

MATHLETICS

Trigonometry and the Right-angled Triangle

Student Book - Series J-2

$\sin \theta$ $\cos \theta$
 $\tan \theta$



Mathletics
Instant
Workbooks



Trigonometry and the right-angled triangle

Student Book - Series J 2

Contents

Topics	Date completed
Topic 1 - Naming the sides of a right-angled triangle	__/__/__
Topic 2 - The trigonometric ratios	__/__/__
Topic 3 - Use of a calculator in trigonometry	__/__/__
Topic 4 - Finding an unknown side	__/__/__
Topic 5 - Finding the hypotenuse	__/__/__
Topic 6 - Finding the unknown angle	__/__/__
Topic 7 - Exact trigonometric ratios	__/__/__
Topic 8 - Angle of elevation, angle of depression and bearings	__/__/__
Topic 9 - Problem solving involving two right-angled triangles	__/__/__

Practice Tests

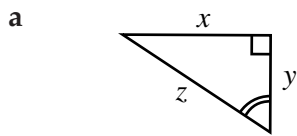
Topic 1 - Topic test A	__/__/__
Topic 2 - Topic test B	__/__/__

Author of The Topics and Topic Tests: AS Kalra

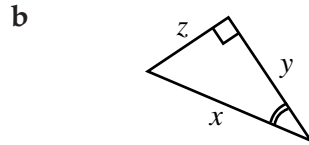
Trigonometry and the right-angled triangle

Topic 1 - Naming the sides of a right-angled triangle

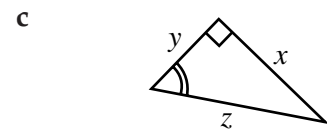
QUESTION 1 In each of the following triangles, state whether x , y and z are the opposite side, adjacent side or hypotenuse with reference to the angle marked.



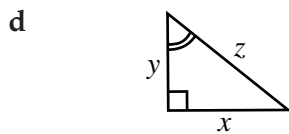
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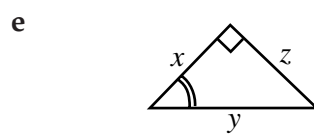
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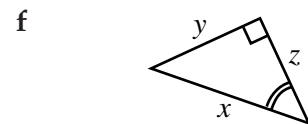
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$x = \text{---}, y = \text{---}, z = \text{---}$

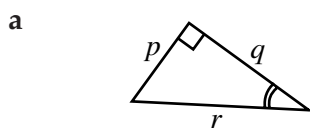


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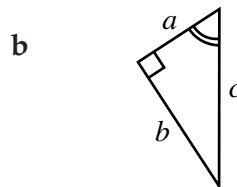


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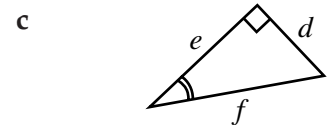
QUESTION 2 Name the sides in the following right-angled triangles with reference to the angle marked.



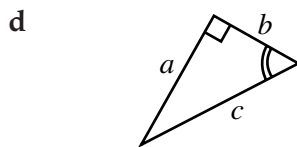
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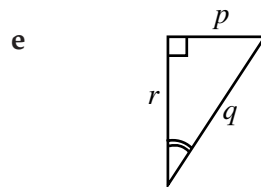
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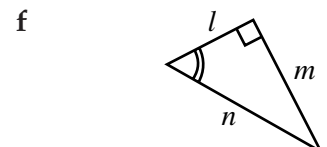
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$a = \text{---}, b = \text{---}, c = \text{---}$

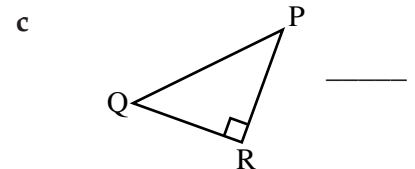
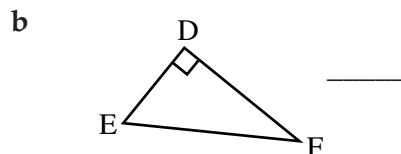
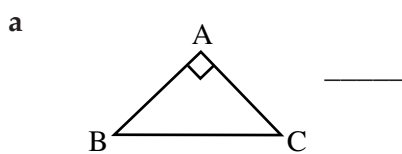


$p = \text{---}, q = \text{---}, r = \text{---}$



$l = \text{---}, m = \text{---}, n = \text{---}$

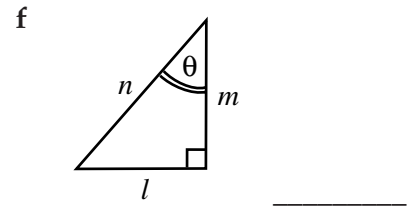
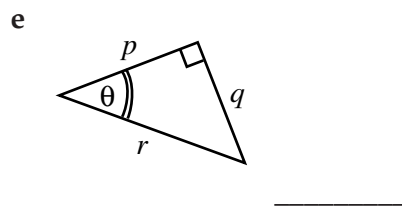
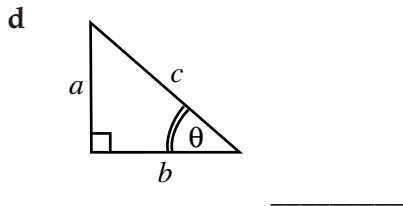
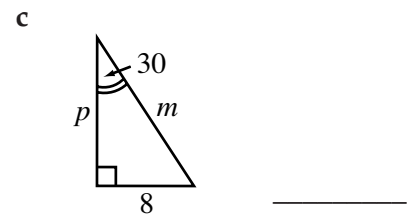
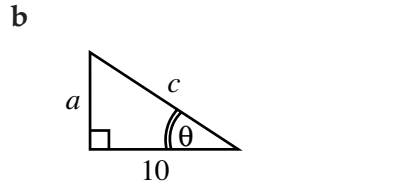
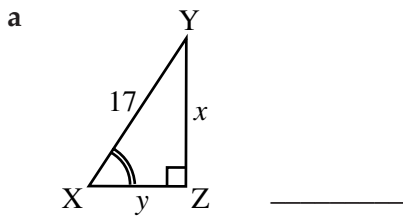
QUESTION 3 Name the hypotenuse in each triangle given below.



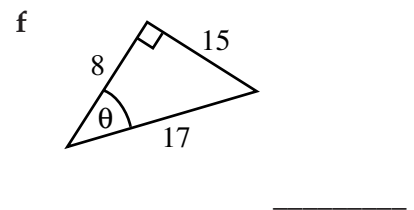
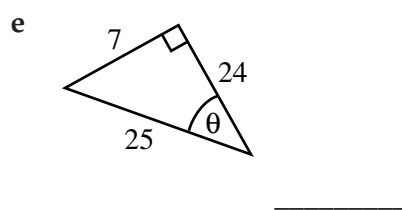
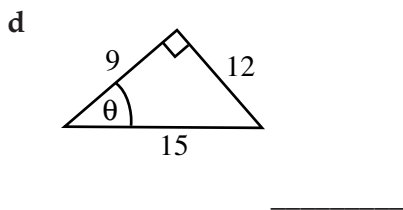
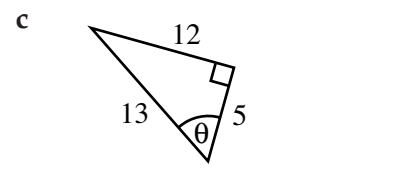
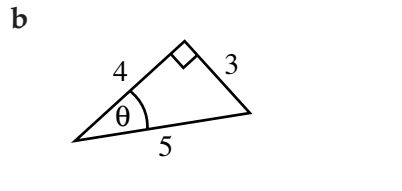
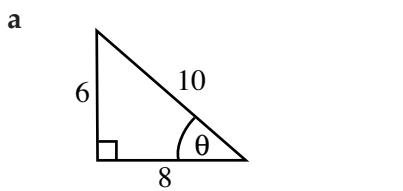
Trigonometry and the right-angled triangle

Topic 2 - The trigonometric ratios

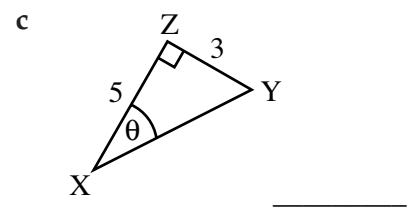
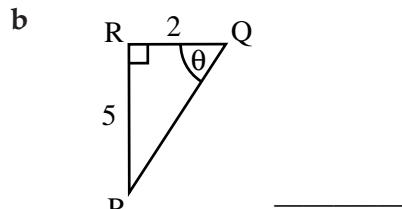
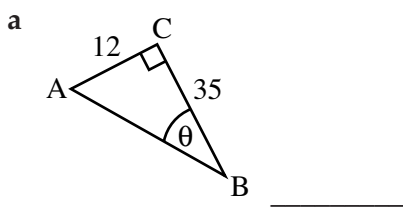
QUESTION 1 Write the trigonometric ratios for the following triangles.



QUESTION 2 Find $\sin \theta$, $\cos \theta$ and $\tan \theta$ in the following triangles.



QUESTION 3 Use Pythagoras' theorem to find the unknown side and then find $\sin \theta$, $\cos \theta$ and $\tan \theta$.



Trigonometry and the right-angled triangle

Topic 3 - Use of a calculator in trigonometry

QUESTION 1 Find the value of the following correct to three decimal places.

a $\sin 69 =$ _____ b $\cos 60 =$ _____ c $\tan 21 =$ _____
d $\cos 82 =$ _____ e $\tan 28 =$ _____ f $\sin 58 =$ _____
g $\tan 31 =$ _____ h $\sin 35 =$ _____ i $\cos 43 =$ _____

QUESTION 2 Find the value of the following correct to three significant figures.

a $2.8 \sin 42 =$ _____ b $\tan 58\ 4' =$ _____ c $\sin 27\ 15' =$ _____
d $8 \cos 19 =$ _____ e $\sin 53\ 27' =$ _____ f $\cos 28\ 35' =$ _____
g $\sin 59\ 28' =$ _____ h $30.6 \cos 65\ 12' =$ _____ i $\tan 31\ 49' =$ _____

QUESTION 3 Find the value of the following correct to two decimal places.

a $\frac{\tan 58}{6} =$ _____ b $\frac{\cos 63}{5} =$ _____ c $\frac{14.3}{\sin 54} =$ _____
d $\frac{\sin 39\ 41'}{4.7} =$ _____ e $\frac{\sin 54\ 28'}{2.5} =$ _____ f $\frac{18.6}{\cos 37\ 15'} =$ _____
g $\frac{\tan 25\ 54'}{8.25} =$ _____ h $\frac{\tan 38\ 29'}{8.6} =$ _____ i $\frac{359}{\tan 75\ 36'} =$ _____

QUESTION 4 A is an acute angle. Find its size to the nearest degree.

a $\sin A = 0.5736$ _____ b $\tan A = 0.7836$ _____ c $\cos A = 0.8126$ _____
d $\cos A = 0.5990$ _____ e $\sin A = 0.7587$ _____ f $\tan A = 1.491$ _____
g $\tan A = 2.5583$ _____ h $\cos A = 0.2935$ _____ i $\sin A = 0.9941$ _____

QUESTION 5 A is an acute angle. Find its size in degrees and minutes.

a $\sin A = 0.5$ _____ b $\cos A = 0.3568$ _____ c $\tan A = 1.326$ _____
d $\cos A = 0.4836$ _____ e $\tan A = 0.7983$ _____ f $\sin A = 0.4839$ _____

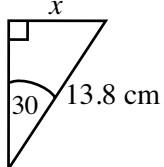
QUESTION 6 Find the size of the acute angle in degrees and minutes.

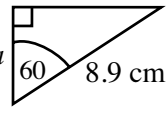
a $\cos A = \frac{1}{2}$ _____ b $\sin A = \frac{13}{18}$ _____ c $\tan A = \frac{15.7}{12.85}$ _____
d $\tan A = \frac{15}{22}$ _____ e $\cos A = \frac{8.5}{11.9}$ _____ f $\sin A = \frac{1.732}{2}$ _____

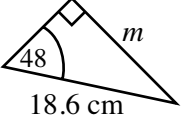
Trigonometry and the right-angled triangle

Topic 4 - Finding an unknown side

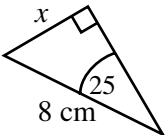
QUESTION 1 Find the value of the unknown side correct to one decimal place.

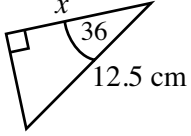
a  _____

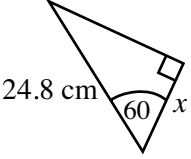
b  _____

c  _____

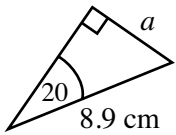
QUESTION 2 Find the value of x in the following triangles, correct to three decimal places.

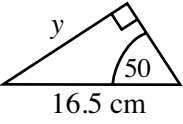
a  _____

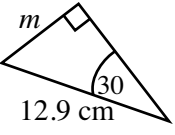
b  _____

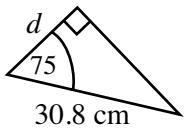
c  _____

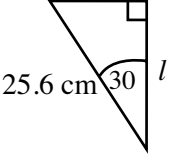
QUESTION 3 Find the value of the pronumeral correct to two decimal places.

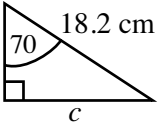
a  _____

b  _____

c  _____

d  _____

e  _____

f  _____

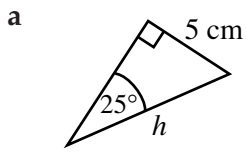
QUESTION 4 Michelle is flying a kite on a 55 metre string that makes an angle of 56° with the horizontal. Calculate the height of the kite to the nearest metre.

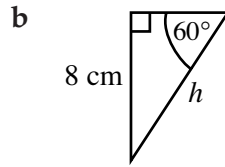
QUESTION 5 In $\triangle ABC$, $\angle C = 90^\circ$, $\angle B = 34.5^\circ$ and $BC = 3.6$ cm. Find AB .

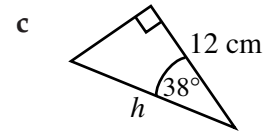
Trigonometry and the right-angled triangle

Topic 5 - Finding the hypotenuse

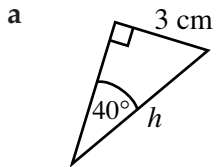
QUESTION 1 Find the length of the hypotenuse correct to one decimal place.

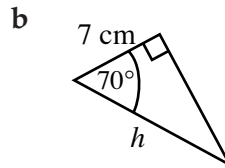


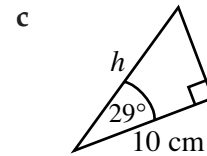




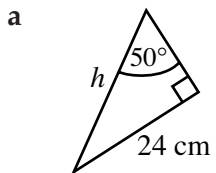
QUESTION 2 Find the length of the hypotenuse correct to one decimal place.

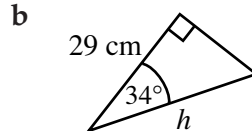


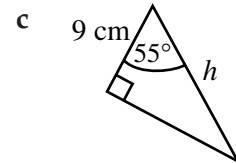


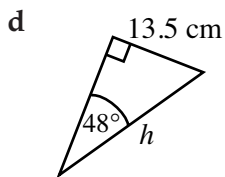


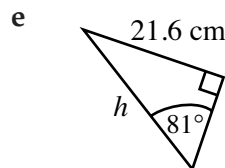
QUESTION 3 Find the length of the hypotenuse correct to one decimal place.

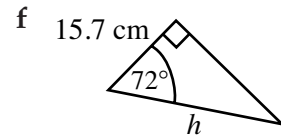




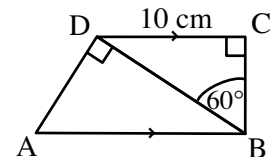








QUESTION 4 The diagram shown opposite is a trapezium with DC parallel to AB. Calculate the length of BD and AB.

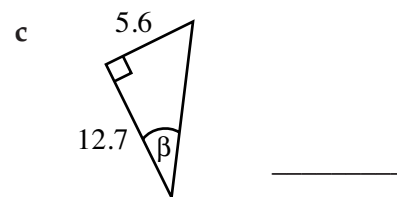
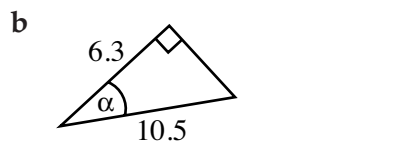
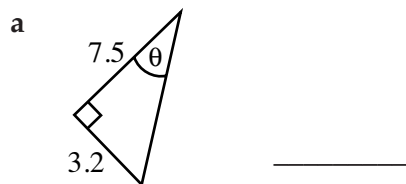


QUESTION 5 Find the length of the diagonal of a rectangle if the length of the rectangle is 10.7 cm and the diagonal makes an angle of 30° with the longer side.

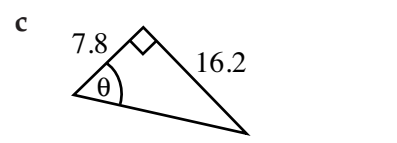
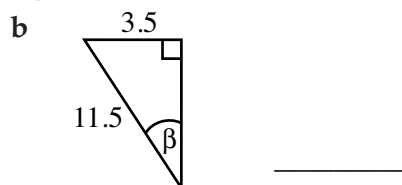
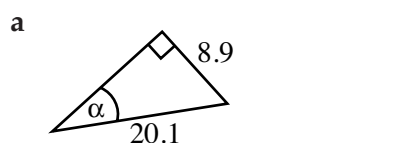
Trigonometry and the right-angled triangle

Topic 6 - Finding the unknown angle

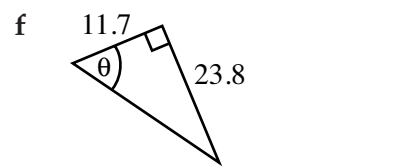
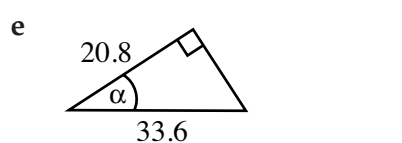
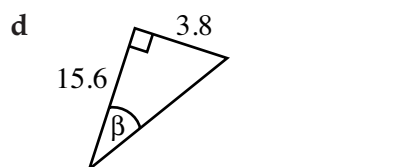
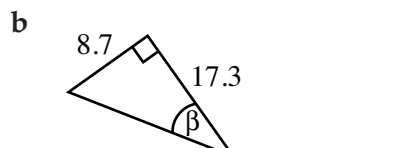
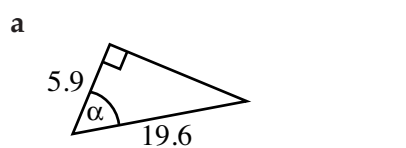
QUESTION 1 Find the size of the angle marked with a pronumeral correct to the nearest minute.



QUESTION 2 Find the size of the angle marked.



QUESTION 3 Find the size of the angle marked.



QUESTION 4 An 18 m ladder standing on level ground reaches 14 m up a vertical wall. Find the angle that the ladder makes with the ground (give your answer to the nearest degree).

QUESTION 5 ABCD is a rectangle with $AC = 25$ cm and $AD = 14$ cm. Find $\angle ACD$ correct to the nearest degree.

Trigonometry and the right-angled triangle

Topic 7 - Exact trigonometric ratios

QUESTION 1 Evaluate the following using the exact values of the trigonometric ratios.

- | | | | | | |
|---|-----------------------------------|---|-----------------------------------|---|-----------------------------------|
| a | $\sin 30 =$ _____ | b | $\sin 60 =$ _____ | c | $\sin 30 \cdot \cos 45 =$ _____ |
| d | $\cos 60 =$ _____ | e | $\cos 45 =$ _____ | f | $\sin 45 \cdot \cos 45 =$ _____ |
| g | $\sin 45 =$ _____ | h | $\tan 60 =$ _____ | i | $\cos 30 =$ _____ |
| j | $\tan 30 =$ _____ | k | $\sin 30 \cdot \cos 60 =$ _____ | l | $\tan 45 =$ _____ |
| m | $\frac{\sin 45}{\cos 45} =$ _____ | n | $\frac{\sin 30}{\cos 30} =$ _____ | o | $\frac{\sin 60}{\tan 60} =$ _____ |
| p | $\frac{\cos 30}{\cos 60} =$ _____ | q | $\frac{\cos 60}{\sin 45} =$ _____ | r | $\frac{\sin 30}{\sin 60} =$ _____ |

QUESTION 2 Prove the following relationships.

- | | | | | | |
|---|-------------------------------------|---|-------------------------------------|---|-------------------------------------|
| a | $\frac{\sin 30}{\cos 30} = \tan 30$ | b | $\frac{\sin 45}{\cos 45} = \tan 45$ | c | $\frac{\sin 60}{\cos 60} = \tan 60$ |
| | _____ | | _____ | | _____ |
| | _____ | | _____ | | _____ |
| d | $2 \sin 30 \cos 30 = \sin 60$ | e | $2 \sin 45 \cos 45 = \sin 90$ | f | $2 \sin 60 \cos 60 = \sin 120$ |
| | _____ | | _____ | | _____ |
| | _____ | | _____ | | _____ |

QUESTION 3 Prove the following results.

- | | | | |
|---|---|---|--------------------------------------|
| a | $\sin 30 \times \cos 60 = \frac{1}{4}$ _____ | b | $\sin 60 + \cos 30 = \sqrt{3}$ _____ |
| | _____ | | _____ |
| c | $\sin 30 + \cos 30 + \cos 45 = \frac{1 + \sqrt{3} + \sqrt{2}}{2}$ _____ | | |
| | _____ | | |

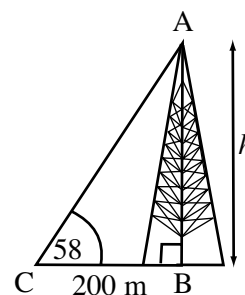
QUESTION 4 A 12 m ladder standing on level ground makes an angle of 60° with the ground. How far up the vertical wall does it reach?

Trigonometry and the right-angled triangle

Topic 8 - Angle of elevation, angle of depression and bearings

QUESTION 1

- a The angle of elevation of the top of a tower AB is 58° from a point C on the ground at a distance of 200 metres from the base of the tower. Calculate the height of the tower to the nearest metre.



- b A man 1.65 m tall is 18 metres away from a tower 25 m high. What is the angle of elevation of the top of the tower from his eyes?

- c From the top of a building 80 metres high, the angle of depression of a car parked on the ground is 52° . Find the distance of the car from the base of the building. (Write your answer correct to two decimal places.)

QUESTION 2

- a A ship sets out from a point A and sails due north to a point B, a distance of 150 km. It then sails due east to a point C. If the bearing of C from A is $048^\circ 37'$, find:

i the distance BC.

ii the distance AC.

- b A ship leaves port for a destination 80 km east and 70 km north. In which direction should it sail?

- c A ship starts from a port P, sails $S46^\circ W$ for a distance of 120 km. Find:

i how far south of P it is.

ii how far west of P it is.

Trigonometry and the right-angled triangle

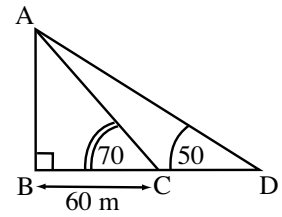
Topic 9 - Problem solving involving two right-angled triangles

QUESTION 1 From the diagram given opposite, find:

- a the length of side AB.

- b the length of side CD.

- c the angle DAC .

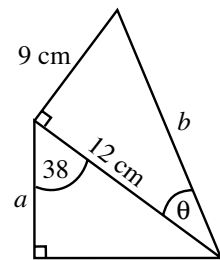


QUESTION 2 In the diagram given opposite, calculate:

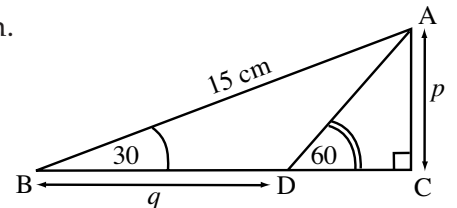
- a the length a (correct to one decimal place).

- b the size of angle θ .

- c the length b .



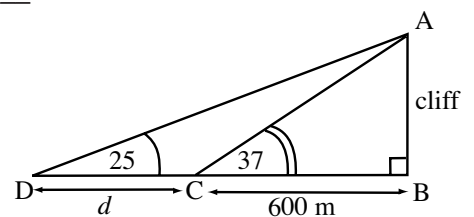
QUESTION 3 Find the value of the unknowns in the given diagram.



QUESTION 4 The angle of elevation of the top of a cliff from a boat 600 m out to sea is 37° . If the boat then travels a further d metres out to sea, the angle of elevation of the cliff is now 25° . Find:

- a the height of the cliff above sea level to the nearest metre.

- b the value of d to the nearest metre.



Trigonometry and the right-angled triangle

Topic Test

PART A

- Instructions** This part consists of 10 multiple-choice questions
Each question is worth 1 mark
Attempt ALL questions
Calculators are NOT to be used
Fill in only ONE CIRCLE for each question

Time allowed: 15 minutes

Total marks = 10

	Marks
1 Use your calculator to find $\sin 36^\circ$ correct to two decimal places. (A) 0.58 (B) 0.57 (C) 0.59 (D) 0.81	1
2 Evaluate $12 \sin 85^\circ$ correct to two decimal places. (A) 12.05 (B) 11.95 (C) 1.05 (D) 137.16	1
3 Find the value of $\frac{\sin 38^\circ - \cos 55^\circ}{\tan 36^\circ}$ correct to one decimal place. (A) 0.2 (B) 0.5 (C) 0.05 (D) 0.1	1
4 If $\sin \theta = \frac{4}{7}$, calculate the size of the angle θ to the nearest degree. (A) 55 (B) 30 (C) 35 (D) 45	1
5 A 3 metre ladder leans against a building with its top reaching a height of 2.6 metres. What angle, to the nearest degree, does the ladder make with the wall? (A) 35 (B) 40 (C) 30 (D) None of these	1
6 In the triangle ABC, the angle B is 90° , AB is 4 m and AC is 5 m. Find the size of angle A correct to the nearest degree. (A) 37 (B) 53 (C) 39 (D) 27	1
7 Jane is flying a kite on a 100 m string that makes an angle of 48° with the horizontal. How high is the kite above Jane's hand? Give your answer correct to the nearest metre. (A) 65 m (B) 82 m (C) 78 m (D) 74 m	1
8 The diagonal of a rectangle makes an angle of 42° with one of the longer sides. If the length of the rectangle is 12 cm, find the length of the diagonal correct to one decimal place. (A) 15.8 m (B) 22.5 m (C) 16.1 m (D) 17.9 m	1
9 From the top of a tower the angle of depression of a boat is 30° . If the tower is 20 m high, how far is the boat from the foot of the tower? (A) 40 m (B) $10\sqrt{3}$ m (C) $20\sqrt{2}$ m (D) $20\sqrt{3}$ m	1
10 If $\cos \theta = \frac{1}{2}$, find the size of angle θ . (A) 30 (B) 60 (C) 45 (D) 55	1

Total marks achieved for PART A

10

Trigonometry and the right-angled triangle

Topic Test

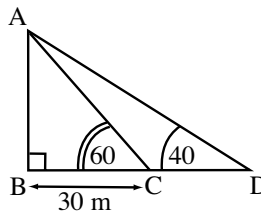
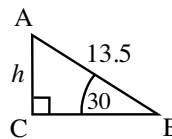
PART B

Instructions This part consists of 15 questions
 Each question is worth 1 mark
 Attempt ALL questions
 Calculators may be used

Time allowed: 20 minutes

Total marks = 15

Questions	Answers only	Marks
Use your calculator to find correct to two decimal places:		
1 $\tan 58$.	_____	1
2 $\sin 63$.	_____	1
3 $19.7 \cos 78$.	_____	1
4 $\frac{28.67}{\sin 46}$.	_____	1
5 $\frac{\sin 35 + \cos 35}{\tan 34}$.	_____	1
6 $\tan 48 - \sin 30 + \cos 73$	_____	1
Calculate the size of each angle to the nearest degree if:		
7 $\cos \theta = \frac{4}{5}$.	_____	1
8 $\sin \theta = \frac{12}{13}$.	_____	1
9 $\tan \theta = 0.6781$.	_____	1
For the triangle ABC given opposite, calculate:		
10 the value of h .	_____	1
11 the size of $\angle A$.	_____	1
12 the length of BC.	_____	1
From the diagram given opposite find:		
13 the length of the side AB.	_____	1
14 the length of the side CD.	_____	1
15 the angle DAC.	_____	1



Total marks achieved for PART B

15