## MATHLETIGS

## Area, Volume and Capacity

## Student Book - Series $\mathrm{H}_{-1}$



## Area, volume and capacity

## Student Book - Series H

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Author of The Topics and Topic Tests: AS Kalra

## Area, volume and capacity

## Topic 1: Area of a square

Question 1 Find the area of the following squares.
a

b

c

d

e

f


Question 2 Find the area of the square whose side is given below. (Show all your working.)
a 3 m
$\qquad$
b $\quad 10 \mathrm{~m}$
$\qquad$
$\qquad$
c $\quad 11 \mathrm{~cm}$
d $\quad 1.5 \mathrm{~m}$
e $\quad 12 \mathrm{~mm}$
f $\quad 3.2 \mathrm{~m}$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Question 3 Find the length of the side of the square whose area is given below. (Show all working.)
a $\quad 16 \mathrm{~cm}^{2}$
$\qquad$
$\qquad$
d $225 \mathrm{~cm}^{2}$
b $\quad 169 \mathrm{~m}^{2}$
$\qquad$
$\qquad$
e $\quad 256 \mathrm{~cm}^{2}$
f $\quad 676 \mathrm{~mm}^{2}$

## Area, volume and capacity

## Topic 2: Area of a rectangle

Question 1 Find the area of the following rectangles.
a

b


d

e

f


Question 2 Find the area of each of the following rectangles whose length and breadth are given.

|  | Length | Breadth | Area |
| :---: | :---: | :---: | :---: |
| a | 9 cm | 7 cm |  |
| b | 12 cm | 3 cm |  |
| c | 14 m | 5 m |  |
| d | 11 mm | 6 mm |  |
| e | 8 m | 3 m |  |


|  | Length | Breadth | Area |
| :---: | :---: | :---: | :---: |
| f | 10 m | 6 m |  |
| g | 15 cm | 8 cm |  |
| h | 25 mm | 6 mm |  |
| i | 20 cm | 7 cm |  |
| j | 16 cm | 10 cm |  |

Question 3 Complete the following.

|  | Length | Breadth | Area |
| :---: | :---: | :---: | :---: |
| a | 6 m | 5 m |  |
| b | 8 cm |  | $32 \mathrm{~cm}^{2}$ |
| c | 18 cm | 4 cm |  |
| d | 12 cm |  | $84 \mathrm{~cm}^{2}$ |
| e | 21 m |  | $105 \mathrm{~m}^{2}$ |


|  | Length | Breadth | Area |
| :---: | :---: | :---: | :---: |
| f | 13 m |  | $65 \mathrm{~m}^{2}$ |
| g | 14 cm | 8 cm |  |
| h |  | 9 cm | $99 \mathrm{~cm}^{2}$ |
| i | 28 mm |  | $140 \mathrm{~mm}^{2}$ |
| j |  | 20 cm | $700 \mathrm{~cm}^{2}$ |

## Area, volume and capacity

## Topic 3: Area of a triangle

Question 1 Find the area of the following triangles.
a

b

c

d

e

f


## Question 2

a A triangle has a base of 30 cm and a height of 15 cm . What is its area?
b A triangle has an area of $112 \mathrm{~cm}^{2}$ and a base length of 28 cm . Find its height.

Question 3 Find the area of the triangles whose base and height are given.

|  | Base | Height | Area |
| :---: | :---: | :---: | :---: |
| a | 6 m | 4 m |  |
| b | 11 cm | 6 cm |  |
| c | 10 cm | 8 cm |  |


|  | Base | Height | Area |
| :---: | :---: | :---: | :---: |
| d | 18 cm | 6 cm |  |
| e | 9 cm | 8 cm |  |
| f | 7 m | 6 m |  |

Question 4 Complete the following. (All lengths are in cm ; areas are in $\mathrm{cm}^{2}$.)

|  | Base | Height | Area of triangle |
| :---: | :---: | :---: | :---: |
| a | 16 | 4 |  |
| b | 9 |  | 36 |
| c | 14 | 6 |  |


|  | Base | Height | Area of triangle |
| :---: | :---: | :---: | :---: |
| d |  | 11 | 44 |
| e | 20 | 10 |  |
| f |  | 13 | 65 |

## Area, volume and capacity

## Topic 4: Composite areas

QUestion 1 Find the areas of the following composite figures by dividing them into rectangles, squares and triangles. All measurements are in centimetres.
a

b


24
d

e

f

g

h

i


Question 2 Find the shaded area of each shape. All measurements are in centimetres.
a

b

c



## Area, volume and capacity

## Topic 5: Volume of a cube

Question 1 Find the volume of the following cubes.


## Question 2

a The volume of a cube is $125 \mathrm{~cm}^{3}$. What is the length of each edge? $\qquad$
b The volume of a cube is $343 \mathrm{~cm}^{3}$. Find its side length. $\qquad$
Question 3 Calculate the volume of each of the following cubes whose side length is given. Show all your working.
a $\quad 1 \mathrm{~cm}$
$\qquad$
$\qquad$
b $\quad 11 \mathrm{~cm}$
c $\quad 10 \mathrm{~cm}$
$\qquad$
d $\quad 2.4 \mathrm{~m}$
e $\quad 3 \mathrm{~m}$
f $\quad 1.6 \mathrm{~m}$
$\qquad$
$\qquad$
g 8 cm
h $\quad 1.9 \mathrm{~m}$
i $\quad 2.5 \mathrm{~m}$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Area, volume and capacity

## Topic 6: Volume of a rectangular prism

Question 1 Find the volume of the following rectangular prisms. All measurements are in centimetres.
a

9
b

c

d

10
e

f


Question 2 Find the volume of each of the following rectangular prisms whose dimensions are given below.

|  | Length | Breadth | Height | Volume |  | Length | Breadth | Height | Volume |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a | 10 cm | 5 cm | 7 cm |  | d | 9 cm | 2 cm | 3 cm |  |
| b | 8 m | 4 m | 6 m |  | e | 11 cm | 4 cm | 5 cm |  |
| c | 9 mm | 5 mm | 2 mm |  | f | 8 m | 3 m | 2 m |  |

Question 3 Complete the following.

|  | Length | Breadth | Height | Volume |
| :---: | :---: | :---: | :---: | :---: |
| a | 6 m | 4 m | 3 m |  |
| b | 7 cm | 5 cm | 3 cm |  |
| c | 6 mm | 7 mm |  | $84 \mathrm{~mm}^{3}$ |


|  | Length | Breadth | Height | Volume |
| :---: | :---: | :---: | :---: | :--- |
| d |  | 6 cm | 4 cm | $216 \mathrm{~cm}^{3}$ |
| e | 9 m |  | 7 m | $252 \mathrm{~m}^{3}$ |
| f | 5 cm | 4 cm | 3 cm |  |

## Area, volume and capacity

## Topic 7: Volume of a triangular prism

Question 1 Find the volume of the following triangular prisms. All lengths are in centimetres, areas in square centimetres.
a

d

b

e

c

f


Question 2 Find the volume of each of the following triangular prisms whose dimensions are given below.

|  | Base area | Height | Volume |
| :---: | :---: | :---: | :--- |
| a | $30 \mathrm{~cm}^{2}$ | 8 cm |  |
| b | $20 \mathrm{~m}^{2}$ | 9 m |  |
| c | $82 \mathrm{~cm}^{2}$ | 15 cm |  |


|  | Base area | Height | Volume |
| :---: | :---: | :---: | :---: |
| d | $84 \mathrm{~cm}^{2}$ | 20 cm |  |
| e | $15 \mathrm{~m}^{2}$ | 4 m |  |
| f | $40 \mathrm{~m}^{2}$ | 12 m |  |

Question 3 Complete the following.

|  | Base area | Height | Volume |
| :---: | :---: | :---: | :---: |
| a | $24 \mathrm{~m}^{2}$ | 5 m |  |
| b |  | 9 cm | $477 \mathrm{~cm}^{3}$ |
| c | $36 \mathrm{~m}^{2}$ | 10 m |  |
| d | $41 \mathrm{~m}^{2}$ |  | $492 \mathrm{~m}^{3}$ |


|  | Base area | Height | Volume |
| :---: | :---: | :---: | :---: |
| e |  | 8 cm | $536 \mathrm{~cm}^{3}$ |
| f | $18 \mathrm{~cm}^{2}$ |  | $162 \mathrm{~cm}^{3}$ |
| g | $72 \mathrm{~m}^{2}$ | 5 m |  |
| h | $58 \mathrm{~m}^{2}$ | 6 m |  |

## Area, volume and capacity

## Topic 8: Volume of prisms - miscellaneous

Question 1 Find the volume of the following prisms. Length are in cm , areas in $\mathrm{cm}^{2}$.
a

b

12
d

e

C

f


Question 2 For the given solid:
a find the number of faces $\qquad$
b find the number of vertices $\qquad$

d draw a line to divide it into a rectangular prism and a triangular prism
e find the volume of the rectangular prism $\qquad$
f find the volume of the triangular prism $\qquad$
$g$ find the total volume of the solid $\qquad$

Question 3 For the given solid:
a find the area of the front big rectangle $\qquad$
b find the area of the front small rectangle $\qquad$
c find the cross-sectional area $\qquad$

d find the volume of the solid $\qquad$

## Area, volume and capacity

## Topic 9: Capacity and volume

Question 1 Convert the following to the unit given.
a $\quad 1000 \mathrm{~mL}=$ $\qquad$ L
b $\quad 75000 \mathrm{~mL}=$ $\qquad$ L c $3500 \mathrm{~mL}=$ $\qquad$ L
d $6 \mathrm{~L}=$ $\qquad$ mL
e $3.25 \mathrm{~L}=$ $\qquad$ mL
f $6.5 \mathrm{~L}=$ $\qquad$ mL g $\quad 1 \mathrm{~kL}=$ $\qquad$ L
h $\quad 4 \mathrm{~kL}=$ $\qquad$ L
i $6.5 \mathrm{~kL}=$ $\qquad$ L

Question 2 Convert each of the following to the unit given.
a $\quad 1000 \mathrm{~mm}^{3}=$ $\qquad$ $\mathrm{cm}^{3}$
b $\quad 1000000 \mathrm{~cm}^{3}=$ $\qquad$ $\mathrm{m}^{3} \quad$ c $\quad 1 \mathrm{~mL}=$ $\qquad$ $\mathrm{cm}^{3}$
d $\quad 1000 \mathrm{~cm}^{3}=$ $\qquad$ L
e $\quad 1000 \mathrm{~L}=$ $\qquad$ kL
f $1 \mathrm{~kL}=$ $\qquad$ $m^{3}$

## Question 3

a A jug has a volume of $12000 \mathrm{~cm}^{3}$. How many litres of water can it hold?
b A swimming pool holds 25000 L of water. How many kilolitres is this?
c A bottle contains $\frac{3}{5}$ of a litre of drink. How many millilitres is this?
d A fish tank measures $80 \mathrm{~cm} \times 60 \mathrm{~cm} \times 15 \mathrm{~cm}$.
i Find its volume in cubic centimetres.
ii How many litres of water will it hold?

Question 4 Find the volume of the following prisms and then find how many mL of liquid each would hold. Show working.
a

b

c


## Area, volume and capacity

## Topic 10: Problem solving with area, volume and capacity

1 A rectangular tank with dimensions $80 \mathrm{~cm} \times 20 \mathrm{~cm} \times 25 \mathrm{~cm}$ is filled with water. Hold many litres of water will it hold?

2 A dripping tap loses 5 mL of water every 30 seconds. How much water will be lost in 1 hour?
$\qquad$
3 The volume of a cube is $729 \mathrm{~cm}^{3}$. Find its side length.

4 Dilnoor drank $\frac{4}{5}$ of a litre of milk. How many millilitres is this?
$\qquad$
5 Three hundred children went on a picnic. Each child drank a can of drink containing 500 mL . How many litres were consumed altogether?

6 A rectangular prism has dimensions 3 cm by 5 cm by 6 cm .
i What is its volume?
$\qquad$
ii If each of these dimensions are doubled, what would be its volume?
$\qquad$
7 A photograph is 40 cm long and 20 cm wide. Find its area.
$\qquad$
8 The perimeter of a square is 40 cm . Find the area of the square.

9 A triangle has an area of $80 \mathrm{~cm}^{2}$. If the base of the triangle is 20 cm , find its height.
$\qquad$
10 Find the total area of the four walls of a room 10 m long, 8 m wide and 3 m high.

11 One of the faces of a cube has an area of $36 \mathrm{~cm}^{2}$. What is the volume of the cube?
$\qquad$
12 Kabir drank 1.25 litres of milk. How many millilitres is this?
$\qquad$

## Area, volume and capacity

## Instructions This part consists of 12 multiple-choice questions

Each question is worth 1 mark
Fill in only ONE CIRCLE for each question
Calculators are NOT allowed
Time allowed: 15 minutes
Total marks $=12$
Marks
1 What is the cost of tiling a floor 9 m by 3 m at $\$ 20$ per square metre?
(A) $\$ 450$
(B) $\$ 504$
(C) $\$ 540$
(D) $\$ 527$

2 How many tiles each measuring $10 \mathrm{~cm} \times 10 \mathrm{~cm}$ are needed to cover a floor $6 \mathrm{~m} \times 6 \mathrm{~m}$ ?
(A) 3600
(B) 60000
(C) 30000
(D) 36

3 A petrol tank when half full holds 40 litres. How much more petrol does it hold if it is three-quarters full?
(A) 15 mL
(B) 25 mL
(C) 18 L
(D) 20 L

4 The area of a square of size 11 cm is
(A) $11 \mathrm{~cm}^{2}$
(B) $121 \mathrm{~cm}^{2}$
(C) $110 \mathrm{~cm}^{2}$
(D) $44 \mathrm{~cm}^{2}$

5 A rectangle is 18 m long and 7 m wide. Its area equals
(A) $50 \mathrm{~m}^{2}$
(B) $49 \mathrm{~m}^{2}$
(C) $126 \mathrm{~m}^{2}$
(D) $324 \mathrm{~m}^{2}$

6 If the volume of cube is $64 \mathrm{~cm}^{3}$, then its side length is
(A) 8 cm
(B) 4 cm
(C) 2 cm
(D) 16 cm

7 How many mm ${ }^{2}$ in $3 \mathrm{~cm}^{2}$ ?
(A) $3 \mathrm{~mm}^{2}$
(B) $30 \mathrm{~mm}^{2}$
(C) $300 \mathrm{~mm}^{2}$
(D) $3000 \mathrm{~mm}^{2}$

8 How many mL in 3.5 L ?
(A) 35 mL
(B) 350 mL
(C) 3500 mL
(D) 35000 mL

9 How many kL in $4 \mathrm{~m}^{3}$ ?
(A) 4 kL
(B) 40 kL
(C) 400 kL
(D) 4000 kL

10 How many $\mathrm{cm}^{3}$ in $2 \mathrm{~m}^{3}$ ?
(A) $2000 \mathrm{~cm}^{3}$
(B) $20000 \mathrm{~cm}^{3}$
(C) $200000 \mathrm{~cm}^{3}$
(D) $2000000 \mathrm{~cm}^{3}$

11 The volume of a rectangular prism $4 \mathrm{~cm} \times 5 \mathrm{~cm} \times 6 \mathrm{~cm}$ equals
(A) $15 \mathrm{~cm}^{3}$
(B) $30 \mathrm{~cm}^{3}$
(C) $60 \mathrm{~cm}^{3}$
(D) $120 \mathrm{~cm}^{3}$

12 The capacity of a glass would be closest to
(A) 30 mL
(B) 300 mL
(C) 3000 mL
(D) 3500 mL

## Area, volume and capacity

Instructions This part consists of 15 questions
Each question is worth 1 mark
Write answers in the answers-only column
Time allowed: $\mathbf{2 0}$ minutes
Total marks $\mathbf{= 1 5}$

## Questions

1 Find the volume of a cube of edge 8 cm .
2 Find the volume of a rectangular prism $6 \mathrm{~cm} \times 9 \mathrm{~cm} \times 3 \mathrm{~cm}$.
3 Find the volume of a triangular prism with base area $30 \mathrm{~cm}^{2}$ and height 10 cm .

4 How many litres in 5000 mL ?
5 The volume of a cube is $1331 \mathrm{~cm}^{3}$. Find its edge length.
6 A rectangular prism has dimensions 2 cm by 3 cm by 4 cm . Find its volume.

7 If each of the dimensions given in question 6 is doubled, what would be the prism's volume?

8 Find the area of a rectangle $10 \mathrm{~m} \times 6 \mathrm{~m}$.
9 Find the side length of a square whose area is $169 \mathrm{~cm}^{2}$.
10 If the area of a triangle is $30 \mathrm{~cm}^{2}$ and its base is 6 cm , find the height of the triangle.

11 There are 28 students in a class. Each student drinks 250 mL of milk. How many litres is this?

12 Find the area of a triangle with a base of 29 mm and a height of 40 mm .

13 Find the number of cubic millimetres $\left(\mathrm{mm}^{3}\right)$ in one cubic centimetre.

14 How many millilitres are in 1 kilolitre?
15 A jug has a volume of $8000 \mathrm{~cm}^{3}$. How many litres of water can it hold?

| Answers only | Marks |
| :--- | :---: |
|  | $\boxed{1}$ |

$\qquad$

