## MVATHLETIGS

## Statistics and Probability


mean mode...
median...


Mathletics Instant Workbooks Im

## Statistics and probability

## Student Book - Series I

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## Practice Tests

Topic 1 - Topic test A $\qquad$
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Author of The Topics and Topic Tests: AS Kalra

## Statistics and probability

## Topic 1: Frequency distribution table

## Question 1

a A survey involves the test results obtained by a class of 24 students. Complete a frequency distribution table for the set of data given below.

| 5 | 9 | 7 | 7 | 5 | 6 | 7 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 7 | 8 | 6 | 6 | 8 | 6 | 5 | 4 |
| 3 | 6 | 7 | 9 | 8 | 9 | 7 | 9 |


| Score (x) | Tally | Frequency (f) |
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b The following table shows the heights in centimetres of 28 students in a class. Complete a frequency distribution table.

| 166 | 169 | 170 | 167 | 171 | 172 | 166 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 168 | 172 | 171 | 169 | 170 | 170 | 167 |
| 173 | 174 | 167 | 168 | 167 | 172 | 171 |
| 174 | 170 | 174 | 172 | 172 | 167 | 165 |


| Score ( $\boldsymbol{x}$ ) | Tally | Frequency ( $\boldsymbol{f}$ ) |
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## Question 2

a A class of 20 students scored the following marks. Draw up a frequency distribution table.

5, 0, 7, 6, 7, 2, 3, 5, 3, 5, 10,
8, 7, 6, 3, 4, 7, 10, 7, 2

| Score (x) | Tally | Frequency ( $f$ ) |
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b Draw up a frequency distribution table for the following set of data.
$7,6,4,6,9,8,6,6,5,7,9$,
$10,9,6,5,6,6,6,10,9$

| Score ( $\boldsymbol{x}$ ) | Tally | Frequency ( $f$ ) |
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## Statistics and probability

## Topic 2: Frequency histogram and frequency polygon

Question 1 Fifty families were surveyed to find how many children each family has and the following set of data was obtained. Draw a frequency histogram and a frequency polygon.

| 5 | 3 | 2 | 4 | 1 | 5 | 0 | 2 | 3 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | 1 | 1 | 3 | 3 | 4 | 1 | 3 | 2 | 1 |
| 3 | 3 | 2 | 2 | 2 | 3 | 2 | 1 | 3 | 1 |
| 2 | 3 | 0 | 1 | 1 | 5 | 3 | 4 | 5 | 0 |
| 3 | 0 | 2 | 0 | 2 | 2 | 1 | 5 | 4 | 3 |



Question 2 The weights of 30 students in a class are shown in the following table. Construct a frequency distribution table and hence draw a frequency histogram and a frequency polygon.

| 52 | 48 | 46 | 53 | 50 | 47 | 50 | 49 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 48 | 51 | 52 | 46 | 48 | 48 | 46 | 49 |
| 48 | 48 | 54 | 50 | 46 | 48 | 46 | 49 |
| 50 | 46 | 52 | 46 | 47 | 51 |  |  |


| Score (x) | Tally | Frequency (f) |
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## Statistics and probability

## Topic 3: Mean

Question 1 Find the mean of the following sets of scores.
a $4,5,6$
b $6,7,8,12$
c $7,8,9,10$
$\qquad$
$\qquad$
$\qquad$
d $10,12,14,18$
$\qquad$
e $5,7,10,12$
f $5,6,9,10,12,18$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
g $2,2,3,3,3,3,4,4,4,4$
h $6,6,7,7,7,8,8,8,8$
i $2,2,5,5,5,6,6,6,6$
$\qquad$
$\qquad$
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$\qquad$

Question 2 Find the mean of the following sets of scores.
a $3,3,3,4,4,5,5,5,5,6,6$
b $2,2,2,3,3,3,3,5,5,5,5,6,6,6,6$
$\qquad$
$\qquad$
$\qquad$
c $5,5,5,7,7,7,7,7,9,9,9,9$
d $5,5,5,6,6,6,7,7,7,7,7,8,8,8,8$
$\qquad$
$\qquad$
$\qquad$

Question 3 Complete the tables below and calculate the mean.


## Statistics and probability

## Topic 4: Mode

Question 1 What is the mode of the following sets of scores?
a $2,2,3,4,4,5,5,5,6,6$
$\qquad$
b $7,8,7,5,3,2,7,6,7,3$
$\qquad$
c $2,3,5,4,2,8,7,2,2$
d $5,3,4,6,5,6,7,5,5$
$\qquad$
e $4,5,6,7,6,8,9,6,4,6$
f $7,8,9,9,9,9,10,7$
$\qquad$
$\qquad$
g $3,4,5,3,5,3,3,6,3,4$
h $2,3,3,2,4,2,5,6,5,3,3$

QUESTION 2 Find the mode of each set of scores.
a $4,3,5,3,6,4,3,5,3$
b $11,10,11,12,9,9,8,11,11,8,11$
$\qquad$
c $7,8,6,9,9,7,9,9,7,6,9,9,10$
d $6,7,9,7,6,7,6,7,7,7,8,7,7$
$\qquad$
e $21,20,21,24,21,22,21,21$
f $4,5,4,3,4,2,4,4,2,4,4$
$\qquad$
$\qquad$
g $52.17,18,52,53,54,52,52,53,52$
h $9,4,5,9,7,9,7,9,6,5,9,9,4,9$
$\qquad$
$\qquad$

Question 3 Select the mode from each of the following sets of scores.
a $3,4,5,4,3,2,4,4,5,4$
b $6,5,8,8,5,8,7,8,9,8,8$
$\qquad$
c $3,4,5,5,6,5,6,5,7,6,5,5,5,4,5$,
d $8,9,10,8,11,8,9,8,10,8,6,8$
$\qquad$
e $2,3,3,4,2,5,2,2,2,6,2,3$
f $5,6,5,5,7,5,6,5,5,5$

## Statistics and probability

## Topic 5: Median

Question 1 Find the median of the following sets of scores.
a $6,7,8$
b $14,17,21$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
c $5,8,10,11,6$
d $13,17,19,15,14$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
e $5,3,6,4,7$
f $20,22,19,17,16$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Question 2 What is the median of each set of scores?
a $6,7,8,9,10$
$\qquad$
b $16,18,11,15,12,17,13,14,18$
$\qquad$
$\qquad$
c $12,62,42,22,52,92,72,82,32$
d $12,4,9,6,5,8,10,11,7,10,12$
$\qquad$
$\qquad$
$\qquad$

e $11,14,9,6,5,6,11,10,8,7,14$
f $5,10,4,8,11,8,6,9,10,11,11$
$\qquad$
$\qquad$
$\qquad$

Question 3 Find the median of the following sets of scores.
a $36,39,31,32,35,36,39$
b $3,2,1,3,0,8,6,6,0$
$\qquad$
$\qquad$
$\qquad$
c $8,11,16,13,12,13,16,11,8,7,8$
$\qquad$
d $7,13,6,10,13,10,8,11,12,13,13$
$\qquad$
e $3,7,9,5,4$
f $16,18,15,13,12$
$\qquad$
$\qquad$
$\qquad$

## Statistics and probability

## Topic 6: Range

Question 1 Find the range of the following sets of scores.
a 2, 6, 8, 1, 3
c $4,8,2,1,5,10$
$\qquad$
e $3,5,5,2,7,9,11$
$\qquad$
g $5,2,7,15,1,18$
i $2,5,1,3,9,2,15$
$\qquad$
b $7,1,0,3,5$
d $9,6,2,1,8,6,7$
f $5,2,3,10,15,2,1$
$\qquad$
h $21,23,29,21,19,10$
j $1,9,10,23,8,7,5$
$\qquad$

Question 2 Find the range of the following sets of scores.
a $2,5,3,8,21,2,5$
b $0,5,1,0,8,15,27$
$\qquad$
c $1,5,3,8,53,5,6,7$
d $2,8,9,13,27,8,31$
$\qquad$
$\qquad$
e $37,6,5,8,41,2,63,69$
f $10,5,1,8,9,25,28,6,34$
$\qquad$
$\qquad$
g $2,5,0,3,9,11,13,15$
h $1,3,5,8,9,15,0$
$\qquad$
i $3,5,17,8,9,0$
j $10,20,30,40,50,60$
$\qquad$
$\qquad$

Question 3 Find the range of the following sets of scores.
a $2,8,9,4,15,7,6,32$
c $5,3,9,18,7,64,32$
d $10,12,20,15,16,7$
$\qquad$
e $46,33,46,10,10,44$
g $12,17,15,37,31$
f $13,21,20,27,25,27$
$\qquad$
b $5,6,7,2,3,8,14,17,5$
$\qquad$
$\qquad$
10,12,20,15,16,7
h $124,132,116,132,128,166$

## Statistics and probability

## Topic 7: Miscellaneous questions

Question 1 A class of 20 students scored the following marks (out of 10) in a mathematics test:

| 5 | 1 | 7 | 6 | 7 | 9 | 8 | 7 | 6 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | 3 | 5 | 3 | 5 | 4 | 7 | 9 | 7 | 2 |

a Draw up a frequency distribution table.
b Draw a frequency histogram.
c Draw a frequency polygon.
d Calculate the mean.
e Calculate the mode. $\qquad$
f Calculate the median. $\qquad$
g Calculate the range. $\qquad$

| Score ( $x$ ) | Tally | Frequency ( $f$ ) |
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Question 2 Below are the number of goals scored by a soccer team in 30 matches.

| 3 | 0 | 2 | 1 | 5 | 2 | 1 | 4 | 2 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 4 | 1 | 3 | 0 | 3 | 2 | 3 | 1 | 2 |
| 1 | 0 | 4 | 2 | 2 | 0 | 1 | 5 | 2 | 1 |

a Organise these scores into a frequency distribution table.
b Draw a frequency histogram.
c Draw a frequency polygon.
d Calculate the mean. $\qquad$
e Calculate the mode. $\qquad$
f Find the median. $\qquad$
g Find the range. $\qquad$

| Score ( $x$ ) | Tally | Frequency ( $f$ ) |
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Score


## Statistics and probability

## Topic 8: Basic probability

Question 1 A bag contains 7 red, 10 blue and 3 yellow balls. If a ball is drawn at random, find the probability that it is
a blue $\qquad$ b red $\qquad$ c yellow $\qquad$
d not red $\qquad$ e non yellow $\qquad$
f white $\qquad$

Question 2 A die is thrown once. Find the probability that it is
a a six $\qquad$
b an odd number $\qquad$
c an even number $\qquad$ d one or five $\qquad$
e zero $\qquad$ f any number from 1 to 6 $\qquad$

Question 3 From the letters of the word 'AUSTRALIA', one letter is selected at random. What is the probability that the letter is
a a vowel $\qquad$ b a consonant $\qquad$
c the letter A $\qquad$ d the letter S

Question 4 A card is drawn at random from a normal pack of 52 cards. Find the probability that the card is
a a spade $\qquad$ b a black card $\qquad$ c a queen $\qquad$
d a red card $\qquad$
e not a club $\qquad$
f an ace or a jack $\qquad$

Question 5 A three-digit number is to be formed from the digits 4, 5 and 9. What is the probability that:
a the number formed is odd? $\qquad$ b the number formed is even? $\qquad$
c the number is less than 900 ? $\qquad$ d the number is divisible by 5 ? $\qquad$

Question 6 The numbers from 1 to 10 are written on separate cards. One card is chosen at random. What is the probability that the number is:
a odd $\qquad$ b even $\qquad$
c seven $\qquad$ d more than seven $\qquad$
e less than seven $\qquad$ f zero
g a prime number $\qquad$ h divisible by 3
i a factor of 5 $\qquad$ j a multiple of 4

## Statistics and probability

## Topic 9: Probability and tree diagrams

Question 1 A coin is tossed twice. What is the probablility of having
a two heads? $\qquad$
b a head and tail in any order? $\qquad$
c two tails? $\qquad$
d no heads? $\qquad$

Question 2 There are four cards marked with the numbers 2, 3, 4 and 5. They are put in a box. Two cards are selected at random one after the other to form a two-digit number.
a How many different two-digit numbers can be formed? $\qquad$
b The probability of a number less than $35=$ $\qquad$
c The probability that the number formed is divisible by $5=$ $\qquad$
d The probability of an odd number $=$ $\qquad$
e The probability of an even number $=$ $\qquad$
f The probability of a number greater than $50=$ $\qquad$

QUESTION 3 Michelle has a box containing one red marble and two green marbles. She selects two marbles at random. Find the probability of
a two green marbles if she replaces the first marble before she selects the second. $\qquad$
b one red marble if she does not replace the first marble. $\qquad$

Question 4 Three coins are tossed together. What is the probability that
a two heads and a tail will be thrown? $\qquad$
b three heads will be thrown? $\qquad$

## Statistics and probability

## Topic 10: Problem solving, statistics and probability

1 What is the mean of the first five counting numbers? $\qquad$

2 What is the mean of the squares of each of the first five counting numbers? $\qquad$

3 If 6 is added to each of the first five counting numbers, find the new mean. $\qquad$

4 John's average weekly income is $\$ 450$. What is his yearly income? $\qquad$

5 Chris covers an average distance of 125 km per day. How many kilometres are covered in 30 days? $\qquad$

6 When a die is thrown, what is the probability of an even number turning up? $\qquad$

7 A bag contains 3 red marbles and 5 blue marbles. If one marble is drawn at random, what is the probability of drawing a red marble? $\qquad$

8 If the probability of an event occurring is $\frac{7}{10}$, how many times would you expect it to occur in 80 trials? $\qquad$

9 A card is drawn from a pack of 52. What is the probability of a King being drawn? $\qquad$

10 Jan had a weekly average income of $\$ 320$ for four weeks. If she earned $\$ 300, \$ 350$ and $\$ 340$ in the first three weeks, what was her income in the fourth week? $\qquad$

## Statistics and probability

Topic Test
PART A
Instructions This part consists of 12 multiple-choice questions
Each question is worth 1 mark
Fill in only ONE CIRCLE for each question
Calculators are NOT allowed
Time allowed: 15 minutes
Total marks $\mathbf{= 1 2}$

1 From the set of scores $3,5,4,6,5,5,3,5,4,5$ the mode is
(A) 6
(B) 5
(C) 4.5
(D) 4

2 The range of the set of scores $8,9,11,6,9,8,5,7,13,6$ equals
(A) 7
(B) 9
(C) 4
(D) 8

3 What is the difference between the mean and the mode of scores $30,50,60,30,70$ ?
(A) 2
(B) 12
(C) 18
(D) 20

4 'HOW NOW BROWN COW'. Which of the answers below gives the mode?
(A) O only
(B) W only
(C) O and W only
(D) $\mathrm{O}, \mathrm{W}$ and N

5 The mean of the set of scores $3,5,3,3,7,3,6,5,4,3$ equals
(A) 4.1
(B) 4.2
(C) 3
(D) 5

6 The median of the set of scores $2,5,3,6,2,2,7,8,2,3,4$ equals
(A) 2
(B) 3
(C) 4
(D) 5

7 From a normal pack of 52 playing cards, one card is selected at random. The probability of a diamond is
(A) $\frac{1}{13}$
(B) $\frac{2}{13}$
(C) $\frac{1}{4}$
(D) $\frac{3}{4}$

8 A card is chosen at random from a pack of 52 playing cards. What is the probability that the card is red?
(A) $\frac{1}{4}$
(B) $\frac{1}{3}$
(C) $\frac{1}{2}$
(D) $\frac{3}{4}$

9 In a single throw of one die, find the probability of having an even number.
(A) $\frac{1}{6}$
(B) $\frac{1}{3}$
(C) $\frac{1}{2}$
(D) $\frac{2}{3}$

10 In a toss of two coins, find the probability of having two tails.
(A) $\frac{1}{2}$
(B) $\frac{1}{3}$
(C) $\frac{1}{4}$
(D) 1

11 A bag contains four white, three red and two black balls. If a ball is drawn at random, the probability of a white ball is
(A) $\frac{3}{9}$
(B) $\frac{4}{9}$
(C) $\frac{2}{9}$
(D) $\frac{5}{9}$

12 A card is chosen at random from a pack of 52 cards. What is the probability that the card is an ace?
(A) $\frac{1}{4}$
(B) $\frac{1}{2}$
(C) $\frac{1}{13}$
(D) $\frac{2}{13}$

## Statistics and probability

## Topic Test

PART B

## Instructions This part consists of 15 questions <br> Each question is worth 1 mark <br> Write answers in the answers-only column

## Time allowed: $\mathbf{2 0}$ minutes

Total marks $=15$

## Questions

For the given set of scores 3, 5, 3, 3, 7, 3, 6, 5, 4, 3 find
1 the mean
2 the mode
3 the median
4 the range
For the set of scores given opposite, find
5 the mode
6 the mean
7 the median
8 the range

| Score | Frequency |
| :---: | :---: |
| 6 | 4 |
| 7 | 5 |
| 8 | 7 |
| 9 | 6 |
| 10 | 3 |

In a single throw of one die, find the probability of
9 an odd number
10 a three
11 a seven
A bag contains five red, seven blue and three white balls. If a ball is drawn at random, find the probability that it is

12 a red ball
13 a blue ball
14 a white ball
15 not a white ball


