

Exercise 3A

Table 1 shows the monthly and annual rainfall for Sydney (Observatory Hill) from 2002 to 2011. Measurements are to the nearest millimetre.

Table 1: Rainfall for Sydney (mm)

| Year | J | F | M | A | M | J | J | A | S | O | N | D | Annual |
|------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|--------|
| 2002 | 98 | 348 | 45 | 68 | 93 | 28 | 24 | 20 | 22 | 6 | 32 | 75 | 860 |
| 2003 | 14 | 59 | 132 | 192 | 349 | 76 | 58 | 43 | 6 | 103 | 109 | 60 | 1200 |
| 2004 | 51 | 129 | 101 | 33 | 8 | 39 | 44 | 153 | 60 | 234 | 67 | 76 | 995 |
| 2005 | 68 | 125 | 154 | 33 | 48 | 79 | 63 | 2 | 51 | 43 | 125 | 25 | 816 |
| 2006 | 121 | 51 | 40 | 10 | 40 | 177 | 140 | 86 | 192 | 17 | 45 | 74 | 994 |
| 2007 | 45 | 108 | 65 | 180 | 10 | 511 | 67 | 152 | 41 | 27 | 170 | 123 | 1499 |
| 2008 | 57 | 258 | 63 | 147 | 3 | 127 | 90 | 44 | 99 | 67 | 73 | 54 | 1083 |
| 2009 | 25 | 128 | 61 | 153 | 126 | 130 | 53 | 6 | 16 | 180 | 13 | 67 | 956 |
| 2010 | 36 | 239 | 51 | 30 | 168 | 147 | 115 | 27 | 42 | 85 | 130 | 83 | 1154 |
| 2011 | 54 | 18 | 192 | 206 | 136 | 94 | 282 | 52 | 72 | 37 | 148 | 78 | 1369 |

- In this time period, which year had the:
 - highest annual rainfall?
 - lowest annual rainfall?
- How much rain fell in:
 - January 2006?
 - May 2007?
 - November 2011?
- Which month had the highest rainfall in:
 - 2004?
 - 2010?
- Which month had the lowest rainfall in:
 - 2003?
 - 2007?
- Which year had the wettest:
 - January?
 - June?
 - December?
- Which year had the driest:
 - February?
 - May?
 - November?
- Considering winter to be the months June, July and August, which year had the:
 - wettest winter?
 - driest winter?



Table 2 summarises the rainfall statistics for Sydney for all records kept from 1859 to 2011.

Table 2: Rainfall statistics for Sydney (mm)

| | J | F | M | A | M | J | J | A | S | O | N | D | Annual |
|---------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|--------|
| Mean | 102 | 118 | 130 | 127 | 121 | 131 | 98 | 80 | 69 | 77 | 84 | 78 | 1215 |
| Lowest | 6 | 3 | 8 | 1 | 3 | 4 | 2 | 0 | 2 | 1 | 2 | 3 | 583 |
| Median | 79 | 94 | 99 | 95 | 91 | 100 | 75 | 55 | 53 | 56 | 67 | 60 | 1160 |
| Highest | 387 | 631 | 521 | 622 | 585 | 643 | 336 | 483 | 356 | 285 | 517 | 402 | 2194 |

- 8** Consider the annual rainfall statistics for Sydney shown in Table 2. What is the annual:
- a** mean? **b** median?
- 9 a** For the month of September, what is the:
- i** mean rainfall? **ii** median rainfall?
- b** Suggest why the 2000 Olympic Games were held in Sydney in the month of September.
- 10** On average, which month of the year is the:
- a** wettest? **b** driest?
- 11 a** What is the least amount of rain that has fallen in any month?
- b** In which month did this occur?
- 12 a** What is the greatest amount of rain that has fallen in any month?
- b** In which month did this occur?
- 13** Which month has the smallest difference between the mean and the median rainfall?

Use tables 1 and 2 to answer questions **14** and **15**.

- 14** For the period 2002–2011, in which years was the annual rainfall in Sydney greater than the long-term mean rainfall?
- 15** For the period 2002–2011, what percentage of years had rainfall that was less than the long-term median rainfall?

Table 3 shows the country of birth of settler arrivals in Australia for the year July 2010 to June 2011.

Table 3: Country of birth of settler arrivals in Australia (July 2010 to June 2011)

| Country of birth | Number of arrivals |
|------------------|--------------------|
| New Zealand | 25 772 |
| China | 14 611 |
| United Kingdom | 10 944 |
| India | 10 566 |
| Philippines | 5 048 |
| South Africa | 4 752 |
| Vietnam | 3 339 |
| Sri Lanka | 3 225 |
| Iraq | 2 988 |

- 16** How many settlers arrived from:
- a** United Kingdom? **b** Vietnam? **c** Iraq?
- 17** The total number of settler arrivals in Australia, from more than 200 countries, was approximately 127 640 from July 2010 to June 2011. Determine the percentage of arrivals who came from:
- a** New Zealand **b** China **c** India
- d** South Africa **e** Sri Lanka.
- 18** How many more arrivals came from:
- a** New Zealand than from Iraq?
- b** the United Kingdom than from Sri Lanka?

Table 4 shows the top 15 countries of birth of Australian residents in 2006 and 2010 (excluding Australian born).

Table 4: Country of birth of Australian residents

| Country of birth | Estimated population 2006 | Estimated population 2010 |
|------------------|---------------------------|---------------------------|
| United Kingdom | 1 153 000 | 1 193 000 |
| New Zealand | 477 000 | 544 000 |
| China | 203 000 | 380 000 |
| India | 154 000 | 341 000 |
| Italy | 220 000 | 216 000 |
| Vietnam | 180 000 | 211 000 |
| Philippines | 136 000 | 177 000 |
| South Africa | 119 000 | 156 000 |
| Malaysia | 104 000 | 136 000 |
| Germany | 115 000 | 129 000 |
| Greece | 126 000 | 127 000 |
| South Korea | 49 000 | 100 000 |
| Sri Lanka | 71 000 | 92 000 |
| Lebanon | 87 000 | 90 000 |
| Hong Kong | 76 000 | 90 000 |



- 19** How many people who were resident Australian in 2010 were born in:
a New Zealand? **b** the Philippines? **c** South Africa? **d** Vietnam? **e** Greece?
- 20** What was the country of birth of the highest proportion of residents in:
a 2010? **b** 2006?
- 21** What was the country of birth of the lowest proportion of residents in:
a 2010? **b** 2006?
- 22** There was a decrease in the resident population from 2006 to 2010 of people born in which country?
- 23** In 2010 approximately 5 994 000 ($\approx 27\%$) of the Australian population were born outside Australia. What percentage of those born outside Australia came from:
a China? **b** India? **c** South Korea? **d** Sri Lanka? **e** Lebanon?
- 24** In 2010 the resident population of Australia was approximately 22 370 000. What percentage of all Australian residents were born in:
a China? **b** India? **c** South Korea? **d** Sri Lanka? **e** Lebanon?
- 25** From 2006 to 2010, what was the percentage increase in the resident population of people born in:
a China? **b** India? **c** South Korea? **d** Sri Lanka? **e** Lebanon?

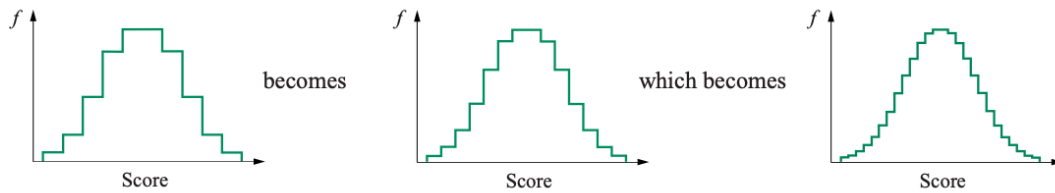
Answers

Exercise 3A

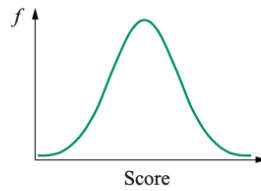
- 1 a 2007 b 2005
- 2 a 121 mm b 10 mm c 148 mm
- 3 a October b February
- 4 a September b May
- 5 a 2006 b 2007 c 2007
- 6 a 2011 b 2008 c 2009
- 7 a 2007 b 2002
- 8 a 1215 mm b 1160 mm
- 9 a i 69 mm ii 53 mm
b September has the lowest average rainfall.
- 10 a June b September
- 11 a 0 mm b August
- 12 a 643 mm b June
- 13 September 14 2007, 2011
- 15 70%
- 16 a 10 944 b 3339 c 2988
- 17 a 20.2% b 11.4% c 8.3%
d 3.7% e 2.5%
- 18 a 22 784 b 7719
- 19 a 544 000 b 177 000 c 156 000
d 211 000 e 127 000
- 20 a UK b UK
- 21 a Hong Kong/Lebanon b South Korea
- 22 Italy
- 23 a 6.3% b 5.7% c 1.7% d 1.5% e 1.5%
- 24 a 1.7% b 1.5% c 0.4% d 0.4% e 0.4%
- 25 a 87.2% b 121.4% c 104.1% d 29.6% e 3.4%

B The shape of displays

As the number of scores in a sample increases, the overall shape of the frequency histogram changes.



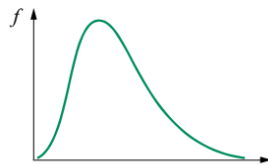
The general shape of a distribution can provide information about the scores. Here is the graph of a symmetric distribution, also referred to as a bell-shaped curve or a normal distribution.



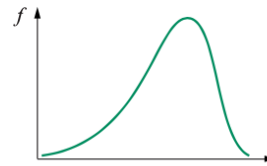
If the distribution is not symmetric then it is said to be **skewed**.

A distribution is **positively skewed** if most of the data is on the left-hand side of the distribution. The data has a 'tail' to the right as shown in the diagram on the left below.

A distribution is **negatively skewed** if most of the data is on the right-hand side of the distribution. The data has a 'tail' to the left as in the diagram on the right below.

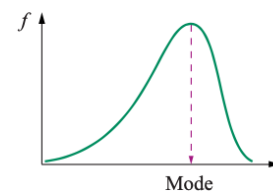
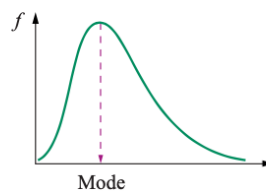
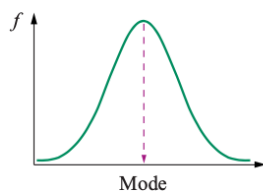


Positively skewed

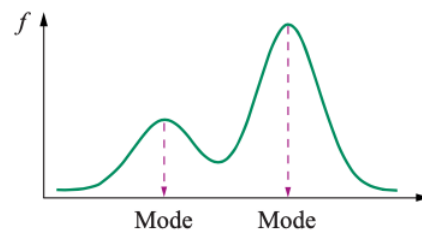
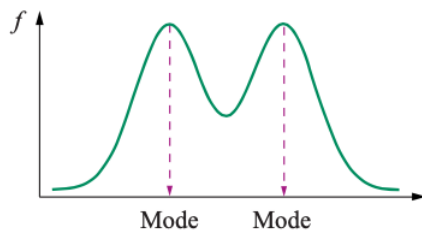


Negatively skewed

The mode is the score with the highest frequency. The mode for the normal and skewed distributions above are shown below.

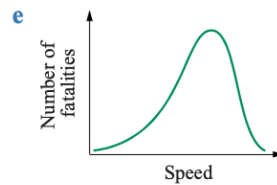
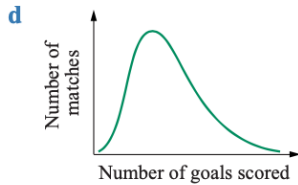
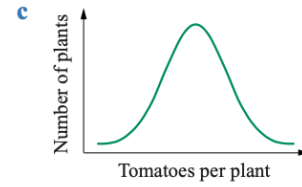
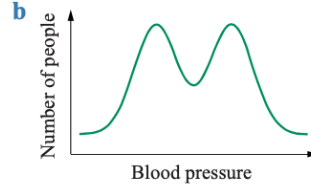
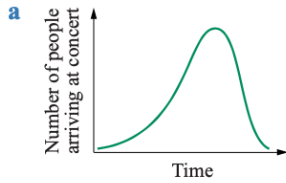


Some distributions have two modes. This is called a **bimodal** distribution. As long as the distribution has two distinct humps, not necessarily with the same frequency (height), then it is said to be bimodal. Two examples are shown below.



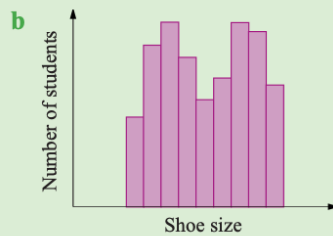
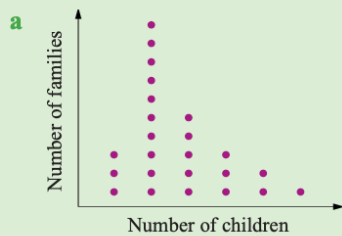
Exercise 3B

- 1 Describe the shape of the following distributions as symmetric, positively skewed, negatively skewed or bimodal.



EXAMPLE 1

Describe the shape of each distribution as symmetric, positively skewed, negatively skewed or bimodal.

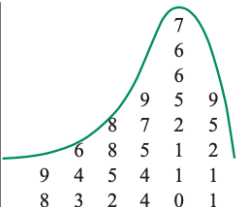


c Marks on test

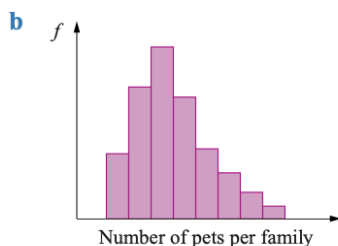
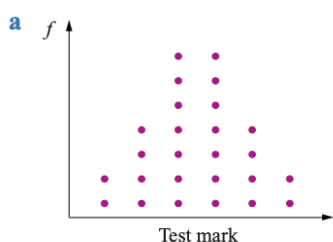
| Stem | Leaf |
|------|-----------------|
| 0 | 8 9 |
| 1 | 3 4 6 |
| 2 | 2 5 8 8 |
| 3 | 4 4 5 7 9 |
| 4 | 0 1 1 2 5 6 6 7 |
| 5 | 1 1 2 5 9 |

| | Solve | Think | Apply |
|----------|--|--|---|
| a | <p>Positively skewed</p> <p>Number of families</p> <p>Number of children</p> | <p>Draw a smooth curve to fit the tops of the columns. The tail is to the right.</p> | <p>Draw a smooth curve through the tops of the columns. Determine from the shape if the distribution is symmetric, positively skewed, negatively skewed or bimodal.</p> |
| b | <p>Bimodal</p> <p>Number of students</p> <p>Shoe size</p> | <p>Draw a smooth curve to fit the tops of the columns. The curve has two humps.</p> | |

EXAMPLE 1 CONTINUED

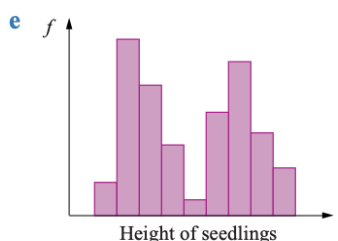
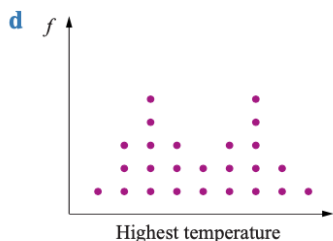
| | Solve | Think | Apply | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|---|--|-------|-------|---|---|---|---|---|---|---|---|--|--|---|---|---|---|---|--|---|---|---|---|---|---|---|---|---|---|---|---|--|--|
| c | <p>Negatively skewed</p> <div><div>Leaf</div><div><table><tr><td>7</td><td>6</td><td>6</td><td>9</td><td>5</td><td>9</td></tr><tr><td>8</td><td>7</td><td>2</td><td>5</td><td></td><td></td></tr><tr><td>6</td><td>8</td><td>5</td><td>1</td><td>2</td><td></td></tr><tr><td>9</td><td>4</td><td>5</td><td>4</td><td>1</td><td>1</td></tr><tr><td>8</td><td>3</td><td>2</td><td>4</td><td>0</td><td>1</td></tr></table></div><div><div>Stem</div><div>0 1 2 3 4 5</div></div></div> | 7 | 6 | 6 | 9 | 5 | 9 | 8 | 7 | 2 | 5 | | | 6 | 8 | 5 | 1 | 2 | | 9 | 4 | 5 | 4 | 1 | 1 | 8 | 3 | 2 | 4 | 0 | 1 | <p>Turn the stem-and-leaf plot on its side and draw a smooth curve to fit the tops of the columns.</p> <p>The tail is to the left.</p> | <p>Turn the stem-and-leaf plot on its side so that the stems are in increasing order, from left to right. Draw a smooth curve through the tops of the columns. Determine from the shape of the distribution if it is symmetric, positively skewed, negatively skewed or bimodal.</p> |
| 7 | 6 | 6 | 9 | 5 | 9 | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 8 | 7 | 2 | 5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6 | 8 | 5 | 1 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 9 | 4 | 5 | 4 | 1 | 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 8 | 3 | 2 | 4 | 0 | 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

2 Describe the shape of each distribution as symmetric, positively skewed, negatively skewed or bimodal.



c Marks on test

| Stem | Leaf |
|------|-------------|
| 1 | 5 |
| 2 | 3 4 |
| 3 | 5 5 7 |
| 4 | 2 3 3 9 |
| 5 | 1 4 4 6 8 9 |
| 6 | 0 1 3 |



- 3 a** Construct a frequency histogram and polygon for the data in the frequency distribution table below.
- b** Describe the shape of the distribution as positively skewed, negatively skewed or bimodal.

| Score | Frequency |
|-------|-----------|
| 6 | 2 |
| 7 | 2 |
| 8 | 3 |
| 9 | 5 |
| 10 | 8 |
| 11 | 6 |



EXAMPLE 2

Describe the shape of both data sets in the back-to-back stem-and-leaf plot as symmetric, positively skewed, negatively skewed or bimodal.

| Scores on topic test | | |
|----------------------|------|---------|
| Females | Stem | Males |
| 9 | 1 | 0 5 |
| 3 | 2 | 3 4 4 7 |
| 5 4 | 3 | 1 8 9 |
| 7 3 3 2 | 4 | 2 7 8 9 |
| 9 8 8 7 6 | 4 | 3 4 |
| 4 2 | 6 | |

| Solve | | Think | Apply |
|------------------------------------|--|--|--|
| Male scores Bimodal | <div> <div>Leaf</div> <div>Stem</div> </div> | <p>For males, turn the plot on its side and draw a curve to fit the columns.</p> <p>For females, flip the data over the stem and turn it on its side. Draw a curve to fit the columns.</p> | <p>Turn each stem-and-leaf plot on its side so that the stems are in increasing order, from left to right. Draw a smooth curve through the tops of the columns and describe the shape of the distribution.</p> |
| Female scores Negatively skewed | <div> <div>Leaf</div> <div>Stem</div> </div> | | |

- 4 Describe the shape of each data set in the following distributions as symmetric, positively skewed, negatively skewed or bimodal.

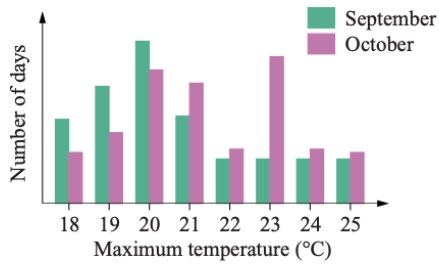
a Scores on Science test

| Females | Stem | Males |
|-------------|------|---------------|
| 9 | 0 | 7 7 8 |
| 4 3 | 1 | 2 3 5 7 9 9 9 |
| 7 1 | 2 | 0 1 1 |
| 9 6 4 0 | 3 | 5 7 |
| 9 7 5 5 2 2 | 4 | 6 |
| 3 1 1 | 5 | 1 |

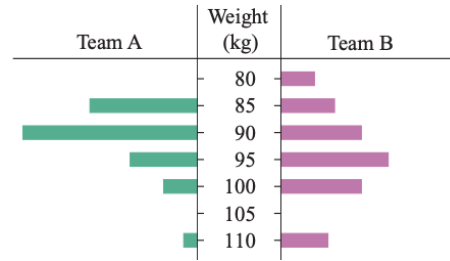
b Scores on Mathematics test

| 9 Blue | Stem | 9 Red |
|-----------|------|-------------|
| 9 9 8 | 4 | 7 |
| 8 7 2 1 1 | 5 | 3 4 7 8 |
| 4 3 2 | 6 | 1 5 |
| 5 4 | 7 | 0 5 5 6 8 9 |
| 3 0 | 8 | 3 4 |
| 1 | 9 | 2 |

- 5 a** This distribution shows the average maximum temperatures (in °C) in Sydney for September and October. This is called a side-by-side histogram. Describe the data distribution.



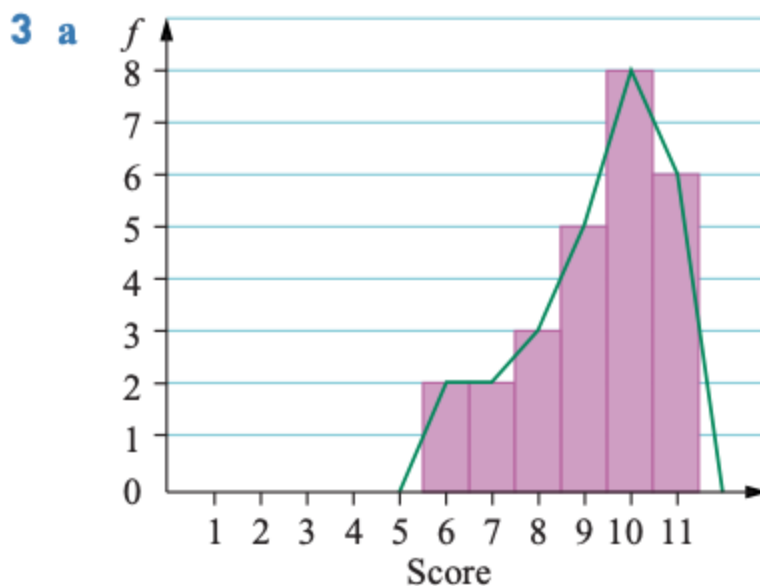
- b** This distribution shows the weight (in kg) of players in two Rugby League teams. This is called a **back-to-back** histogram. Describe the data distribution for each team.



Answers

Exercise 3B

- 1 **a** Negatively skewed **b** Bimodal
c Symmetric **d** Positively skewed
e Negatively skewed
- 2 **a** Symmetric **b** Positively skewed
c Negatively skewed **d** Bimodal
e Bimodal



b It is negatively skewed.

- 4 **a** Female: negatively skewed, males: positively skewed
b 9 Blue: positively skewed, 9 Red: bimodal
- 5 **a** September: positively skewed, October: bimodal
b Team A: positively skewed, team B: approximately symmetrical