A Complete Guide to ...



Utilising the objectives as written in

MATHEMATICS in the New Zealand CURRICULUM

for

Level 3

This resource contains:

- ☑ Table of contents
- ☑ Teaching notes
- ☑ In class activity sheets involving
 - worked examples
 - basic skills
 - word problems
 - problem solving
 - group work

☑ Homework / Assessment activity sheets

☑ Answers

These resources are supplied as PHOTOCOPY MASTERS

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This resource unit may be used as a master, and therefore can be photocopied, only by the school or institution that has purchased this resource unit.

Note from the author:



This resource ...

***A Complete Guide to Statistics**

is one of a series of FIVE resources written utilising the objectives as stated in

Mathematics in the New Zealand Curriculum for Level 3.

With my experiences as a specialist mathematics teacher, I enjoyed mathematics as a subject, but I am aware that not all teachers feel the same way about mathematics. It can be a difficult subject to teach, especially if you are unsure of the content or curriculum and if resources are limited.

This series of resources has been written with you in mind. I am sure you will find this resource easy to use and of benefit to you and your class.



For more information about these and other resources, please contact ...





Acknowledgement:

I would like to thank the staff and pupils of **Mairehau Primary School, Christchurch** for their assistance in making these resources possible.

This resource has been divided into EIGHT sections as listed below.

Although there are no page numbers, the sections follow in sequential order as listed.

Note: 'In-class' Worksheets Masters are lesson by lesson reuseable worksheets that can be photocopied or copied on to an OHP.

Homework / **Assessment Worksheets Masters** can be used as homework to reinforce work covered in class or they can be used for pupil assessment.





Statistics

The following are the objectives for Statistics, Level 3, as written in the

MATHEMATICS in the New Zealand Curriculum document, first published 1992. [REFER PAGE 178]

Statistical investigations

Within a range of meaningful contexts, students should be able to:

- **S1** plan a statistical investigation of an assertion about a situation;
- S2 collect and display discrete numeric data in stem-and-leaf graphs, and strip graphs, as appropriate.

Interpreting statistical reports

Within a range of meaningful contexts, students should be able to:

- S3 use their own language to talk about the distinctive features, such as outliers and clusters, in their own and others' data displays;
- S4 make sensible statements about an assertion on the basis of the evidence of a statistical investigation.

Exploring probability

Within a range of meaningful contexts, students should be able to:

- S5 use a systematic approach to count a set of possible outcomes;
- **S6** predict the likelihood of the outcomes on the basis of a set of observations.

At the top of each 'In-class' worksheet and Homework / Assessment worksheet, the Statistics objective(s) being covered has been indicated. *EXAMPLE:* **S1** means objective 1, **S2** means objective 2, etc.



The Mathematical Processes Skills: Problem Solving,

Developing Logic & Reasoning, Communicating Mathematical Ideas,

are learned and assessed within the context of the more specific knowledge and skills of number, measurement, geometry, algebra and statistics. The following are the **Mathematical Processes Objectives** for **Level 3**.

Problem Solving Achievement Objectives [Refer page24]

- MP1 pose questions for mathematical exploration;
- MP2 effectively plan mathematical exploration;
- MP3 devise and use problem-solving strategies to explore situations mathematically;
- **MP6** use equipment appropriately when exploring mathematical ideas.

Developing Logic and Reasoning Achievement Objectives [Refer page26

- MP8 classify objects, numbers and ideas;
- **MP9** interpret information and results in context;
- **MP14** use words and symbols to describe and continue patterns.

Communicating Mathematical Ideas Achievement Objectives [Refer page28]

- **MP15** use their own language and mathematical language and diagrams to explain mathematical ideas;
- **MP16** devise and follow a set of instructions to carry out a mathematical activity;
- MP18 record, in an organised way, and talk about the results of mathematical exploration.

Note:

The codes MP1, MP2, etc. have been created by numbering the Mathematical Processes Achievement Objectives in order as listed in the MATHEMATICS in the New Zealand Curriculum document. The numbering gaps occur as not all objectives are covered at Level 3. [REFER TO PAGES 23 - 29 OF THE CURRICULUM DOCUMENT]

'In-class' Statistics Worksheets Table of Worksheet Number / Objectives Covered

See the opposite page for details of each objective.

	St	Statistics Objectives				Mathematical Processes Objectives										
Worksheet Number	S 1	S 2	S 3	S 4	S 5	S 6	МР 1	MP 2	MP 3	МР 6	MP 8	МР 9	MP 14	MP 15	MP 16	MP 18
1	*						*	*	×					*	*	
2		*						*	*			*		*	*	*
3		*						*	*			*		*		*
4		*						*	*			*		*		*
5		*	*					*				*		×		*
6		*	*					*				*		×		*
7		*						*				*		*		*
8		*	*					*	×			*		*	*	*
9			*	*								*			*	*
10			*									*			*	
11			*	*				*	*			*			*	*
12			*	*								*			*	
13			*	*								*			*	
14			*	*								*		*	*	*
15			*	*								*		*	*	*
16			*	*				*	*			*		*	*	*
17					*				*			*		*	*	*
18					*				*			×		×	*	*
19						*						*				
20		*				*		*	*			*		*	*	*

Table of Contents for the 'In-class' Worksheet Masters for Statistics, Level 3

Worksheet Number	Торіс	Statistics Objective(s)
1	Planning an investigation	S1
2	Collecting and organising data / creating tally charts / carrying out an investigation	S2
3	Creating column graphs	S2
4	Creating pictograms	S2
5	Creating stem and leaf graphs	S2 / S3
6	Creating dot plot graphs	S2 / S3
7	Creating strip graphs	S2
8	Creating time-series graphs	S2 / S3
9	Finding the mean (average)	S3 / S4
10	Finding the median (middle score)	S3
11	Finding the mode (most common)	S3 / S4
12	Finding the range	S3 / S4
13	Mean, median, mode & range	S3 / S4
14	Understanding data displays	S3 / S4
15	Understanding data displays	S3 / S4
16	Creating statistical reports	S3 / S4
17	Finding all possible outcomes using boxes	S5
18	Finding all possible outcomes using tree diagrams	S5
19	Using language associated with chance	S6
20	Using data to predict outcomes	S2 / S6
	Teaching Notes / Answers	



Every year the Mairehau Primary School Home & School Committee organises a school fair, with the help of parents, teachers and pupils. The money raised is used to improve the school environment in some way.



plant trees around the school?

Planning an Investigation

With the money raised this year the pupils want new playground equipment, teachers want new computers and the principal wants more library books. Who should decide?

Task 1

Working on your own, or in a small group, plan an investigation on how YOU would work out how the money raised from the fair should be spent.

- Write a plan of how you are going to conduct this investigation.
 - Are you going to use a questionnaire? 溵 What questions should you ask?
 - Who are you going to ask and why?
 - How are you going to ask these guestions? Example: ring people up, ask people at the school gate, etc.

Task 2

AWS

Present your plan to the class.

Other topics you may like to investigate could include:

- should the school have a school uniform?
- changes to the school uniform
- where to go on a school trip?
- how much homework should you have each night?

favourite television programmes

- favourite music groups
- favourite sports
- favourite pets

or any other topic that is of interest to you.

Who should Lask?



Collecting and Organising Data

Discussion:

Look at this list of vowels. [a, i, e, a, o, u, i, a, u, u]

Because there were only 10 vowels it was easy to work out, but if there were 50 or 100 vowels, how could you work out the number of times each vowel occurred?

Using a tally chart can help.

Example:

u, o, o, i, a, u, e, e, i, o, i, u, e, a, e, u, i, o, e, i ,a, o, u ,u, a, e, o, i, e, u

Make a mark in the **tally column** next to the vowel as you go through the list. Remember to mark off in 5's, **##** means 5.

Frequency means 'how often something occurs'. Add up the frequency column to find out how many vowels there were. Answer, 30 vowels.

Creating Tally Charts

Task 3

Pupils in a class were asked how many pets they each had.

- 1. Create a **tally chart** to display these results.
- 2. How many pupils had 2 pets?
- 3. How many pupils are in this class?

Pupils in Room 5 were asked how they travelled to school.

- 4. Create a **tally chart** to display these results.
- 5. How many pupils walked to school?
- 6. How many pupils biked to school?
- 7. How many pupils in this class?

Mr. McGregor has a problem with caterpillars on his cabbages. One day he counted the number of caterpillars = on each cabbage plant. These were his results.

5, 6, 9, 5, 7, 8, 6, 7, 10, 7, 5, 6, 8, 9, 6, 7, 8, 7, 9, 6, 7, 7, 6, 8, 9, 10, 9, 7, 8, 7, 8, 9, 10, 5, 6, 5, 8, 6, 4, 6, 8, 7, 9, 4, 5, 6, 9, 5, 7, 4, 10, 9 How many are there of each vowel?

Tally chart of the vowels in the list.

Vowel	Tally	Frequency
а	1111	4
е	HHT II	7
i	HHT I	6
0	₩r I	6
u	HHT II	7
		30



Ē	

walk, bike, bus, walk, bike, bike, car, walk, car, bike, bus, car, walk, walk, bike, walk, bike, walk, bus, bus, car, walk, walk, bike

- 8. Create a **tally chart** to display these results.
- 9. What was the most common number of caterpillars on a cabbage?
- 10. How many cabbage plants were there?



Carrying out an Investigation

Task 4

Using the plan you created in **Task 1** worksheet 1, collect the data you need so that you can work out how the school is going to spend the money raised at the school fair. Present your results in a **tally chart**.





Creating Column Graphs

Displaying Data:

Column Graphs

Data that has been collected using a tally chart can be displayed in several ways. Example:



All column graphs should have ...

- a title or name.
- a label on each axis (lines with arrows),
- a scale on the frequency axis,
- gaps between columns.
- all columns should be the same width

From this graph we can see that there were 8 e's. How many u's were there?

Task 5

Jim counted the number of cars going past the school gate in 30 minutes. He noted the colour of each car.

Pupils in the year 5 & 6 classes have to choose one sport to play during the winter. This table shows their choices.

On a school camp, pupils can have either an apple, a banana, an orange or a pear for afternoon tea. This is what they selected.



Car Colour	Frequency	1.
red	8	
white	9	3.
blue	7	
grey	5	
black	6	4.
		5.

<u>A</u>	Sport	Total
	netball	11
	hockey	16
	rugby	12
	soccer	13

Create a **column graph** to display his results.

What was the most common car colour? How many more white cars than grey cars were there?



What colour of car came past the gate 8 times? How many cars did Jim count altogether?

- Create a **column graph** to display these 6. results.
- 7. What sport was most popular?



- How many wanted to play soccer? 8. If both classes have the same number of 9
 - pupils in them, how many are there in each class?

banana, apple, orange, orange, pear, banana, pear, orange, pear, apple, apple, orange, pear, banana, pear, pear, apple, apple, pear, orange, banana, orange, pear, orange, apple, pear, apple, apple, pear, apple, banana, pear, orange, pear



- 11. 12.
- Organise this data into a **tally chart**.
 - Create a **column graph** using your tally chart results.





- 13. What fruit was chosen 5 times?
- 14. If all pupils on camp ate fruit, how many pupils were on camp?

Create column graphs from the tally charts you created in Task 3, Worksheet 2. 15.

Carrying out an Investigation

Task 6

Using the tally chart you created in **Task 4**, **Worksheet 2** create a **column graph** of your results.



Pictograms

Data that has been collected using a tally chart can be displayed in several ways. *Example:*





Pictograms represent data with pictures. All pictograms should have ...

- ctograms should hav □ a title or name,
- □ a key.

a scale stating how many each picture represents.
 From this pictogram we can see that there were 4 e's drawn, so therefore there were 8 e's in the sentence.
 How many vowels are represented by a 'half' diagram in this pictogram, such as in the a's and u's ?

Creating Pictograms

Task 7



3.

4.





- 1. Draw a **pictogram** to display these results.
- 2. How many pupils in Jacqui's class?

During June, at 3:00 p.m. each day, the weather was recorded as either sunny, cloudy or raining. This table shows the results, but the rainy days were not noted.







Weather	Total
sunny	10
cloudy	5
raining	?

On how many days in June was it raining at 3:00 p.m.? Draw a **pictogram** to display these results.

On a school camp, pupils can have a biscuit or a piece of cake, some ice-cream and a drink for dessert. The box shows what they selected.



drink, cake, drink, ice-cream, drink, biscuit, cake, ice-cream, biscuit, cake, ice-cream, drink, ice-cream, biscuit, drink, cake, ice-cream, drink, biscuit, drink, ice-cream, ice-cream, drink, drink, biscuit, cake, drink, ice-cream, drink, cake, cake, drink



- Organise this data into a **tally chart**.
- Create a **pictogram** using your tally chart results.
- What was more popular, cake or biscuits?
- If half the class had ice-cream, how many in the class?
- How many in the class DID NOT have a drink?

10. Create pictograms from the tally charts you created in Task 3, Worksheet 2.

Carrying out an Investigation

Task 8

Using the tally chart you created in Task 4, Worksheet 2, create a pictogram of your results.



Stem & Leaf Graphs

1 2, 7, 5, 8, 6

3 4, 1, 0, 7

Number of cards pupils have collected

2 3, 5, 0, 7, 9, 4, 1, 7, 3

Data can be organised using a stem and leaf graph, without having to draw a tally chart.

Example:

Pupils have been collecting cards from packets of chips. Below is a list of how many cards each pupil has collected.



12, 23, 34, 25, 17, 20, 31, 15, 27, 29, 30, 24, 21, 27, 37, 18, 23, 16

As these numbers are in the 10's, 20's or 30's, the numbers 1,

2 and 3 form the **stem** of the graph.

The second numbers or digits form the leaf part of the graph and can be added to the graph in the order listed.

Understanding Stem & Leaf Graphs



1. List the numbers that are represented in these stem & leaf graphs.

> Number of books pupils have read this year.



0 7, 9, 3, 5 1 5, 6, 2 ,0, 6 ,9 2 2, 6, 7, 3, 1 3 2, 0

2. How many pupils in the class? Time taken on telephone toll calls



during a long weekend (minutes)

2, 0, 9, 5, 3, 4 3 9, 5, 4, 7, 6, 3, 1 4 8, 2, 7, 0 5 6, 2, 7, 9, 0





What were the longest and shortest toll calls?

Creating Stem & Leaf Graphs

3.



A survey was conducted to find out how much families spent on 'take-aways' each week. The results are shown in this box below (rounded to the nearest dollar).





- Create a stem & leaf graph for these results.
- What was the least amount spent on 'take-aways'?

How many families were surveyed?

A class was given a test to find out multiplication facts. The results a

4. Create a **stem & leaf** graph

t how well they knew their basic	41, 37, 28
re shown in Box A.	27, 31, 26
n for the results in Box A.	25, 36, 37

5. What were the lowest and highest marks in the test?

The class was given two weeks to relearn the basic multiplication facts before being given the same test again. The results of the second test are shown in Box B.

- Create a stem & leaf graph for the results in Box B. 6.
- 7. What were the new lowest and highest marks in the second test?
- 8. What do you think the test was out of?
- 9. Did the class improve? Can you tell this from looking at the two stem and leaf graphs? Explain your answer.

Box A			
41, 37, 28, 31, 37, 39, 41,			
27, 31, 26, 34, 27, 39, 28,			
25, 36, 37, 42, 24, 39, 31,			
28, 35, 37, 42, 29, 24, 30			

Box B						
29,	36,	39,	42,	48,	46,	38,
45,	37,	32,	46,	50,	41,	39,
37,	29,	36,	48,	46,	32,	46,

37, 30, 46, 40, 46, 37, 34



Dot Plot Graphs

Data can be organised using a dot plot graph, without having to draw a tally chart.

Example:

Pupils have just started collecting cards from packets of chips. Below is a list of how many cards each pupil has collected.



Name	Total
David	7
Wendy	4
Rangi	3
Melissa	5
Miri	6



All dot plot graphs should have ...

□ a title or name, □ a label on each axis,

 $\hfill\square$ a scale on the frequency axis

New dots could be added to the graph in any order.

Creating Dot Plot Graphs

Task 11

15 pupils were asked to choose their favourite colour from this

- list: blue, red, white and black. Their choices are shown in this table.
 Create a **dot plot graph** to display these results.
- Create a **dot plot graph** to display these results.
 What was the most favourite colour chosen?
- What was the most favourite colour chosen?
 Four more pupils choose blue, blue, red and white. Add these to the graph.

Every day for two school weeks (Monday to Friday), Jason recorded his mark in the '10 Quick Questions', done at the beginning of each maths lesson.

These were his marks.

- 4. Create a **dot plot graph** to display his results.
- 5. What was his most common mark?
- 6. On what day did he score 6 out of 10?

A radio station ran a competition with a walkman, CD player, video camera and televison as prizes. People were asked what they would like, if they

won first prize. Their

choices are in the box.

7. 8. 9.

9. 10. 11.

walkman, TV, CD player, video camera, TV, walkman, CD player, walkman, CD player, video camera, TV, CD player, TV, CD player, video camera, walkman, video camera, CD player, TV, walkman, TV, video camera, TV, CD player, TV

Create a **dot plot graph** to display their choices. What was the most popular prize chosen? How many people chose a walkman as their prize? How many people were asked altogether?

What prize would you have chosen?

12. Create dot plot graphs from the tally charts you created in Task 3, Worksheet 2.

Task 12

Using the tally chart you created in **Task 4 Worksheet 2** create a **dot plot graph** of your results.

Colour	Total
blue	4
red	3
white	6
black	2

Strip Graphs

Data that has been collected using a tally chart can be displayed in several ways.

Example:

House points have been awarded during the school athletic sports. This strip graph shows the results.

Points scored by each House

Each square = 10 points

All strip graphs should have ...

- a title or name.
- a key.
- a scale stating how many each square represents.

From this strip graph we can see that there were 3 squares for Blue House. This means they scored $3 \times$ 10 points = 30 points at the sports.

Understanding Strip Graphs

Task 13

The strip graph below shows what Karen did with money she was given for her birthday.

Each square = \$8.00

- How much money does each
- square in the strip graph represent? How much did she spend on books? 2.
- How much did she spend on clothes? 3.
- 4 How much did she save?

Creating Strip Graphs

Task 14

In Emma's class pupils wear different styles of footwear. This table shows the style of shoes worn.

Draw a strip graph that

is NINE squares long, where each square represents 3 pupils' shoes.

- 2. Shade in the squares needed to display these results.
- 3. How many pupils in Emma's class?

In Brett's class there are 12 boys and 16 girls. Draw a strip graph that is SEVEN squares long and shade in the squares needed to display these results.

In Tim's class pupils were asked what pets they had at home. The box below shows what pets they have.

4.

- Organise this data into a tally chart. 5.
- 6. How many pupils have a horse?
- How many pupils have a dog? 7.
- How many pupils have a sheep? 8.
- 9. How many pets were there altogether?
- 10. Use your tally chart results to create a strip graph to display these results.

Time-Series Graphs

Data that changes with time can be graphed on a time-series graph.

Example:

Michael has been unwell. He recorded his temperature every hour for 4 hours. These results are shown on the graph.

All time-series graphs should have

- a title or name,
- time on the bottom axis
- label and scale on each axis
- □ or X to mark each point, joined by lines.

From this graph we can see that Michael's temperature was 39°C after two hours. What was his temperature after 4 hrs?

Creating Time-Series Graphs

3

Task 15

During a school week, Monday to Friday, Wendy recorded the number of pupils away from class each day.

Below is a table of her findings.

Mon	Tues	Wed	Thur	Fri
5	2	3	1	4

Every day after school, for 1 week, the number of cars parked in the wrong place outside the school gate was noted.

These results are shown in the table.

7. 8

- 4. Create a time-series graph to display these results.
- 5. On what day were there 5 cars parked in the wrong place?
- 6. What would be a good way to tell the parents NOT to park in the wrong place?

Every day Jim goes for a run around the same course.

He records the time it takes him, to the nearest minute. He has run 7 times so far and these are his times.

Create a time-series graph to display his times. What was his most common time taken to run the course?

Each day for a week, starting on Sunday, the air temperature ($^{\circ}C$) at the airport at 3:00 p.m. was recorded. These were the results.

23°C	26°C	13⁰C	19ºC	24°C	26°C	18°C
------	------	------	------	------	------	------

- 9. Create a time-series graph to display these results.
- 10. What day(s) of the week was the temperature highest?
- 11. On what day do you think it might have rained? Explain why.

Collecting Time-Series Data

Task 16

Using a thermometer, record the temperature of your classroom every 30 minutes, or each hour, of the school day. Create a time-series graph of your results.

- Create a time-series graph to display these results.
- On what day of the week were the most pupils away?
- On what day were there 2 pupils away?

Mon	Tues	Wed	Thur	Fri
3	5	2	6	4

Data Calculations:

Finding the Mean (Average)

Looking at any data display graph can tell you a lot about the data, but there are some calculations you can do that will give you more information about the data, that you cannot get by just looking at a graph.

Example:

Three boys each have some blocks as shown below.

How many blocks are there altogether?

If you collected all blocks and then shared them equally among the three boys, how many blocks would each boy get?

By doing this you are finding the 'average' or **mean** number of blocks that the boys would have.

Answer: The mean number of blocks each boy would have is 3.

To find the **mean** for a list of scores (numbers), there are two steps. Step 1: **Add** up all the scores. Step 2: **Divide** this total by the number of scores you added up.

Example; Find the **mean** of 5, 6, 7 & 10.

This would be the working:

ng: Add up the scores, 5 + 6 + 7 + 10 = 28, There are four scores, so divide by 4, 28 ÷ 4 = 7 Answer: **Mean** = 7

Task 17

Find the **mean** (average) for each list of scores below.

1.	5, 9	2.	10, 16	3.	17, 13
4.	5, 8, 8	5.	7, 10, 13	6.	3, 4, 5, 8
7.	5, 8, 10, 13	8.	9, 9, 13, 17	9.	10, 30, 40 ,40
10.	4, 7, 9, 12, 13	11.	4, 5, 8, 9, 10, 12	12.	3, 5, 6, 8, 6, 4, 7, 9

Each week the pupils in Mr. Stevenson's class are expected to read books, as part of their homework. He hopes they will read 2 or 3 books each per week. Last week this is the number of books each pupil read.

4, 3, 2, 5, 1, 3, 4, 3, 2, 3, 4, 2

- 13. How many pupils in Mr. Stevenson's class?
- 14. Find the **mean** number of books read by the pupils in his class.
- 15. Would Mr. Stevenson be happy with the class mean? Explain.

Mr Stevenson gave his class a maths test on fractions, marked out of 10. Mr Stevenson said, "The class will have to do the test again, if the class mean is less than 7!" The results were as follows.

(8, 5, 6, 1, 8, 8, 9, 3, 9, 6, 7, 2)

Just by looking at the results, do you think the class average is higher than 7?
 Find the **mean** of this test. Will Mr. Stevenson be pleased or not? Explain.

Data Calculations:

Finding the Median (Middle Score)

Looking at any data display graph can tell you a lot about the data, but there are some calculations you can do that will give you more information about the data, that you cannot get by just looking at a graph. Finding the **mean** is one type of 'average', but so is the **median**.

The **median** is the middle score or number, once the scores are in order from smallest to biggest.

Example:

Task 18

The results of a class test are listed below.

from smallest to biggest. In this example, the scores in order would be ...

To find the **median**, scores must be placed in order

5, 6, 7, 8, 9, 10, 10

6, 8, 10, 10, 9, 7, 5

What is the **median** or 'middle' score?

Then, start counting one off each end, keep going until you have one score left in the middle What number is in the middle of this list, as this is the **median**? Answer: The number 8 is the **median**.

Find the **median** (middle score) for each list of scores below. (Remember scores must be in order)

1.	4, 8, 9	2.	4, 6, 6, 7, 9	3.	4, 9, 12, 13, 16, 19, 21
4.	1, 3, 4, 6, 8, 9, 9	5.	6, 8, 9, 15, 17, 18, 21	6.	2, 3, 3, 4, 5, 6, 7, 8, 9, 9, 11
7.	6, 4, 9	8.	7, 6, 1, 3, 8	9.	5, 2, 4, 7, 9, 4, 5

In the questions above, there is an odd number of scores and one number is left in the middle. When you have an even number of scores, there will be two scores left in the middle.

The **median** or middle score, is taken as halfway between the two middle scores.

Example: 3, 6, 8, 9 6 & 8 are in the middle, Halfway between 6 & 8 is 7. The **median** is 7.

Find the **median** (middle score) for each list of scores below. (Remember scores must be in order)

10.	1, 5, 7, 8	11.	4, 6, 10, 12	12.	1, 3, 6, 8, 12, 16
13.	6, 8, 9, 13, 14, 17	14.	8, 10, 15, 17, 19, 22	15.	3, 6, 6, 7, 8, 10, 10, 12
16.	6, 2, 7, 4	17.	3, 10, 8, 7, 10, 12	18.	6, 15, 6, 8, 13, 7, 12, 17

Miri likes throwing her frisbee. She threw it 7 times and measured the distance to the nearest metre. These were her results.

(34, 25, 42, 39, 45, 29, 31)

19. Find the **median** distance (m) the frisbee was thrown.

During the holidays these girls set up a lemonade stall. They recorded the number of glasses of lemonade sold each day. These results are listed below.

(5, 6, 8, 4, 10, 6, 9, 10, 8, 2, 3, 8, 9, 5)

20. Find the **median** number of glasses of lemonade sold.

Example:

For the scores For the scores 4, 5, 5, 6, 7, 7, 8 2, 3, 5, 6, 7, 8, 9

2.

8.

3.

6.

9.

6, 9, 7, 5, 6, 3, 8, 7

7, 6, 9, 2, 7, 5, 3, 9, 6, 7

1, 6, 0, 8, 7, 9, 4, 5, 3, 2

Task 19

Find the **mode** (most common score) for each list of scores below. (Remember there may not be one)

6, 8, 7, 6, 5, 9, 10

5. 6, 8, 10, 9, 10, 8, 9, 5

- 1. 1, 2, 3, 7, 6, 3
- 4. 6, 4, 8, 3, 7, 11, 12, 9
- 7. 3, 6, 8, 2, 4, 6, 9, 3, 2, 4

Every time a T-shirt is sold, its size is noted. During the morning these T-shirts were sold.

size 8, size 10, size 8, size 8, size10, size 12, size 10, size 12, size 14, size 10, size 8, size 10, size 12, size 10, size 12, size 12, size 8, size 10

6, 9, 5, 2, 3, 7, 6, 9, 4, 6

- 10. Organise the data into a **tally chart**.
- 11. Use your tally chart to find the **mode** or most common size of T-shirt sold.
- 12. Why would it be helpful for a shop-keeper to record this information?

During the weekend toll calls are only \$5.00 and you can talk for as long as you like. In the box below are the length of twenty tolls to the nearest minute.

13. Find the **mode** or most common time for a toll call.

Data Calculations:

Finding the Range (Spread)

Looking at any data display graph can tell you a lot about the data, but there are some calculations you can do that will give you more information about the data, that you may not be able to get by just looking at a graph. The difference between the highest and lowest score may be useful to know. This is called the **range** or spread of the scores.

Example:

In the school cross-country the fastest time was 23 minutes and the slowest time was 39 minutes.

What is the range of these times?

Answer: 39 - 23 = 16 minutes. The range is 16 minutes

Range = Highest score – Lowest score

Task 20

Find the range (spread) for each list of scores below.

1.	4, 8, 9	2.	4, 6, 6, 7, 9	3.	4, 9, 12, 13, 16, 19
4.	1, 3, 4, 6, 8, 9, 9	5.	6, 8, 9, 15, 17, 18, 21	6.	2, 3, 3, 4, 5, 6, 7, 8, 9, 9, 11
7.	6, 4, 9, 14, 2	8.	7, 6, 0, 3, 8, 12, 21	9.	6, 2, 4, 7, 9, 4, 6
10.	12, 56, 12, 24, 63, 19	11.	14, 23, 141, 56, 74, 69	12.	85, 23, 45, 39, 111, 109, 161

In Brett's family there are five children. Brett has two sisters who are 5 and 13. He has two brothers who are 8 and 17. Brett is 10 years old.

What is the range of ages in Brett's family? 13.

These children have just had their height measured in centimetres. These were the results.

123, 117, 109, 128, 132, 115

14. What is the range of heights for these children?

Heather likes hamburgers. There are several 'take-away' bars she can buy them from. One day she walked around each 'take-away' bar and checked out the price for a double meat & cheese burger. This is what she found.

\$2.95, \$2.75, \$3.10, \$2.65, \$2.80

- How many 'take-away' bars did she visit? 15.
- What is the range of hamburger prices? 16.
- 17. When buying hamburgers, is cheapest best? What do you think?

The weather has been very changeable lately. The temperature has been up and down. The daily high and low temperatures are listed below ($^{\circ}C$).

Daily high temperatures

Daily low temperatures

[15°C, 13°C, 9°C, 17°C, 27°C, 16°C, 23°C]

9°C, 5°C, 7°C, 11°C, 15°C, 9°C, 15°C

Find the range for the high and low daily temperatures. 18.

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3. 8, 13, 19, 20

8, 0, 23, 14, 7, 14

6.

John

22, 13, 7, 36, 22

Data Calculations: Mean, Median, Mode & Range

Reminder:

The **mean** is the 'average' of all numbers or scores.

The **median** is the middle score, once the scores are in order. The **mode** is the most common score, there may be more than one or none at all. The **range** is the highest score - the lowest score.

Use this information above to work out the following problems.

Task 21

Find the **mean**, **median**, **mode** & **range** for each list of scores below.

5

2.

- 1. 2, 2, 4, 6, 11
- 4. 5, 2, 7, 9, 2

Martin and John both like cricket. During the season they both scored many runs, but who is the better batsman? Each batsman had five turns at bat and scored the following runs. John said, "I'm the better batsman!" Is he correct?

4, 8, 8, 9, 10, 12, 12

9, 6, 8, 12, 3, 8, 10

7. Find the **mean** for both Martin and John's batting scores.

Martin

14, 9, 21, 9, 47

- 8. Find the **median** for both Martin and John's batting scores.
- 9. Find the **mode** for both Martin and John's batting scores.
- 10. Find the **range** for both Martin and John's batting scores.
- 11. Was John correct? Using the information you have calculated above, who is the better batsman? Explain your answer.

Two groups of 10 pupils within a class sat the same test. Their test results are in the boxes. Michelle, who is in Group B, said, " Our group is better as we had three

pupils who got 10 out of 10!" Is Michelle correct?

Group A
7, 4, 4, 6, 5,
5, 9, 7, 8, 5

- 12. Find the **mean** for both test results.
- 13. Find the **median** for both test results.
- 14. Find the **mode** for both test results.
- 15. Find the **range** for both test results.
- 16. Was Michelle correct? Using the information you have calculated above, which of the two groups scored better in the test? Explain your answer.

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Understanding Data Displays:

Look at each data display and use them to answer these questions.

Task 22

This column graph displays the results of the soccer games played by a school team during a season.

- How many games did they win? 1.
- 2. How many games were drawn?.
- What was the total number of games they played? 3.
- 4. If they obtained 3 points if they won, 2 points for a draw and 1 point if they lost, how many points did they score in this season?
- 5. What can you say about their soccer season?

Fruit pupils had for lunch 6. 7. 8. 9. ()

What fruit do you like best? This pictogram shows the fruit that pupils in Mrs. Jacob's class had in their lunch boxes on one day of the week. All pupils had one piece of fruit each.

- Copy and complete the key by naming each fruit.
- How many pupils does each picture represent?
- How many pupils had oranges?
- How many pupils had apples?
- 10. What fruit did 8 pupils have in their lunch boxes?
- 11. How many pupils in Mrs. Jacob's class?

During the Christmas school holidays, a local garden centre ran a tomato growing competition. On the last Friday of the holidays, children brought in the largest tomatoes they had. Each tomato was weighed, to the nearest gram, with the results being displayed in a stem & leaf graph.

- 12. Copy the stem & leaf graph.
- 13. Kim's tomatoes weighed 29, 35, 16 and 40 grams. On your stem & leaf graph, circle the numbers in the leaf part that represent Kim's 4 tomatoes she entered.
- 14. Find the mean (average) weight of Kim's 4 tomatoes.
- 15. List the weights of all tomatoes in order from lightest to heaviest.
- What is the median (middle) tomato weight? 16.
- 17. What was the weight of the winning tomato?
- 18. What is the range of tomato weights?
- 19. What was the most common weight of tomato, also called the mode?
- 20. How many tomatoes were entered in the competition?

Weight of tomatoes (grams)

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'10 Quick Question' results

Days of the School Week

Understanding Data Displays:

Look at each data display and use them to answer these questions.

Task 23

This dot plot graph displays how well Jeremy scored in the '10 Quick Questions' called out at the beginning of each day for two school weeks.

- 1. What was the highest score Jeremy got and on which day?
- 2. On what day did he score 7?
- 3. Work out the range for his scores.
- 4. List the scores in order of lowest to highest.
- 5. What is his median score?
- 6. Calculate the mean of these scores.
- 7. What was the mode or most common score?
- 8. Should Jeremy be pleased with his results? Explain.

trip araph displays the three most popular pets that

MTWTFMTW

This strip graph displays the three most popular pets that the pupils in one class have.

9. How many boxes are in this strip graph?

10

5

٥

Total

in

Test

- 10. How many pets does each box in the strip graph represent?
 - How many pet cats were there?
 - How many pet dogs were there?
 - How many more pet cats were there than pet horses?
- 14. How many pets were there altogether?
 - If 12 pupils each had 2 pets and the other pupils only had 1 pet each, how many pupils are in this class?

Michael has not been well. His temperature has been taken every 30 minutes, starting at 9:00 a.m. This time-series graph shows his temperature readings.

- 16. For how many hours was his temperature taken?
- 17. What was his highest recorded temperature?
- 18. List his temperature readings from lowest to highest.
- 19. What was his median (middle) temperature reading?
- 20. What was the range of his temperature readings?
- 21. What was the mode or most common temperature reading?
- 22. Add up all the temperature readings and use your answer to find Michael's mean or average temperature reading.

Creating Statistical Reports:

Working in groups of 2 or 3, your task is to use the data below to create a statistical report that will prove or disprove a statement. Remember you can create many types of graphs and work out the mean, median, mode or range to use in your report. Finish your report with a conclusion.

SA	L	ES	<u> </u>		
				2	
	2	4			

Task 24

In a recent mathematics competition test for year 5 & 6 pupils, the best pupils at Mairehau Primary scored the following marks. The test was marked out of 20.

St Albans Primary School results

ſ	12,	13,	10,	14,	16,	14,	12,	
	16,	18,	17,	19,	14,	11,	12,	
	15,	14,	16,	17,	12,	13,	10,	
	11,	12,	14,	13,	16,	13,	14,	
	12,	10,	11,	15,	20,	14,	13	
ſ	. '		,			,		

Mairehau Primary School results

15, 14, 13, 10, 18, 19, 19, 16, 17, 15, 16, 13, 12, 15, 16, 18, 17, 16, 17, 16, 19, 19, 15, 16, 14, 16, 14, 17, 15, 14, 18, 16, 14, 18, 19

St Albans School also sat the same mathematics competiton test and the results of their top year 5 & 6 pupils are shown in the box on the left.

Karen, who goes to St Albans School said, "Our school did better than your school in the test as we had someone get 20 out of 20 for the test!"

Is Karen's statement correct or not? Your task is to prove or disprove her statement. Draw at least **TWO** different types of **graphs or tables.** What other calculation can you do?

Task 25

Mr. McGregor is a market gardener who grows vegetables to sell to supermarkets. This year he has been growing two new varieties of carrots. He is unsure as to which variety he should grow next season. Mr. McGregor said, *"I will grow the carrot variety that produces the longer carrots."*

Your task is to use the data below to help Mr. McGregor decide which carrot variety to grow. Draw at least **TWO** different types of **graphs or tables.** What other calculations can you do?

- A coin and a six-sided die (dice) are tossed at the same time. Copy and complete this box, then use it to list all the possible outcomes. coin
- 2. How many possible outcomes are there altogether?

Depending on the weather, Stuart has a choice of wearing shorts or sweatpants, and a t-shirt or skivey.

- 3. What clothes could Stuart wear? Draw a 'box', as in the question above, to help you work out all possible outcomes.
- 4. How many possible outcomes are there?

- In the summer pupils can play either cricket, softball or tennis. In the winter pupils can play either netball or soccer.
- 5. If you can choose one summer and one winter sport, list all possible outcomes by using a 'box' as above.

Н

т

H1

Т4

6. How many possible outcomes are there?

For breakfast Jim can either have cornflakes, ricies or toast to eat. He can have a drink of either milk, juice or milo.

- 7. Draw up a box to help work out all possible outcomes for Jim's breakfast.
- 8. How many possible outcomes are there?

12. What is the least expensive meal?

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Language Associated with Chance:

The likelihood of an event or something happening could be described by using one of the following words ... certain, possible, impossible.

Example:

if this month is June it is certain that next month is July if a ball hits the window it is possible it might break it is impossible to have a birthday on the 30th of February

certain, good chance, even chance, poor chance, impossible.

Other words that could be used are ...

certain, likely, unlikely, impossible

or

Task 28

1. Use the words

certain, likely, unlikely, and impossible,

to write statements about events that you know of, that could be described by using these words.

- Arrange these events in order of likelihood. Put the least likely event first.
 - A If today is Saturday then tomorrow will be Sunday.
 - B It will snow in Whangarei on Christmas Day.
 - C A dinosaur will walk down the street today.
 - D If you toss a coin you will get heads.
 - E A bottle will break when dropped.

Decide if these events are certain, likely, unlikely, possible or impossible.

- 3. It will rain tomorrow.
- 4. The Queen will visit your school tomorrow.
- 5. The sun will rise tomorrow.
- 6. All pupils in your class will be away sick tomorrow.
- 7. Christmas Day will occur on the 25th of December this year.
- 8. It is your birthday tomorrow.
- 9. Tomorrow you will go to the dentist.
- 10. Today it will be dark by 11:00 p.m.
- 11. I will win first prize in Lotto this week.
- 12. Someone in New Zealand will win first prize in Lotto this week.

- 13. A die (dice) is thrown and one comes up
- 14. A die is thrown and a six comes up.
- 15. A die is thrown and an even number comes up.
- 16. A die is thrown and a number less than 5 comes up.
- 17. A die is thrown and a number greater than 5 comes up.
- 18. A coin is tossed and a head comes up.
- 19. Two coins are tossed and two tails come up.
- 20. Two coins are tossed and one is a head, one is a tail.

Using data to Predict Outcomes:

Data that has been collected can be used to make predictions about a group or a population, or anything that the data is about. This can be very useful especially if you run a business.

Example:

A local sports shop recorded the brand of shoes sold in a week. The results are shown in this table.

Tiger	3
Puma	2
Reebok	7
Adidas	3
Nike	5

20 pairs were sold in the week.

From this data we can say, '5 out of 20 shoes sold were Nike shoes'.

What can you say about the other brands?

This information can be used when the shop owner decides how many of each brand to buy, when replacing stock sold.

Task 29

This spinner will always land on a number. The chance of it landing on the number '8' is 1 chance out of 8.

- What is the chance that the spinner will land on 1. an even number?
- What is the chance that the spinner will land on a 2. number greater than 5?
- 3. What is the chance that the spinner will land on a number less than 3?

6 2
6
4
5
7
6

30 pupils were asked to choose their favourite colour from this list.

blue, red, green, orange, white, black

- This frequency table displays their choices.
- Which colour was chosen '2 out of 30' times? 4.
- How many pupils chose green? 5.
- Which colours ended up with the same chance of being selected? 6.
 - '4 out of 30' pupils chose orange. If there were 60 pupils, how many pupils could you expect to choose orange?

School lunches must be ordered early in the day. There is a choice of chicken (CR), ham (HR) or salad (SR) bread rolls, fruit juice (FJ) and flavoured milk (FM). This table shows what was ordered on Monday, using the letter codes above.

Choice of Bread Roll

7.

HR, CR, CR, SR, HR, CR,
HR, HR, CR, SR, HR, SR,
CR, HR, HR, CR, SR, SR
CR, SR, HR, HR, CR, SR,
CR, HR, SR, HR, CR, SR

FM, FJ, FM, FM, FJ, FJ, FJ,	8.
FM, FM, FJ, FM, FJ, FM, FJ,	
FJ, FM, FJ, FJ, FM, FJ, FM,	9.
FJ, FM, FJ, FM	

Choice of Drink

- Draw two tally charts to display their choices.
- How many bread rolls and drinks were sold?
- What is the chance that a pupil had a chicken bread roll? 10.
- 11. What is the chance that a pupil had a flavoured milk drink?
- If 90 pupils ordered a bread roll, how many salad bread rolls would you expect to be sold? 12.
- If 100 pupils ordered a drink, how many fruit juices would the school expect to sell? 13.

'In-class' Worksheet

Teaching Notes & Answers

How to use this section:

Teaching notes are enclosed in a box with a 'push-pin' at the top left corner. The teaching notes precede the answers for each worksheet / task. The teaching notes have been included to provide assistance and background information about each topic or unit of work.

Introduction:

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Worksheet 1

Statistics is concerned with the planning of investigations, the collection, presentation and analysis of quantities of information or data. This information can then be used to draw conclusions or make predictions.

Worksheet 1, **Task 1** is concerned with conducting an investigation. There are some important statistical words that need to be understood.

Survey: A **survey** is a brief or detailed study, whereby data that is collected can be used to do analysis so that conclusions or predictions can be made.

Questionnaire: A **questionnaire** is one way of surveying a population when you are asking opinions about an issue. A good questionnaire has questions that are clear and concise, with not too many questions.

Population: In everyday language the word '**population**' refers to the number of people in a town, city or country. In statistics a 'population' can refer to a group of not just people or animals but a group of anything. *Example:* a population of school desks, a population of trees.

Sample: A **sample** is part of a population you are taking about. A sample of the population is used if the population is very large or if it is not necessary to survey the whole population.

Representative Sample: When we want to make statements about a population, using a survey of a sample of the population, the sample must be a **representative sample**. *Example:* If we wish to find the opinions of pupils in a class that has twice as many girls than boys, then our sample should contain twice as many girls than boys.

Biased Sample: A sample that is not a representative sample is called a **biased sample**.

Once pupils have decided on their investigation topic, the aim of **Task 1** is to encourage pupils to think about what questions should be asked, who should be asked, how they are going to be asked. Producing a simple questionnaire is a good idea. The questions asked and the data collected needs to be done in such a way that it will be easy to do an analysis and draw data displays.

Task 2 is to have pupils present their plan. There are no model answers for Task 1 & Task 2.

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Tally Charts:

Worksheet 2

The use of **tally charts** is an effective way to collect data that is randomly collected, called out or presented in a list. Encourage pupils to count in 'fives' as this makes for easier adding up, marking off each data item as they read from left to right. Searching for all of one type of data, then another type, can result in data being overlooked. The word **frequency** (or total) means how often something occurs.

Task 3 is designed to give practice at creating tally charts and then to use them to answer questions. Note: In the tally charts **F** stands for frequency.

For **Task 4** pupils are to conduct their investigation and present the data in tally charts as appropriate.

Answers: Task 3

Number of pets pupils have 1

No. of pets	Tally	F
0	,IHI,	5
1	₩ĭ.	5
2	, 1 41, 111	8
3	, I II, III	7
4	₩¥.	5
		30

8 pupils had two pets

30 pupils in the class

2.

3.

4. Ways of travelling to school

Ways of travel	Tally	F
bike	, I II TIII,	7
bus	1111	4
car	1111	4
walk	, I III	9
		24

- 5. 9 pupils walked to school
- 7 pupils biked to school 6.
- 7. 24 pupils in the class

Number of caterpillars on each cabbage plant

8.

No. of caterpillars	Tally	F
4	II	3
5	, III , III	7
6		10
7		11
8		8
9		9
10		4
		52

- 9. 7 caterpillars
- 10. 52 cabbage plants

8.

13 pupils

- 2. white cars
- 3. 4 more cars
- 4. red cars
- 5. 35 cars

9. 52 pupils in total, therefore 26 in each class.

Answers: Task 7

- 1. Pets pupils like in Jacqui's class
- 2. 27 pupils

3. 15 rainy days in June

Answers: Task 9

1. 7, 9, 3, 5, 15, 16, 12, 10, 16, 19, 22, 26, 27, 23, 21, 32, 30

22, 20, 29, 25, 23, 24, 39, 35, 34, 37, 36, 33, 31, 48, 42, 47, 40, 56, 52, 57, 59, 50 2. 17 pupils in the class 3. 59 minutes, 20 minutes

4.

5.

6.

Answers: Task 10

1. Money spent on 'take-aways' (\$)

- 0 9, 8, 1 2, 6, 2, 3, 7, 4, 7, 4, 9, 6, 2, 1 2 4, 1, 9, 2, 5, 0
- 2. \$8.00
- 3. 20 families

Test results for first test

- 2 8, 7, 6, 7, 8, 5, 4, 8, 9, 4 3 7, 1, 7, 9, 1, 4, 9, 6, 7, 9, 1, 5, 7, 0 4 1, 1, 2, 2
- lowest mark = 24, highest mark = 42

Test results for second test

NOTE: you could draw a back-to-back stem & leaf graph for these two tests results. 2 9, 9 3 6, 9, 8, 7, 2, 9, 7, 6, 2, 7, 0, 7, 4 4 2, 8, 6, 5, 6, 1, 8, 6, 6, 6, 0, 6 7. lowest mark = 29, highest mark = 50

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- 8. At least 50, but not really possible to say for sure.
- 9. YES, the class did better in the second test. There are more scores in the 40's and one in the 50's. Both the new low and high marks have improved.

A strip graph is also known as a bar graph or percentage bar graph. At this level it is too difficult for pupils to work out percentages to be shaded, so the strip graph has been divided into squares, with each square representing a certain number of data scores. *Example:* one square = 5 people All strip graphs should have ...

a title or name

a scale stating how much each picture is worth

Task 12 is designed to assist pupils to understand strip graphs.

□ a key

Task 13 is designed to give practice at creating strip graphs, then to use them to answer questions.

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Finding the 'Average'

Worksheet 9, 10, & 11

There are **three different types of 'averages'** that can be worked out, depending on what information you require from your data.

The **mean** is commonly known as the 'average'. To find the mean, add up all the scores, then divide by the number of scores. *Example:* Find the mean of 4,7, & 10: 4 + 7 + 10 = 21, $21 \div 3 = 7$ Not all answers will be whole numbers.

The **median** is the middle score, once the scores are in numeric order. If there is an odd number of scores, cross one off each end until there is only the middle score left. If there is an even number of scores then the median is halfway between the two scores left in the middle.

Example: 1, 6, 8, 9, 10 has a median of 8: 5, 8, 10, 12 has a median of 9 (halfway between 8 & 10) The **mode** is the most common score. There can be more than one mode or none at all.

Example: 2, 2, 4, 6, 8 has a mode of 2: 4, 4, 5, 8, 8, 9 has a mode of 4 & 8: 5, 8, 9, 10 has no mode

Which 'average' to use?

Example: For test results the mean may be helpful. If a class is to be divided into two groups based on their ability, the median would be useful. A shop-keeper would use the mode when replacing jeans sold.

Task 17 is designed to give practice at working out the mean and using this to explain results.

Task 18 is designed to give practice at working out the median and using this to explain results.

Task 19 is designed to give practice at working out the mode and using this to explain results.

A	nswers: '	ſask	17								
1.	7	2.	13	3.	15	4.	7	5.	10	6.	5
7.	9	8.	12	9.	30	10.	9	11.	8	12.	6
13.	12 pupils	14.	3 books	15.	Yes, Mr St books. All	evenso pupils,	on would be p except one,	oleased read a	d as the clas at least 2 boo	s mear oks.	was 3
16.	It should b	e as th	ere were ma	any sco	res of 7, 8 &	9.					
17. be	mean = 6, done agair	Mr. Si า.	tevenson wo	uld not	be pleased a	as the i	mean was be	elow 7,	therefore th	e test v	vill have to
A	nswers: '	Fask	18								
1.	8	2.	6	3.	13	4.	6	5.	15	6.	6
7.	6	8.	6	9.	5	10.	6	11.	8	12.	7
13.	11	14.	16	15.	7.5	16.	5	17.	9	18.	10.
19.	34m	20.	7 glasses	of lemo	onade						
A	nswers: '	ſask	19								
1.	3	2.	6	3.	6&7	4.	no mode	5.	8, 9, 10	6.	7
7.	2. 3. 4	8.	6	9.	no mode						

10.

T-Shirts sold

T-shirt size	Tally	F	
8	₩¥	5	
10	JWY II	7	
12	,₩¥	5	
14	I	1	
		18	

- 11 size 10 t-shirt
- The shop-keeper can use this information to assist when reordering new 12. stock to replace the t-shirts sold. He may also want to buy more of the most popular sizes, so he does not run out of stock.
- 20 & 36 minutes 13.

nan	iye						
The	range	for	а	set	of	data	s

Danga

Worksheet 12

Worksheet 13

cores indicates how spread out the scores are. The range is calculated as follows.

Range = highest score – lowest score

Why work out the range?

Example: Compare the two sets of scores.

& 10, 20, 30, 40, 50 28, 29, 30, 31, 32 Both sets of scores have a mean and median of 30, **BUT** the ranges are 50 - 10 = 40 & 32 - 28 = 4. If these were test results the range would be helpful, as it indicates the range of pupil ability, for this test.

Task 20 is designed to practice working out the **range** and using this information to explain results.

Answers: Task 20

-											
1.	5	2.	5	3.	15	4.	8	5.	15	6.	9
7.	12	8.	21	9.	7	10.	51	11.	127	12.	138
13.	12 years	14.	23cm	15.	5 take-awa	ay bars		16.	45 cents		
4 —						· · ·		• •			

Cheapest may not be best. What the hamburgers taste like is more important. 17.

18. Range for high temperatures was 18°C. Range for the low temperatures was 10°C.

Mean, Median, Mode & Range

By calculating all or some of the above, informed statements can be made about a set of data scores.

Task 20 is designed to give practice at working out the mean, median, mode & range and using this information to explain results.

Answers: Task 21

- 1. mean = 5, median = 4, mode = 2, range = 9
- 3. mean = 15, median = 16, no mode, range = 125. mean = 8, median = 8, mode = 8, range = 9 Martin's scores John's scores
- 7. mean = 20 runsmean = 20 runs
- median = 14 runs8
- median = 22 runs9. mode = 9 runsmode = 22 runs
- range = 38 runs 10. range = 29 runs
- Group A Group B 12. mean = 6mean = 5
- 13. median = $5\frac{1}{2}$ median = $3\frac{1}{2}$
- 14 mode = 5mode = 10
- 15. range = 5range = 9

- 2. mean = 9, median = 9, mode = 8 & 12, range = 8
- 4. mean = 5, median = 5, mode = 2, range = 7
- mean = 11, median = 11, mode = 14, range = 23 6.
- 11. John was correct. They both had the same mean but John had the better median and mode. Although Martin had the highest score, John's scores were more consistent as the range was less spread out.
- 16. Michelle's statement was incorrect. Group A may not have had anyone who scored 10 out of 10, but their mean and median were higher than that of Group B. Group A had a narrower range indicating this group was of similar ability, whereas Group B had a range of 9. The mode of 10 for Group B does not reflect the overall ability of this group.

Worksheet 15

Creating Statistical Reports

Having completed all the preceding tasks, pupils are now ready to give a full **statistical report** using some of the many skills they have learnt.

In **Tasks 24 & 25**, pupils have been given two sets of data and a statement about the data. Pupils are to decide which graphs they are going to create. Calculations involving either the mean, median, mode or range could be done. From the graphs drawn and the calculations done, pupils are to prove or disprove each statement, In other words they are to write a **statistical report**.

Answers: Task 24

Mairehau Primary School results

Test mark	Tally	F
10	I	1
11		0
12	I	1
13	II	2
14	HH.	5
15	₩ I	5
16	111T III	8
17		4
18		4
19	HHI.	5
20		0

Calculating the mean for this data would be difficult at this level, however the Mean = 15.9

Scores in order

10, 12, 13, 13, 14, 14, 14, 14, 14, 15, 15, 15, 15, 15, 16, 16, 16, 16, 16, 16, 16, 16, 16, 17, 17, 17, 17, 18, 18, 18, 18, 19, 19, 19, 19, 19 Median = 16, Mode = 16, Range = 9

Test mark	Tally	F
10	III	3
11	III	3
12	HHT I	6
13	HH.	5
14	₩T II	7
15	II	2
16	1111	4
17	II	2
18	I	1
19	I	1
20	I	1

St Albans Primary School results

Calculating the mean for this data would be difficult at this level, however the Mean = 13.8

Scores in order 10, 10, 10, 11, 11, 11, 12, 12, 12, 12, 12, 12, 13, 13, 13, 13, 13, 14, 14, 14, , 14, 14, 14, 14, 15, 15, 16, 16, 16, 16, 17, 17, 18, 19, 20 Median = 14, Mode = 14, Range = 10

Looking at the tally chart and the column graphs for the two test results, it appears that Karen's statement about St Albans Primary School performing better than Mairehau Primary School is **incorrect**.

Calculations of the mean, median, mode and range support the fact that Mairehau Primary School did in fact score better in the test.

Looking at the dot plot graphs and the stem & leaf graphs, carrot variety A has more longer carrots. Calculations of the mean and median support this fact. Both carrot variety A & B had the same mode and a similar range. Mr. McGregor should plant carrot variety A.

Exploring Probability: Finding Outcomes

Worksheets 17 & 18

Probability is a measure of how likely it is that an event will happen. The rolling of a die, the drawing of a card etc. are **experiments**. An **outcome** is the **result** of an **experiment**. Finding all possible outcomes can be done in several ways. Two ways to do this are using **'boxes'** and **'tree diagrams'**. By using either of these two methods you are more likely to obtain all outcomes.

Tasks 26 & 27 are designed to give practice at finding outcomes using a systematic method, such as the 'box' or 'tree diagram' method.

3.

Answers: Task 26

1	
	•

Six-sided die (dice) 1 2 3 4 5 6 **H1** H2 H3 H5 H6 н H4 coin Т Τ2 Т4 T5 Т6 Т1 Т3

t-shirtskiveyshortsshorts/t-shirtshorts/skiveysweatpantssp/t-shirtsp/skivey

Outcomes:

H1, H2, H3, H4, H5, H6, T1, T2, T3, T4, T5, T6

2. 12 outcomes

- Outcomes: shorts/t-shirt, shorts/skivey, sweatpants/t-shirt, sweatpants/skivey
- 4. 4 outcomes

5.

4.

	cricket (C)	softball (SB)	tennis (T)
netball (N)	N/C	N/SB	N/T
soccer (SR)	SR/C	SR/SB	SR/T

Outcomes:

netball/cricket, netball/softball, netball/tennis soccer/cricket, soccer/softball, soccer/tennis

6. 6 outcomes

Answers: Task 27

- 1. toast/soup, toast/cheese, bread/soup, bread/cheese
- 3. R = red. B = blue

- red/red/red, red/red/blue, red/blue/red, 5. red/blue/blue, blue/red/red, blue/red/blue, blue/blue/red. blue/blue/blue
- 6. 8 outcomes
- 8. 12 possible choices or outcomes
- 3 choices 9.
- 10. 3.50 + 16.50 + 5.00 = 25.00
- 11. \$3.50 + \$17.50 + \$5.00 = \$26.00
- \$2.75 + \$15.00 + \$4.50 = \$22.25 12.

Ÿ

3.

7.

10.

13.

17.

milk (MK) juice (J) milo (MO) cornflakes (C) C/MK C/J C/MO R/MK R/J R/MO ricies (R) toast (T) T/MK T/J T/MO

Outcomes:

cornflakes/milk, cornflakes/juice, cornflakes/milo ricies/milk, ricies/juice, ricies/milo, toast/milk, toast/juice, toast/milo

8. 9 outcomes

2. 4 outcomes

7. Let S = soup, G = garlic bread, C = chicken, F = fish, T = t-bone steak, I = ice-cream A = apple pie

Worksheet 19

Language Associated With Chance Many words can be used to describe the chance of something happening. Words such as certain or impossible are at the extremes. There are a number of words, likely, unlikely, possible, even chance, poor chance, good chance, that can be used to describe events that occur between these extremes.

Task 28 is designed to give practice at using words to describe events, to help pupils gain an understanding of what simple probability is.

Answers: Task 28

1.	-		2.	C, B, D, E, A	
For	questions	3 to 12 th	ere may	y be more than o	ne answer.

11.

14.

18.

poor chance

even chance

ions 3 to	12 there may	be more th
sible	4.	impossible

- possible certain 8.
- 5.
- certain certain or impossible 9.
 - certain or impossible, unlikely
- impossible, possible but unlikely 12. possible or likely
 - 15. even chance 19. poor chance
- 16. good chance 20. even chance

unlikely or possible

6.

certain

poor chance

poor chance

R В R

3rd marble

R

В

В

R

В

Worksheet 20

Using Data To Predict Outcomes

Being able to predict outcomes can be useful. Imagine if you could predict the outcome of Lotto this week! If a sample of a population is surveyed, the outcome of the survey can be used to make predictions about the whole population. If you conduct an experiment, the results of the experiment can also be used to make predictions.

Task 29 is designed to introduce the idea of 'chance' and how this can be used to make predictions. Also practice at making predictions by working out the outcomes for a given situation and applying the chance of an outcome occurring, to making predictions about the situation. *Example:* 4 out of 10 people like apples. If there were 100 people, how many would you expect to like apples?

Answers: Task 29

1. 4 out of 8

8.

6. blue and white 7. 8 pupils

2.

3 out of 8

3. 2 out of 8

5.

5. 5 pupils

Bread Roll	Tally	F
chicken	HIT HIT	10
ham	HAL HAL I	11
salad		9
		30

Drinks	Т	ally		F
fruit juice	łłł	₩ł	III	13
flavoured milk	łłł,	₩ł	II	12
				25

- 9. 30 bread rolls and 25 drinks
- 12. 27 salad rolls

- 10. 10 out of 30 13. 52 fruit juices
- 11. 12 out of 25

black

4.

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Table of Content for the Homework / Assessment Worksheet Masters for Statistics, Level 3

Worksheet Number	Торіс	Statistics Objective(s)
1	Planning an investigation / Tally Chart	S1 / S2
2	Column Graphs / Pictograms	S2
3	Stem & Leaf Graphs / Dot Plot Graphs	S2
4	Time-Series Graphs / Strip Graphs	S2
5	Mean, Median, Mode & Range	S3
6	Interpreting Data / Statistical Reports	S3 / S4
7	Listing Outcomes: 'Box' & Tree Diagrams	S5
8	Language of Chance / Predicting Outcomes	S2 / S6
	Answers	

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		alist	-101		
	omework	/ Assessme	ent Wor	ksheet	
		/ 1100000111			
Name:		Class		Complete by	y:
A: 10 'Quick Quest	ions'	B: Mean	n, Mediar	n, Mode & I	Range
1. 51.6 + 9.7 =	Fill in	the missing word	s from the b	, box, to comple	te these sentences
2. 14.75 - 6.34 =	1.	To find the 'aver	age' or		for a list of
3. 157 × 20 =		scores, first ad	1 up all the s	scores, then d	ivide by the
4. 440 ÷ 11 =		number of score	s you added	up.	
5. Convert 1.5m to cm	2.	The middle score	e, once the s	cores are plac	ed in order from
		smallest to bigge	est, is called	the	
6. \$6.40 ÷ 8 =	3.	The most commo	n score is co	alled the	
7. What is	12	There may be may	ore than one	or none at all.	
the time in	2 4.	The highest scor	re — lowest:	score is called	the
on this	4	range	mode	median	mean
CIOCK? 7	6 5	C	• Finding	the Mean	
8 Find $\frac{1}{2}$ of \$450	 Find ·	the mean for ea	ch list of sci	ores	
	1	6 8 10		2 558	3 10
9. How many milligram	s in 3.	2, 7, 3, 4, 6, 2		4. 3.6.4	, <u>2</u> , 1, 3, 2
5 grams?		12, 10, 8, 14		6. 5,102	, 64, 29
10. If 6 books cost \$13	.80,				
what does one book	cost?	D :	Finding	the Mediar	1
	Find	the median for	each list of	scores.	T E
F. Finding the Ra	nge 1	mber the scores	must be in oi	rder.	• 10 12
Find the range for these	ists of 2	D, D, D, 9, 12	•••••		7, 10, 12 17 20
scores	5 5 5	36729	•••••	4. 10, 15	, 17, 20 median =
1. 2.6.8.9.12		5, 0, 7, 2, 7	•••••, •••••, •••	,,	median =
2. 15, 3, 0, 8, 7		0, 1, 7, 0, 7, 10	,,	····, ····, ····, ····, ····	
3. 6, 3, 4, 8, 12, 21			: Finding	; the Mode	
4. 12, 36, 19, 24, 15	Find	the mode for ea	ch list of sco	ores.	
5. 57, 36, 17, 81, 47	1.	2, 2, 4, 6, 8, 7	•••••	2. 6, 5, 3	3, 6, 4, 5
6. 36, 45, 12, 8, 24	3.	2, 10, 9, 5, 1	4.	3, 6, 8, 3, 4,	, 6, 4
7. Five cars were sold	for 5.	3, 3, 5, 6, 7, 9, 6		6. 1, 6, 7	7, 2, 3, 9, 7
the following prices	: >	G. W	ord Probl	ems	(O.L.
\$8500	Tn th	e first nine holes	of and the	f recorded th	
\$12950	follov	vina scores	5658	95457	
\$7250		Find his mean so	(0, 0, 0, 0)	, e, e, i, e, i	CE SAIN
\$18420	2.	What was the ran	ge of his sco	ores?	E D
p9990 area	of the 3.	What was the mo	de score?		
car prices	01 me 4.	List the scores fro	om lowest to	highest.	0
8. If the cheanest car	sells 5.	What was the me	dian for his a	,,,, . olf scores?	·····, ·····
for \$8000 and the	range In the	next nine holes J	eff recorded	the following s	cores
of car prices is \$75	ioo,		5, 3, 9, 8	, 4, 6, 7, 5, 6	
what would the mos	t _	Combine the two	ente of nine	scores to find t	he new median
expensive car sell f	or?				
	人	,,,	<u> </u>	New median	=,
Comments:					Please sign: Parent / Caregiver
AWS				1 / @	

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Homework / Assessment Worksheet

Answers

Worksheet 1

A:

1. 1302 2. 437 3. 1125 4. 60 5. 230mm 6. \$20.00 7. 20 past 8 8. \$2.40 9. 2000m 10. \$11.25

B:

- 1. Parents / caregivers need to give permission. They may have to pay towards the cost of the trip and / or help with transport and come along as parent help.
- other classmates, teachers, friends or in fact anyone who might know of good places to visit on a class trip. The principal, as he/she will need to give permission as well as perhaps the BOT.

Number red

jellybeans

7

8

9

10

11

12

33 packets

3. Where should we go? (3 or 4 choices) Will the trip be ½ day or full day?

Will we combine the trip with another class? etc. etc.

D:

1.

2.

C:

4

1.		
Number of children	Tally	Total or Frequency
1	HHT III	8
2		12
3	₩¥ I	6
4	III	3

2. 12 families

Worksheet 2

A:

1. 993 2. 522 3. 1464 4. 60 5. 25cm 6. \$26.60 7. 20 to 4 8. \$1.35 9. 5km 10. \$10.80

B:

1. Friday 2. 9 hours 3. Tuesday, as the temperature was only $2^{\circ}C$

snowing =

- 1. Number of cats and dogs living in one street.
- 2. 16 cats

D:

E:

1.

2. 6

F

5

3

9

7

4

5

Tally

١

ш

₩t IIII

₩**1** ||

1111

١Ħ

Test

Results

4

5

6

7

8

9

3. 33 pupils

F

4

7

10

7

3

2

Tally

1111

₩**†** ||

HHT ||

ш

п

HH HH

3. 10 dogs

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cloudy =

videos =

A:

1. 61.3 3. 3140 4.40 5. 150cm 6. \$0.80 7. 25 to 10 8. \$2.25 9. 5000mg 2. 8.41 10. \$2.30 **B**: 1. mean 2. median 3. mode 4. range C: 1.8 2.7 3. 4 4.3 5. 11 6.50 D: 5. 2, 3, 6, 7, 9 median = 6 6. 1, 3, 5, 7, 9, 10 median = 6 1.8 2.9 3.9 4. 16 **E**: 1. 2 4.3,4&6 2.5&6 3. no mode 5.3&6 6.7 F: 6. 37 1. 10 2. 15 3. 18 4. 24 5. 64 7. \$11170 8. \$15500 G: 1. 6 2. 5 3. 5 4. 4, 5, 5, 5, 5, 6, 7, 8, 9 5. 6 6. 3, 4, 4, 5, 5, 5, 5, 5, 5, 6, 6, 6, 7, 7, 8, 8, 8, 9 new median = $5\frac{1}{2}$

Worksheet 6

A:

B:

1. 5.83 2. 8.5 3. 2025 4. 3.1 5. 5m 6. \$73.35 10. \$1.30

Possible comments:

12 girls chose cats, 6 boys chose cats, 10 girls chose dogs, 12 boys chose dogs, more boys than girls chose dogs, more girls than boys chose cats, there are 40 pupils in these two classes, etc.

C:

1. Simon's batting scores: mean = 15 runs, median = 11, no mode, range = 28 Mark's batting scores: mean = 17.5 runs, median = 17, no mode, range = 26

Mark has a better mean and median, therefore Mark was the better batsman.

D:

Possible comments:

The furtherest throw was 63m, the shortest throw was 26m, the median was 41m, the range was 37m, there was no mode, the mean was 42m

E:

Rebecca's daily results were 9, 10, 9, 8 & 9, with a mean of 9, a median of 9, a mode of 9 and range was 2. Wendy's daily results were 7, 6, 10, 7, 10, with a mean of 8, a median of 7, a mode of 10 and range of 4. While Wendy scored two 10 out of 10 scores, Rebecca's results were more consistent, with a better mean, median and range. Wendy's statement is incorrect.

Worksheet 7

A:

D:

(blue socks, sports shoes), (blue socks, leather shoes), (blue socks, canvas shoes), (red socks, sports shoes), (red socks, leather shoes), (red socks, canvas shoes), (black socks, sports shoes), (black socks, leather shoes), (black socks, canvas shoes)
 9 combinations

E:

 Let S = St Albans School and M = Mairehau School Let Mo = Monday, Tu = Tuesday, Th = Thursday and Fr = Friday

	Monday	Tuesday	Thursday	Friday	_
St Albans	S/Mo	S/Tu	S/Th	S/F	ĺ
Mairehau	M/Mo	M/Tu	M/Th	M/F	

2. 8 possible outcomes or combinations

Worksheet 8

A:

8. \$9.30

5.

unlikely

1. 28.25 2. 7.6 3. 17220 4. 1500 5. 2300mm 9. 2.7kg 10. \$2.95

B:

1. unlikely 2. possible, likely or certain 3. certain 4. possible but certain or impossible

6. C, B, A, Ė, D

C: 1.

5.

WeatherTallyTotal40 milkshakes2.15 out of 403.vanilla4.16 banana milkshakes6.30 days7.9 out of 308.cool weather

6. \$62.70

Weddilei	Tuny	Total
hot	₩ † III	9
warm	₩ †	7
cool	H #	5
cold	₩ * I II	9

. 30 days 7. 9 out of 30 8. cool weather

7.

D:

1. 1 = 7, 2 = 6, 3 = 8, 4 = 6, 5 = 5, 6 = 8 2. 6 out of 40 3. zero out 40

	Comments								
Worksheet	Objectives								
20	S2 / S6								
19	S5								
18	S5								
17	S5								
16	S3 / S4								
15	S3 / S4								
14	S3 / S4								
13	S3 / S4								
12	S3 / S4								
11	S3 / S4								
10	S3								
9	S3 / S4								
4	S2 / S3								
7	S2								
6	S2 / S3								
5	S2 / S3								
4	S2								
ũ	S2								
2	S2								
1	S1								
Statedice	Name								

Tracking Sheet: 'In-class' Activity Sheets

		Tracking Sheet:				et: I	Homework /			Assessment			Worksheets			
	Comments															
Worksheet	Objectives															
7	S5															
6	S3 / S3															
5	S2															
4	S2															
3	S2															
2	S2															
1	S1 / S2															
Statedics	Name															