than the English scores as there were more Mathematics scores in the 30's, 40's and 50's.

7. $500 \times 10 = 5000$

8. <

Worksheet 6

A:

2. 6.3L 1. 60 3. 29, 38, 47, 56 4. 0.60 6. h = 65. 9. 49.2 10. circle the digit 3

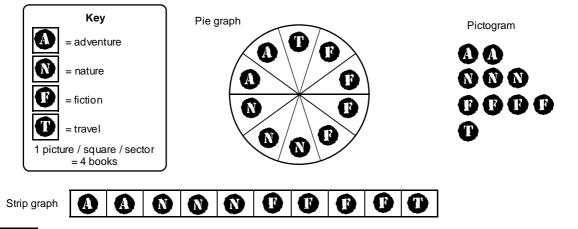
B:

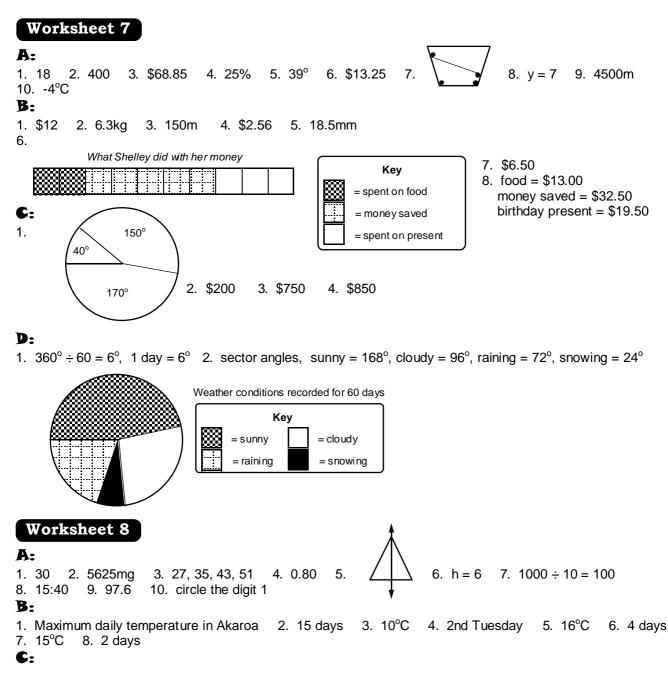
1. fries = 20 items, hamburgers = 24 items, juice = 28 items C:

1. Pie graph: sunny = 20 days, cloudy = 25 days, raining = 5 days

Strip graph: sunny = 15 days, cloudy = 25 days, raining = 10 days 2. 50 days







Set A	Set B	Set C	Set D	Set E
9 + 13 = 22	8 + 17 = 25	7 + 29 = 36	59 + 6 = 65	7 + 16 = 23
23 + 9 = 32	24 + 7 = 31	38 + 5 = 43	8 + 47 = 55	45 + 8 = 53
21 - 8 = 13	33 - 9 = 24	32 – 10 = 22.	30 - 9 = 21	36 - 9 = 27
42 - 9 = 33	57 - 8 = 49	53 – 12 = 41	72 – 21 = 51	53 – 22 = 31
5 × 8 = 40	6 × 9 = 54	7 × 10 = 70	9 × 7 = 63	9 × 7 = 63
6 × 7 = 42	7 × 8 = 56	8 × 9 = 72	6 × 8 = 48	8 × 5 = 40
4 × 9 = 36	9 × 5 = 45	5 × 10 = 50	9 × 9 = 81	6 × 9 = 54
32 ÷ 8 = 4	48 ÷ 6 = 8	56 ÷ 8 = 7	64 ÷ 8 = 8	56 ÷ 7 = 8
49 ÷ 7 = 7	54 ÷ 9 = 6	35 ÷ 7 = 5	63 ÷ 7 = 9	72 ÷ 8 = 9
36 ÷ 4 = 9	28 ÷ 4 = 7	111 ÷ 3 = 37	68 ÷ 4 = 17	48 ÷ 3 = 16
Time taken:	Time taken:	Time taken:	Time taken:	Time taken:

Worksheet 9

A:

8. y = 4 6. \$29.50 7. 1. 21 2. 1.44 3. \$59.40 4. 65% 5. 40° 9. 5.265kg 10. -2°C B: 1. mean 2. median 3. mode 4. range C: 1. 10 2. 9 3. 6 4. 5 5. 13.5 6. 52.5 D: 1. 11 3. 14 4. 20 5. 6, 11, 13, 18, 21, median = 13 6. 3, 5, 7, 9, 11, 12, median = 8 2. 10 E: 1. 4 2. 7, 8 3. no mode 4. 6, 8 5. 5, 7 6. 9 F: 1. 14 - 2 = 12 2. 17 - 1 = 163. 21 - 0 = 21 4. 41 - 9 = 325. \$198500 - \$147990 = \$50510 6. \$205400 - \$67900 = \$137500 G: 1. 5 2. 8 - 3 = 5 3. 4 4. 3, 4, 4, 4, 4, 5, 6, 7, 8 5.4 6. 3, 3, 3, 4, 4, 4, 4, 4, 4, 5, 5, 5, 6, 6, 7, 7, 7, 8 median = 4 Worksheet 10

A:

6. 27.60 7. $500 \div 10 = 50$ 8. 1. 32 2. 09:35 3. h = 6 4. $\frac{3}{4}$ 5. 25° 9. 0.00089 10. 12cm



certain 4

- B:
- 1. Cats are the most popular choice of pets that pupils in Room 5 do have, however only 10 of the 26 pupils in Room 5 have a cat as a pet. Therefore, Sally's statement is incorrect as more pupils have pets that are not cats.
- 2. Consider Richard's scores: highest score = 59, lowest score = 14, therefore the range is 45 mean = 27, median = 25.5, mode = 28

Consider David's scores: highest score = 45, lowest score = 26, therefore the range is 19 mean = 37, median = 38.5, mode = no mode

While Richard did have the highest score, David's scores were better overall, therefore Richard's statement is incorrect.

C:

- 1. The strip graph shows the weather conditions for June. Each square represents 3 days. During June it was sunny for 12 days, cloudy for 12 days and raining on 6 days. Quite a good month as there was little rain.
- 2. In this frisbee throwing competition, 20 people took part. The best throw was 79 metres and the worst throw was 44 metres, therefore there was a range of 35 metres. The mean throw was 60.7 metres, with a median throw of 60.5. A good competition.

Worksheet 11

A:

1. 15 3. \$30 4. 25cm² 5. 111° 6. y = 6 7. 2:35 p.m. 8. 0.40 9. 2.88 10. 34mm 2.13 B:

1.
$$1 = \frac{23}{150}$$
, $2 = \frac{25}{150}$, $3 = \frac{28}{150}$, $4 = \frac{21}{150}$, $5 = \frac{27}{150}$, $6 = \frac{26}{150}$
2.

Î γ

Event	Tally	F	3. 70 times 4. $^{19}/_{70}$ 5. HH 6. $^{34}/_{70}$
НН	++++ ++++	17	7.
HT	HH HH HH I	16	impossible
ТН	++++ ++++ ++++ III	18	' <u>†</u> † †
TT	++++ ++++ ++++	19	HH TT HT & TH

9. red = $\frac{25}{200}$, white = $\frac{40}{200}$, blue = $\frac{15}{200}$, green = $\frac{20}{200}$, yellow = $\frac{100}{200}$ 8. 200 Lego blocks 10. green 11. impossible certain

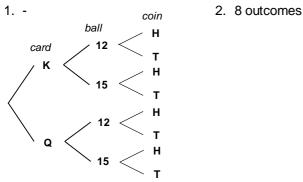
Worksheet 12

A:

```
7. 450 × 2 = 900 8. 06:52
1. 41
        2. 2.47m 3. 37, 49, 61, 73
                                                              6. h = 5
                                      4. 0.45
                                               5.
9. 55.6 10. circle the digit 9
B:
```

Let T = toast, C = cereal, F = fruit. Mo = milo, Mi = milk, J = juice

(T,Mo), (T,Mi), (T,J), (C,J), (C,Mo), (C,Mi), (C,J), (F,Mo), (F,Mi), (F,J) 2. 9 outcomes 1. C:



D:

1. Karen wears a skirt and t-shirt 2. Karen wears shorts and a tank-top 3. 9 combinations E:

1.

	1	2	3	4	5	6
	1,1					
2	2,1	2,2	2,3	2,4	2,5	2,6
3	3,1	3,2	3,3	3,4	3,5	3,6
4	4,1	4,2	4,3	4,4	4,5	4,6
5	5,1	5,2	5,3	5,4	5,5	5,6
6	6,1	6,2	6,3	6,4	6,5	6,6

2. 36 outcomes

Worksheet 13

A:

2. 14 3. \$60 4. 28cm 5. 113° 6. y = 8 7. 6:15 p.m. 8. 0.65 9. 4.32 1. 37 10. 5cm B:

1. $\frac{1}{6}$ 2. $\frac{2}{6}$ or $\frac{1}{3}$ 3. $\frac{3}{6}$ or $\frac{1}{2}$ 4. $\frac{1}{6}$ of 120 = 20 times 5. $\frac{1}{3}$ of 240 = 80 times 6. 120 drinks 7. $\frac{30}{120}$ or $\frac{1}{4}$ 8. $\frac{20}{120}$ or $\frac{1}{6}$ 9. Fanta 10. 25 Fanta drinks 11. 60 fruit juice drinks 12. 9 outcomes 13. $\frac{1}{3}$ 14. $\frac{1}{3}$ 15. $\frac{1}{9}$ 16. $\frac{3}{9}$ or $\frac{1}{3}$

C:

1. Monday = $\frac{4}{30}$ or $\frac{2}{15}$ Wednesday = $\frac{5}{30}$ or $\frac{1}{6}$ 2. $\frac{7}{30}$ 3. $\frac{8}{30}$ or $\frac{4}{15}$

Tracking Sheet: 'In-class' Activity Sheets

	Comments							
Worksheet	Objectives							
13	S3							
12	S 3							
11	S 3							
10	S 3							
9	S3							
\$	S 3	 						
7	S2 / S3							
6	S2 / S3							
5	S2 / S3							
4	S2							
3	S2			 				
2	S1			 	 		 	
1	S1							
Stellettes	Name							

Tracking Sheet: 'In-class' Activity Sheets

			U						
	Comments								
Worksheet	Objectives								
25	S9								
24	S 9								
23	S9								
22	S8								
21	S 8								
20	S 7								
19	S6								
18	S5								
17	S2 / S5								
16	S5								
15	S5								
14	S4								
Stated	Name								

Tracking Sheet: Homework / Assessment Worksheets

			5						
	Comments								
Worksheet	Objectives								
13	S 9								
12	S9								
11	S 8								
10	S6 / S7								
9	S5								
۵	S4								
7	S3								
6	S 3								
5	S 3								
4	S 3								
3	S 3								
2	S2 / S3								
1	S1						- 		
Sacredetec	Name								